

$$\text{الف) } \lim_{x \rightarrow r^+} f(x) = d \quad (1)$$

$$\text{ب) } \lim_{x \rightarrow r^-} f(x) = d$$

$$\text{الف) } \lim_{x \rightarrow r^+} f(x) = f(r^+) = d \quad (2)$$

$$\text{ب) } \lim_{x \rightarrow r^-} f(x) = f(r^-) = d$$

$$\text{الف) } \lim_{x \rightarrow r^+} [f(x)] = [d^+] = d \quad (3)$$

$$\text{ب) } \lim_{x \rightarrow r^-} [f(x)] = [d^-] = d$$

$$\text{الف) } \left[\lim_{x \rightarrow r^+} f(x) \right] = d \quad (4)$$

$$\text{ب) } \left[\lim_{x \rightarrow r^-} f(x) \right] = d$$

ا) $\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{x - 0} = \frac{0}{0}$
 $\begin{cases} x^+ \rightarrow +\infty \rightarrow \frac{9}{0^+} \\ x^- \rightarrow -\infty \rightarrow \frac{9}{0^-} \end{cases}$
 (3)
 جواب

ب) $\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{(x - 0)^2} = \frac{9}{(0^+)^2} = +\infty$
 $\frac{9}{(0^-)^2} = +\infty$
 $= +\infty$

ا) $\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{\sqrt{x - 0}}$
 $\begin{cases} x^+ \rightarrow \frac{9}{\sqrt{0^+}} = \frac{9}{0^+} = +\infty \\ x^- \rightarrow \frac{9}{\sqrt{0^-}} = \text{ج.ب} \end{cases}$
 (4)
 جواب

ب) $\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{\sqrt{x^2 - f(x) + 0}}$
 $\begin{cases} x^+ \rightarrow \frac{9}{\sqrt{0^+}} = +\infty \\ x^- \rightarrow \frac{9}{\sqrt{0^-}} = \text{ج.ب} \end{cases}$
 جواب

ا) $\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{x^2 + \sqrt{x} + 0}$
 $\begin{cases} x^+ \rightarrow \frac{9}{0^+} = -\infty \\ x^- \rightarrow \frac{9}{0^-} = +\infty \end{cases}$
 (5)
 جواب

ب) $\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{[x - 0]}$
 $\begin{cases} x^+ \rightarrow \frac{9}{0} = \text{ج.ب} \\ x^- \rightarrow \frac{9}{0^-} = -9 \end{cases}$
 (6)
 جواب

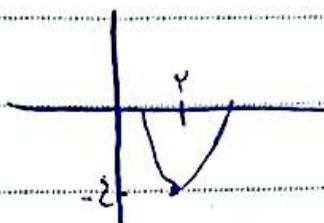
ا) $\lim_{n \rightarrow \infty} [f(n)] - [-f(n)]$
 $\begin{cases} n^+ \rightarrow 9 + (-0) = 9 \\ n^- \rightarrow 1 + (-0) = 1 \end{cases}$
 (7)
 $\Rightarrow 9$

ب) $\lim_{n \rightarrow \infty} [-f(n)] + [f(n)]$
 $\begin{cases} n^+ \rightarrow -9 + 0 = -9 \\ n^- \rightarrow -1 + 0 = -1 \end{cases}$
 (8)
 $\Rightarrow -9$

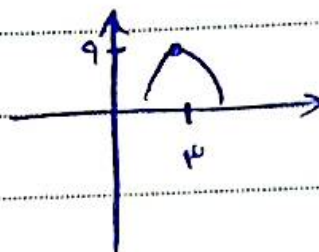
Arman

9

$$\text{a) } \lim_{x \rightarrow 2} [x^2 - 4x] \xrightarrow{\text{بسط}} \boxed{-4}$$



$$\text{ب) } \lim_{x \rightarrow 2} [-x^2 + 4x] \xrightarrow{\text{بسط}} \boxed{4}$$



$$\text{c) } \lim_{x \rightarrow 2} \frac{|x-2|}{x^2 - 4x + 4} \begin{matrix} x^+ \rightarrow \frac{x-2}{(x-1)(x-2)} = 1 \\ x^- \rightarrow \frac{-(x-2)}{(x-1)(x-2)} = -1 \end{matrix} \rightarrow \text{ليس}$$

$$\text{د) } \lim_{x \rightarrow 1} \frac{x - [a]}{x^2 - 1} \begin{matrix} 1^+ \rightarrow \frac{x-1}{(x-1)(x+1)} = \frac{1}{2} \\ 1^- \rightarrow \frac{a}{(x-1)(x+1)} = \frac{1}{0^-} = -\infty \end{matrix} \rightarrow \text{ليس}$$