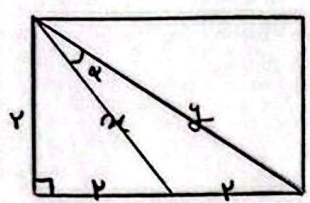


$$S = \frac{1}{2} ab \sin \alpha \rightarrow \text{فد} = \frac{1}{2} \times \sqrt{2} \times \sqrt{2} \times \sin \alpha \rightarrow \sin \alpha = \frac{\sqrt{2}}{2}$$

$$\rightarrow \alpha_1 = \frac{\sqrt{2}}{2} \quad \therefore \alpha_2 = \frac{\pi}{4}$$

$$\frac{\alpha_{\max}}{\alpha_{\min}} = \frac{\frac{\sqrt{2}}{2}}{\frac{\pi}{4}} = \boxed{\sqrt{2}}$$

1



$$x^2 = 1 + 1 \rightarrow x = \sqrt{2} \rightarrow m = \sqrt{2}$$

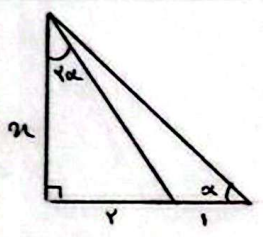
$$y^2 = 1 + 1 = 2 \rightarrow y = \sqrt{2}$$

$$c = \sqrt{a^2 + b^2 - 2ab \cos \alpha} \rightarrow 2 = \sqrt{1 + 1 - 2 \cos \alpha}$$

$$\Rightarrow 2 = 2 - 2 \cos \alpha \rightarrow \cos \alpha = \frac{1}{\sqrt{2}} \rightarrow \sin \alpha = \frac{1}{\sqrt{2}}$$

$$\cot \alpha = \frac{\cos \alpha}{\sin \alpha} = \frac{\frac{1}{\sqrt{2}}}{\frac{1}{\sqrt{2}}} = \boxed{1}$$

2



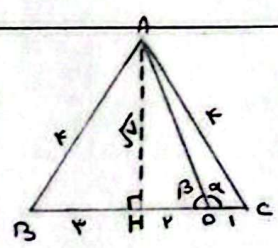
$$\left. \begin{array}{l} \cot \alpha = \frac{m}{n} \\ \cot \alpha = \frac{m}{n} \\ \tan \alpha = \frac{n}{m} \end{array} \right\} \rightarrow \cot \alpha - \tan \alpha = 2 \cot \alpha$$

$$\Rightarrow \frac{m}{n} - \frac{n}{m} = m \rightarrow \frac{m^2 - n^2}{mn} = m \rightarrow m^2 - n^2 = m^2 n$$

$$\rightarrow n^2 = \frac{m^2}{m} \rightarrow n = \frac{m}{m} = \boxed{1}$$

$$\Rightarrow \cot \alpha = \frac{m}{n} = \frac{m}{1} = \boxed{m}$$

3



$$\triangle AHB : AB^2 = AH^2 + BH^2 \rightarrow AH = \sqrt{2}$$

$$\left. \begin{array}{l} BC = 2 \\ \text{مستوی} \\ \text{الساكن} \end{array} \right\} \rightarrow BH = CH = 1$$

$$\tan B = \frac{AH}{OH} = \frac{\sqrt{2}}{1} \xrightarrow{\text{مقابل } \beta \text{ و } \alpha} \tan \alpha = -\tan \beta = \frac{-\sqrt{2}}{1}$$

4

$$2 \sin^2 m + \cos^2 m = \frac{1}{2} \rightarrow \sin^2 m + \underbrace{\sin^2 m + \cos^2 m}_{=1} = \frac{1}{2} \rightarrow \sin^2 m = \frac{1}{4}$$

$$\cos^2 m = 1 - \sin^2 m = 1 - \frac{1}{4} = \frac{3}{4}$$

$$\tan^2 m = \frac{\sin^2 m}{\cos^2 m} = \frac{\frac{1}{4}}{\frac{3}{4}} = \boxed{\frac{1}{3}}$$

5

$$\frac{\sin^2 \alpha + r \cos \alpha}{1 + \cos \alpha} - \frac{\cos^2 \alpha + r \sin \alpha}{1 + \sin \alpha} = \frac{\sin^2 \alpha - r \sin \alpha + r}{r - \sin \alpha} - \frac{\cos^2 \alpha - r \cos \alpha + r}{r - \cos \alpha}$$

$$= \frac{(\sin^2 \alpha - r)^r}{r - \sin \alpha} - \frac{(\cos^2 \alpha - r)^r}{r - \cos \alpha} = -\sin^2 \alpha + r - r + \cos^2 \alpha = \cos^2 \alpha - \sin^2 \alpha = \frac{1 + \cos 2\alpha}{2} - \frac{1 - \cos 2\alpha}{2}$$

$$= \boxed{\cos 2\alpha}$$

$\tan \alpha = \frac{r}{q} \xrightarrow{\frac{p}{q}}$ $\cos \alpha = \frac{1}{1 + \frac{14}{q}} = \frac{q}{r+14} \rightarrow \cos \alpha = \frac{-r}{2}, \sin \alpha = \frac{-r}{2}$

$$\frac{\sin\left(\frac{9\pi}{r} + \alpha\right)}{\cos \alpha} \frac{\cos\left(\frac{7\pi}{r} - \alpha\right)}{-\sin \alpha} - \frac{\tan\left(\alpha - \frac{7\pi}{r}\right)}{-\cot \alpha} = -\sin \alpha \cos \alpha + \frac{\cot \alpha}{\frac{\cos \alpha}{\sin \alpha}} = \frac{\cos \alpha (1 - \sin^2 \alpha)}{\sin \alpha}$$

$$\Rightarrow \frac{\cos^2 \alpha}{\sin \alpha} = \frac{\left(\frac{-r}{2}\right)^r}{\frac{-r}{2}} = \boxed{\frac{r^r}{100}}$$

$\alpha = \frac{\pi}{17} = 18^\circ$

$$\frac{r \cos \frac{\pi}{r} + \sqrt{r} \sin \frac{\pi}{r} - \sqrt{r} \cos \frac{\pi}{r}}{r \cos \frac{\pi}{r}} = \frac{r \cos 4^\circ + r \sin (-4^\circ)}{\sqrt{r} (\sin \frac{\pi}{r} - \cos \frac{\pi}{r})} = \frac{r \times \frac{1}{r} - r \times \frac{1}{r}}{\sqrt{r} \sin\left(\frac{\pi}{r} - \frac{\pi}{r}\right)} = \boxed{\frac{1}{r}}$$

$\tan\left(\frac{\alpha}{r}\right) = \frac{1}{r}$

$\tan \alpha = \frac{r \tan\left(\frac{\alpha}{r}\right)}{1 - \tan^2\left(\frac{\alpha}{r}\right)} = \frac{r \times \frac{1}{r}}{1 - \frac{1}{r^2}} = \frac{\frac{1}{15}}{1 - \frac{1}{14}} \rightarrow \cos \alpha = \frac{18}{19}, \sin \alpha = \frac{1}{19}$

$$\frac{\tan \alpha - \sin \alpha}{\sin \alpha - \cos \alpha} = \frac{\frac{1}{18} - \frac{1}{19}}{\frac{1}{19} - \frac{18}{19}} = \frac{1(19-18)}{18 \times 19} = \frac{-1}{108}$$

$\frac{\sin \alpha}{\cos \alpha} > 0 \rightarrow \frac{\cos \alpha}{\sin \alpha} > 0 \rightarrow \cos \alpha > 0 \rightarrow \text{في الربع 1} \textcircled{1}$

$r \sin \alpha (\sin^2 \alpha \rightarrow r \sin \alpha (\sin \alpha \cos \alpha \rightarrow \sin \alpha \cos \alpha - \sin \alpha) > 0 \rightarrow \sin \alpha (\cos \alpha - 1) > 0$

$\Rightarrow \sin \alpha < 0 \rightarrow \text{في الربع 3} \textcircled{2}$

$\textcircled{1}, \textcircled{2} \rightarrow \boxed{\text{الربع 3}}$