

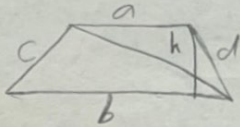
بسمه تعالی

موسسه مالی و اعتباری ثامن الحجج (ع)
(تحت نظارت بانک مرکزی)

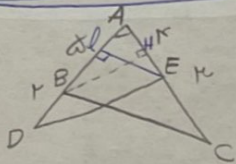


تاریخ:
شماره:
پیوست:

(X) - 1



$$\frac{(a+b)h}{2} = 25$$



$$S_{ABC} - S_{ADE} = 1 \sqrt{5}$$

$$v \times lE - v \times BH = 1 \sqrt{5}$$

$$v(lE - BH) = 1 \sqrt{5} \rightarrow lE - BH = \frac{1}{v}$$

$$lE = BH + \frac{1}{v}$$

$$\frac{BH}{AH} = \frac{lE}{Al}$$

(X) - 2

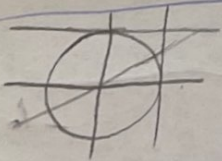
$$\frac{1}{\tan \alpha} - \frac{\sin \alpha}{\cos \alpha} = \frac{1 + \sin \alpha}{\tan \alpha} \rightarrow \cos \alpha - \sin \alpha = 1 + \sin \alpha$$

$$2 \sin \alpha = \cos \alpha - 1 \rightarrow \boxed{\cos \alpha > 0}$$

نقصی است

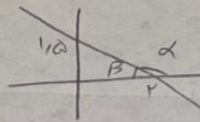
$$\frac{|\sin \alpha|}{\cos \alpha} = -\frac{\sin \alpha}{\cos \alpha} \rightarrow \boxed{\sin \alpha < 0} \rightarrow \boxed{\alpha \text{ در ربع سوم}}$$

در ربع دوم



$$\tan \alpha = \tan(\pi + \alpha)$$

$$\tan \alpha = -\tan(\pi - \alpha)$$



$$\tan \beta = -\tan \alpha$$

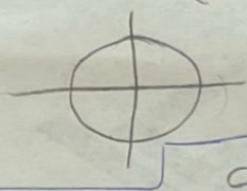
$$\tan \beta = \frac{1 \sqrt{5}}{1} = \boxed{1 \sqrt{5}}$$

$$\boxed{\tan \alpha = -1 \sqrt{5}}$$

$$\Rightarrow \tan\left(\frac{\pi}{2} - \alpha\right) = +\cot \alpha \rightarrow \boxed{\cot \alpha = -\frac{1}{1 \sqrt{5}}}$$

- 3

$$\frac{r \cos(\frac{\pi}{r} - \pi) - r \sin(\pi - \pi)}{\sin(\pi + \pi) - \cos(\frac{\pi}{r} + \pi)} = \frac{-r \sin \pi - r \sin \pi}{-\sin \pi - \sin \pi} = \frac{-0 - r}{-(-r)} = \boxed{\frac{d}{r}}$$

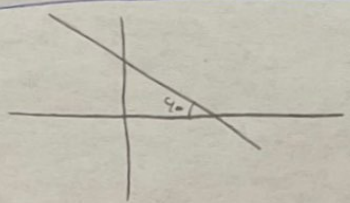


$$\cos \alpha = \frac{r}{r} \rightarrow \sin^2 = 1 - \cos^2$$

$$1 - \frac{r}{r} = \frac{d}{r} \rightarrow \sin \alpha = \frac{\sqrt{d}}{r} \rightarrow \tan \alpha = \frac{\frac{\sqrt{d}}{r}}{\frac{r}{r}} = \frac{\sqrt{d}}{r}$$

$$\frac{\cos \alpha + \sin \alpha}{|\tan \alpha - 1|} = \frac{\frac{\sqrt{d}}{r} + \frac{r}{r}}{\frac{1}{r}} = \frac{r(\sqrt{d} + r)}{r} = \boxed{\frac{r + r\sqrt{d}}{r}}$$

$$\sin \alpha + \cos \alpha \rightarrow \sin^2 + \cos^2 = 1 \rightarrow \cos \alpha \leq 1 \rightarrow \boxed{\cos \alpha = \frac{1}{\sqrt{2}}}$$



$$(m^2 - 1)y = -rmx + r \rightarrow y = \frac{-rm}{m^2 - 1}x + \frac{r}{m^2 - 1}$$

$$\tan \alpha = \frac{\sqrt{r}}{r} = \frac{-rm}{m^2 - 1} \rightarrow -4m = \sqrt{r}m^2 - \sqrt{r}$$

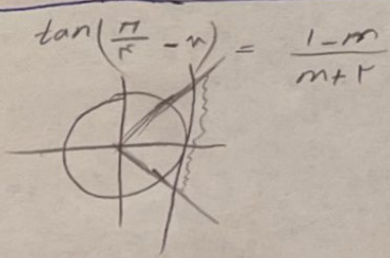
$$\sqrt{r}m^2 + 4m - \sqrt{r} = 0$$

$$m^2 + 4m - r = 0 \rightarrow \frac{-4 \pm \sqrt{16 + 4r}}{2} = -2 \pm \sqrt{4 + r}$$

$$\frac{-r \pm r\sqrt{r}}{\sqrt{r}} \rightarrow \frac{-r + r\sqrt{r}}{\sqrt{r}} = -\sqrt{r} + r = m_1$$

$$\frac{-r - r\sqrt{r}}{\sqrt{r}} = -\sqrt{r} - r = m_2$$

$$m_1 - m_2 = r - \sqrt{r} + r + \sqrt{r} = \boxed{2r}$$



$$\tan(\frac{\pi}{r} - \alpha) = \frac{1 - m}{m + r}$$

$$\alpha = -\frac{\pi}{r} \rightarrow \tan \frac{\pi}{r} = \dots$$

$$\alpha = \frac{\pi}{r} \rightarrow \tan 0 = 0$$

$$\alpha = 0 \rightarrow \tan \frac{\pi}{r} = 1$$

$$\boxed{\frac{1}{r} < m < 1}$$

$$0 < \frac{1 - m}{m + r} < 1 \quad \frac{-1}{r} < m$$

$$1 - m < m + r \rightarrow -1 < r + m$$

$$0 < 1 - m \rightarrow m < 1$$

$$\tan(\frac{r\pi}{r} + \pi) \cos(\pi + \pi) + \tan(\frac{d\pi}{r} + \pi) \sin(\frac{d\pi}{r} + \pi)$$

$$(-\cot \pi - \cos \pi) + (-\cot \pi + \cos \pi)$$

$$\frac{\cos \pi}{\sin \pi} - \frac{\cos \pi}{\sin \pi} = \boxed{0}$$