

$$\lim_{x \rightarrow r^+} f(x) - r = a \quad \lim_{x \rightarrow r^-} f(x) - r = a$$

1

$$\lim_{x \rightarrow r^+} f[n] - r = f(r) - r = a \quad \lim_{x \rightarrow r^-} f[n] - r = f(1) - r = 1$$

2

$$\lim_{x \rightarrow r^+} [f(x) - r] = \lim_{x \rightarrow r^+} [f(x)] - r = 1 - r = a$$

3

$$\lim_{x \rightarrow r^-} [f(x) - r] = \lim_{x \rightarrow r^-} [f(x)] - r = 1 - r = a$$

$$[\lim_{x \rightarrow r^+} f(x) - r] = [a] = a \quad [\lim_{x \rightarrow r^-} f(x) - r] = [a] = a$$

4

$$\lim_{x \rightarrow r} \frac{f(x) - r}{x - r} \rightarrow x = r \Rightarrow \begin{matrix} \text{صورت عددی غیر صفر} \\ \text{مخرج صفر} \end{matrix} \begin{matrix} x \rightarrow r^- = \frac{9}{0^-} = -\infty \\ x \rightarrow r^+ = \frac{9}{0^+} = +\infty \end{matrix} \text{ (محدود)}$$

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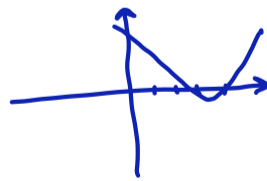
$$\lim_{x \rightarrow r} \frac{f(x) - r}{(x - r)^2} \rightarrow x = r \Rightarrow \begin{matrix} \text{صورت عددی غیر صفر} \\ \text{مخرج صفر} \end{matrix} \begin{matrix} x \rightarrow r^- = \frac{9}{0^+} = +\infty \\ x \rightarrow r^+ = \frac{9}{0^+} = +\infty \end{matrix} \text{ (محدود)}$$

$$\lim_{x \rightarrow r} \frac{f(x) - r}{\sqrt{x - r}} \rightarrow x = r \Rightarrow \begin{matrix} \text{صورت صفر} \\ \text{مخرج صفر} \end{matrix} \begin{matrix} x \rightarrow r^- = \text{ج.ن.} \\ x \rightarrow r^+ = \frac{9}{0^+} = +\infty \end{matrix} \text{ (محدود)}$$

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$$\lim_{x \rightarrow r} \frac{f(x) - r}{\sqrt{x^2 - x + r}} \rightarrow x = r \Rightarrow \begin{matrix} \text{صورت صفر} \\ \text{مخرج صفر} \end{matrix} \begin{matrix} x \rightarrow r^- = \text{ج.ن.} \\ x \rightarrow r^+ = \frac{9}{0^+} = +\infty \end{matrix} \text{ (محدود)}$$

$$\lim_{x \rightarrow r} \frac{f(x) - r}{x^2 - \sqrt{x+1}} \rightarrow \begin{matrix} x \rightarrow r^- = \frac{9}{0^+} = +\infty \\ x \rightarrow r^+ = \frac{9}{0^-} = -\infty \end{matrix} \text{ (محدود)}$$



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$$\lim_{x \rightarrow r} \frac{f(x) - r}{[x - r]} \rightarrow \begin{matrix} x \rightarrow r^- = \frac{9}{-1} = -9 \\ x \rightarrow r^+ = \frac{9}{0} = \text{ج.ن.} \end{matrix} \text{ (محدود)}$$

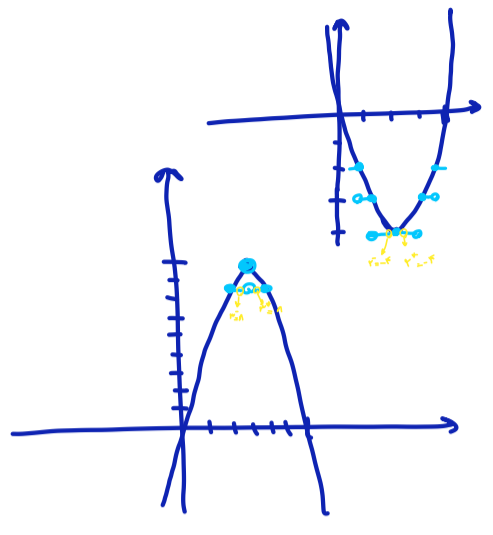
$$\lim_{x \rightarrow r} [f(x)] + [-r] \rightarrow \begin{matrix} x \rightarrow r^+ = 9 - 1 = 8 \\ x \rightarrow r^- = 1 - 1 = 0 \end{matrix} \text{ (محدود)}$$

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$$\lim_{x \rightarrow -4} [-f(x)] + [g(x)] \left[\begin{array}{l} \rightarrow x \rightarrow -4^- = 2f - 1g = 12 \\ \rightarrow x \rightarrow -4^+ = 2f - 1g = 10 \end{array} \right] \text{ (دليله)}$$

$$\lim_{x \rightarrow 2} [x^2 - f(x)] \left[\begin{array}{l} \rightarrow x \rightarrow 2^- = -f \\ \rightarrow x \rightarrow 2^+ = -f \end{array} \right] \text{ (دليله)}$$

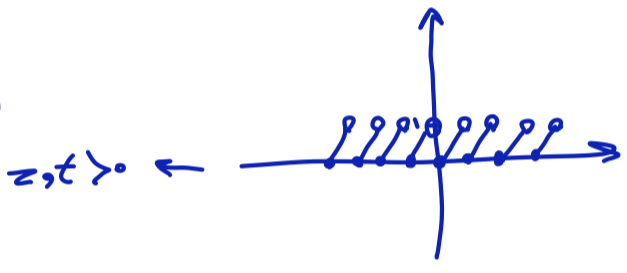
$$\lim_{x \rightarrow 2} [4x - x^2] \left[\begin{array}{l} \rightarrow x \rightarrow 2^- = 1 \\ \rightarrow x \rightarrow 2^+ = 1 \end{array} \right] \text{ (دليله)}$$



(9)

$$\lim_{x \rightarrow 2} \frac{|x-2|}{x^2 - x + 2} \left[\begin{array}{l} \rightarrow x \rightarrow 2^- = \frac{(2-x)}{(x-1)(x-2)} = \frac{-1}{x-1} = -1 \\ \rightarrow x \rightarrow 2^+ = \frac{(x-2)}{(x-1)(x-2)} = \frac{1}{x-1} = 1 \end{array} \right] \text{ (دليله)}$$

$$\lim_{x \rightarrow 1} \frac{x - [x]}{x^2 - 1} \left[\begin{array}{l} \rightarrow x \rightarrow 1^- = \frac{z}{0^-} = -\infty \\ \rightarrow x \rightarrow 1^+ = \frac{t}{0^+} = +\infty \end{array} \right] \text{ (دليله)}$$



(10)