

$A(4,2) \quad B(0,-2) \quad \begin{cases} y=mx+h \\ m=\frac{2}{-4}=-\frac{1}{2} \end{cases} \xrightarrow{(4,2)} y=-\frac{1}{2}x+h \rightarrow h=4 \rightarrow y=-\frac{1}{2}x+4$ $2y+4x=-1 \xrightarrow{\text{دراز می‌بند}} m=\frac{-4}{2}=-2 \rightarrow y=-2x+h \xrightarrow{(4,2)} y=-2x+10$ $x+3y=1 \xrightarrow{\text{عمود باشد}} m=\frac{-1}{3} \rightarrow m'=3 \rightarrow y=3x+h \xrightarrow{(4,2)} y=3x-10$ $\frac{1}{\sqrt{3}} \rightarrow m=\tan \frac{\pi}{3}=\sqrt{3} \rightarrow y=\sqrt{3}x+h \xrightarrow{(4,2)} y=\sqrt{3}x+2-4\sqrt{3}$	(الف) (ب) (ج) (د)	۱
$d((2,3),(1,5)) = \sqrt{\Delta x^2 + \Delta y^2} = \sqrt{1^2 + 2^2} = \sqrt{5}$ $d = \frac{ ax_0+by_0+c }{\sqrt{a^2+b^2}} = \frac{ 4+12-2 }{5} = \frac{14}{5}$	(الف) (ب)	۲
$\begin{cases} d_1: 4x+2y-12=0 \\ d_2: 4x+2y-1=0 \end{cases} \Rightarrow m' = -\frac{4}{2} = -2 \text{ و } c' = \frac{c_1+c_2}{2} = \frac{-12-1}{2} = -\frac{13}{2}$ $\rightarrow d': 4x+2y-13=0$ $\frac{ c-c' }{\sqrt{a^2+b^2}} = \frac{ -12-(-\frac{13}{2}) }{\sqrt{4^2+2^2}} = \frac{\frac{11}{2}}{\sqrt{20}} = \frac{11}{2\sqrt{20}}$	(الف) (ب)	۳
$\frac{ 3x-2y-1 }{\sqrt{13}} = \frac{ 2x+5y-3 }{\sqrt{13}} \rightarrow 3x-2y-1 = 2x+5y-3 $ $\rightarrow 3x-2y-1 = 2x+5y-3 \Rightarrow x-7y+2=0$ $3x-2y-1 = -(2x+5y-3) \Rightarrow 5x+3y-4=0$		۴
$\tan \alpha = \left \frac{-2-2}{\frac{1+4}{-5}} \right = \frac{4}{5} = 1 \Rightarrow \alpha = 45^\circ = \frac{\pi}{4}$ $m = -2$ $m' = 2$		۵

$d = \sqrt{\Delta n^2 + y^2} = \sqrt{1^2 + 4^2} = 5$	الف	
$M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \left(\frac{-4+2}{2}, \frac{4-2}{2} \right) = (-1, 1)$	ب	٦
$\text{مركز ثقل} = \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right) = (-3, -3)$	الف	
$S = \begin{vmatrix} -10 & -13 & 1 \\ -2 & 3 & 1 \\ 3 & 1 & 1 \end{vmatrix} = \frac{\begin{vmatrix} 20 & -11 \\ 9+24+(-1) \end{vmatrix} - \begin{vmatrix} -30+(-2)+(-29) \end{vmatrix}}{2} = \frac{11+20}{2} = 15.5$	ب	٧
$-y = \frac{2x+1}{x-3} \rightarrow y = \frac{-2x-1}{x-3}$	الف	
$y = \frac{-2x+1}{-x-3}$	ب	٨
$x = \frac{2y+1}{y-3} \rightarrow y = \frac{-2x-1}{x-3} = \frac{2x+1}{x-3}$	ج	
$-x = \frac{-2y+1}{-y-3} \rightarrow x = \frac{2y+1}{y+3} \rightarrow y = \frac{-2x+1}{x+2}$	د	
$\begin{cases} x' = x-2 \rightarrow x = x'+2 \\ y' = y+3 \rightarrow y = y'-3 \end{cases} \rightarrow y'-3 = \frac{2(x'+2)+1}{x'+2-3} \rightarrow y' = \frac{2x'+5}{x'-1} + 3 = \frac{5x'+2}{x'-1}$	الف	
$\begin{cases} x' = x-3 \rightarrow x = x'+3 \\ y' = y-2 \rightarrow y = y'+2 \end{cases} \rightarrow y'+2 = \frac{2(x'+3)+1}{x'+3-3} \rightarrow y' = \frac{2x'+7}{x'} - 2 = \frac{7}{x'}$	ب	٩
$\begin{cases} 3x+4y=2 \\ 3x-10y=3 \end{cases} \Rightarrow 14y=-1 \rightarrow y = -\frac{1}{14}, x = \frac{14}{19}$	الف	
$x = -\frac{\begin{vmatrix} 14 & 2 \\ 19 & 4 \end{vmatrix}}{\begin{vmatrix} 3 & 4 \\ 3 & -10 \end{vmatrix}} = -\frac{14}{-19} = \frac{14}{19}, y = \frac{\begin{vmatrix} 13 & 2 \\ 11 & 4 \end{vmatrix}}{\begin{vmatrix} 3 & 4 \\ 3 & -10 \end{vmatrix}} = \frac{1}{-19}$	ب	١٠