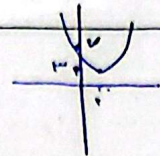
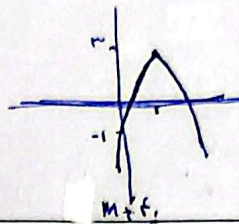


الف) $y = x^2 - 4x + 1$ $\begin{cases} x_s = \frac{-b}{2a} = \frac{4}{2} = 2 \\ y_s = 4 - 8 + 1 = -3 \end{cases}$ 

ب) $y = -(x^2 - 4x + 1)$ $\begin{cases} x_s = 2 \\ y_s = -(4 - 8 + 1) = 3 \end{cases}$ 

$2x^2 + (m+1)x + \frac{1}{2}m + 2 = 0$ $\Delta = (m+1)^2 - 4(2)(\frac{1}{2}m+2) = m^2 + 2m + 1 - 4m - 8 = m^2 - 2m - 7$
 $\Delta > 0 \rightarrow (m-5)(m+2) > 0 \rightarrow m \in (-\infty, -2) \cup (5, +\infty)$ (الف)
 $\Delta = 0 \rightarrow (m-5)(m+2) = 0 \rightarrow m \in \{5, -2\}$ (ب)
 $\Delta < 0 \rightarrow (m-5)(m+2) < 0 \rightarrow m \in (-2, 5)$ (ج)
 $\Delta \geq 0 \rightarrow m \in (-\infty, -2] \cup [5, +\infty)$ (د)

۳ $(m-2)x^2 - 2(m+1)x + 1 = 0$ $\begin{cases} P > 0 \rightarrow \frac{1}{m-2} > 0 \rightarrow m > 2 \\ S < 0 \rightarrow \frac{2(m+1)}{m-2} < 0 \rightarrow m < 2 \\ \Delta > 0 \rightarrow \frac{4(m+1)^2}{(m-2)^2} > 0 \rightarrow m \neq 2 \end{cases}$ (الف)
 $m \in \mathbb{R} \setminus \{2\}$
 $\Delta = 4(m+1)^2 - 4(m-2) = 4m^2 + 8m + 4 - 4m + 8 = 4m^2 + 4m + 12 = 4(m^2 + m + 3)$ همیشه $\Delta > 0$ است.
 $\begin{cases} P < 0 \rightarrow \frac{1}{m-2} < 0 \rightarrow m < 2 \\ S < 0 \rightarrow \frac{2(m+1)}{m-2} < 0 \rightarrow m < 2 \\ \Delta > 0 \rightarrow \text{همیشه} \end{cases} \Rightarrow m \in (-\infty, 2)$ (ب)

۴ $\begin{cases} a \neq 0 \rightarrow m \neq 2 \\ \Delta > 0 \rightarrow \text{همیشه برقرار} \\ P < 0 \rightarrow \frac{1}{m-2} < 0 \rightarrow m < 2 \end{cases} \Rightarrow m \in (-\infty, 2)$ (الف)

ب) $x_s = \frac{-b}{2a} = \frac{x(m+1)}{x(m-2)} = -2 \rightarrow -2m + 4 = m + 1 \rightarrow -3m = -3 \rightarrow m = 1$

۵ $\Delta > 0 \rightarrow 4 \sin^2 \alpha - 4 > 0 \rightarrow 4(\sin^2 \alpha - 1) > 0$
 $\sin^2 \alpha = 1 \rightarrow \sin \alpha = \pm 1 \rightarrow \sin \alpha = 1 \rightarrow \alpha = \frac{\pi}{2}$ (طبق جدول)
 $\sin \alpha = -1 \rightarrow \alpha = \frac{3\pi}{2}$
 $\Rightarrow \frac{2x^2}{3} - 2x + \frac{2}{3} < 0 \xrightarrow{\times 3} 2x^2 - 12x + 2 < 0 \rightarrow x^2 - 12x + 1 < 0$
 $\rightarrow (x-6)(x-1) < 0$
 $\rightarrow x \in (1, 6)$

$y = \frac{(2n^2 - 2n - 1)(2n^2 - 2n - 0)}{1 - n^2} = \frac{(n-1)(2n+1)(2n-0)(n+1)}{(1-n)(1+n)}$ $= -(2n^2 - 2n - 0) = -2n^2 + 2n + 0 \rightarrow \begin{cases} n_{\max} = \frac{1}{2} \\ y_{\max} = -2\left(\frac{1}{4}\right) + \frac{1}{2} + 0 = \frac{1}{4} \end{cases}$ $y_{\max} = \frac{-149 + 231 + 12}{25} = \frac{74}{25}$	8
$\Psi S = \partial P + V \rightarrow \Psi\left(\frac{m+r}{m}\right) = \partial\left(\frac{-r}{m}\right) + V \xrightarrow{\Psi m + r} \Psi m + r = -1 + \Psi m$ $\rightarrow -\epsilon m = -1 \rightarrow m = \frac{1}{\epsilon}$ $\rightarrow S = \frac{m+r}{m} = \frac{r}{\epsilon}, P = \frac{-r}{m} = \frac{-r}{\epsilon} = -\frac{1}{\epsilon}$ $\rightarrow \alpha^r + \beta^r = S^r - rP = \frac{1}{\epsilon} + 1 = \frac{1+r}{\epsilon}$	7
$\alpha + \beta = 0, \alpha\beta = r \rightarrow \alpha = -\beta$ $\beta^r = 0\beta - r \rightarrow \beta^r = \beta(0\beta - r) = 0\beta^r - r\beta = r0\beta - 1 = -r\beta = \alpha\beta - 1$ $\beta^r = \beta(r\beta - 1) = r\beta^2 - 1\beta = r\beta(0\beta - r) = 1\beta - \epsilon\beta$ $\beta^0 = \beta(1\beta - \epsilon\beta) = \epsilon\beta^2 - 1\beta$ $\frac{1 - r\beta + \epsilon\beta^2 - 1}{r0\beta - 1} = \frac{\epsilon\beta^2 - 1}{r0\beta - 1} = \frac{19(r0\beta - 1)}{r0\beta - 1} = 19$	6
$y = an^2 + bn + c \xrightarrow{c=0} y = an^2 + bn + c$ $\begin{pmatrix} 1 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} \rightarrow \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 1 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} \rightarrow \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \rightarrow \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ $\rightarrow y = n^2 + 2n + 1 \xrightarrow{ns} ns = \frac{-b}{2a} = \frac{-2}{2} = -1$	9
$2n^2 + (m+1)n + m + 9 = n \rightarrow 2n^2 + mn + m + 9 = 0$ $\Delta = 0 \rightarrow m^2 - 4m - 36 = 0 \rightarrow (m-12)(m+3) = 0 \rightarrow \begin{cases} m=12 \\ m=-3 \end{cases}$	10