

$$m = \frac{m-k}{6} = \frac{-1}{2} \rightarrow -6 = 2m - 2k \rightarrow m - k = -3$$

$$AB = \sqrt{(4^2) + (\frac{m-k}{2})^2} = \sqrt{16+9} = 5 \rightarrow S = (5\sqrt{5})^2 = 125$$

$AB = \sqrt{3^2 + 3^2} = 3\sqrt{2}$
 $CD = 0 = \sqrt{(x+1)^2 + (y-4)^2} = \sqrt{4x^2 + 4x + 1 + y^2 - 8y + 16} = \sqrt{4x^2 + 4x + y^2 - 8y + 17}$
 $\rightarrow 4x^2 + 4x - 16 = 0 \rightarrow x^2 + x - 4 = 0 \rightarrow (x-3)(x+1) = 0$
 $\rightarrow x = -1$ (circled) $\rightarrow \frac{-1}{2} = \frac{-1}{2}$, $\sqrt{(x-3)^2 + (y-1)^2} = \sqrt{x^2 + y^2} \rightarrow x = \frac{5}{2}$

$m = \tan 45^\circ = \sqrt{3}$
 $\rightarrow \frac{-2m}{m^2-1} = \sqrt{3} \rightarrow \sqrt{3} m^2 + 2m - \sqrt{3} = 0 \rightarrow m^2 + 2m - 3 = 0 \rightarrow (m+3)(m-1) = 0$
 $\rightarrow m = -3$ (circled)
 $m = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$ (circled)

$m_{BC} = \frac{11-2}{3-1} = 5 \rightarrow m_{AH} = -\frac{1}{5}$
 $y_{BC} = 5x + h \rightarrow 2 = 5 + h \rightarrow h = -3 \rightarrow y = 5x - 3$
 $y_{AH} = -\frac{1}{5}x + h \rightarrow 9 = -\frac{1}{5}x + h \rightarrow h = \frac{45}{5} \rightarrow y = -\frac{1}{5}x + 9$
 $5x - 3 = -\frac{1}{5}x + 9 \rightarrow \frac{25}{5}x = \frac{48}{5} \rightarrow x = \frac{48}{5} \rightarrow y = \frac{21}{5}$
 $AH = \sqrt{(\frac{48}{5}-1)^2 + (\frac{21}{5}-9)^2} = \sqrt{\frac{41}{5}} = \frac{\sqrt{41}}{5}$

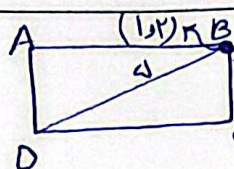
$A \Rightarrow \frac{m_{AH}}{5} = 5 - 2x \rightarrow 21 - 11x = 5x + 15 \rightarrow 11 = 11x \rightarrow x = 1, y = 1$
 $B \Rightarrow 5 - 2x = \frac{5x - 19}{5} \rightarrow 15 - 10x = 5x - 19 \rightarrow 11x = 34 \rightarrow x = \frac{34}{11}, y = 1$
 $y_{AC} = \frac{5}{4}x + h \rightarrow 1 = \frac{5}{4} + h \rightarrow h = -\frac{1}{4} \rightarrow \frac{5}{4}x + \frac{1}{4} = -\frac{1}{4}x + 0 \rightarrow \frac{6}{4}x = -\frac{1}{4} \rightarrow x = -\frac{1}{6}$
 $y_{BH} = -\frac{5}{4}x + h \rightarrow 1 = -\frac{5}{4}x + h \rightarrow h = \frac{5}{4}x + 1$
 $\Rightarrow BH = \sqrt{(3-\frac{1}{6})^2 + (\frac{1}{4}-1)^2} = \sqrt{(\frac{17}{6})^2 + (\frac{3}{4})^2} = \sqrt{\frac{900}{144} + \frac{9}{144}} = \frac{\sqrt{909}}{12}$

$$y = mx + h \rightarrow m = \frac{-\frac{9}{\sqrt{2}}}{\frac{\sqrt{2}}{2}} = -1 \rightarrow y = -1x - 9$$

$$\text{نقطه } x=y \rightarrow x = -1x - 9 \rightarrow 2x = -9 \rightarrow x = -\frac{9}{2} = -\frac{\sqrt{2}}{2}$$

$$\rightarrow \text{قطر} = \frac{\sqrt{2}}{2} \sqrt{2}$$

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$$y = ax + 1 \quad y = x + 1 \quad m_{AB} = m_{DC} = \frac{a}{1} = \frac{1}{a} \Rightarrow a^2 = 1 \rightarrow a = \pm 1$$

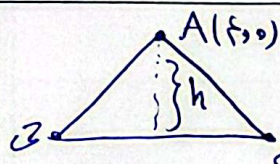
$$y = ax + 1 \xrightarrow{a=1} y = x + 1$$

$$y = \frac{1}{a}x + \frac{a-1}{a} \rightarrow y = x$$

$$BC = \frac{1-1}{\sqrt{2}} = \frac{\sqrt{2}}{2} \Rightarrow S = (2 \times \frac{\sqrt{2}}{2}) \times \frac{\sqrt{2}}{2} = 0 \sqrt{2}$$

منتهی بتدریج روی یک خط منتهی می شود

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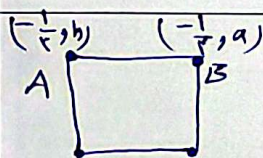


$S = ?$

$$\frac{|1-1|}{\sqrt{1.}} = \frac{\sqrt{2}}{\sqrt{1.}} \Rightarrow BC = h$$

$$\rightarrow S = \frac{BC \times h}{2} = \frac{(\frac{\sqrt{2}}{\sqrt{1.}}) \times \frac{1}{\sqrt{2}}}{2} = \frac{9}{1.} \div 2 = \frac{9}{2.}$$

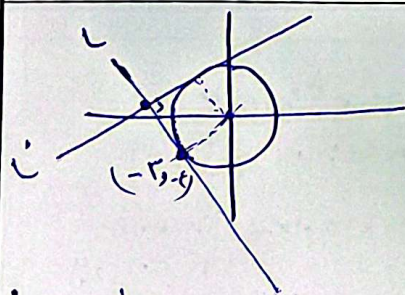
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$$m = \frac{b-a}{\frac{1}{4}} = \sqrt{2} \rightarrow b-a = \frac{\sqrt{2}}{4}$$

$$\text{طول قطر} = AB\sqrt{2} \rightarrow \sqrt{(\frac{1}{4})^2 + (\frac{\sqrt{2}}{4})^2} \times \sqrt{2} \times \sqrt{2} = \frac{\sqrt{2}}{2} \sqrt{2} = \frac{\sqrt{2}}{2}$$

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$$\text{شیب } m_L = \frac{-r}{-r} = \frac{r}{r}$$

$$m_L = -\frac{r}{r} \rightarrow y = -\frac{r}{r}x + h \rightarrow -r = +\frac{r}{r} + h \rightarrow h = -\frac{2r}{r}$$

$$\rightarrow y = -\frac{r}{r}x - \frac{2r}{r}$$

$$m_L' = \frac{r}{r} \rightarrow y = \frac{r}{r}x + h \rightarrow y = \frac{r}{r}x + \frac{2r}{r}$$

$$|0+0+h| = d \rightarrow h = \frac{2r}{r}$$

$$\frac{2r}{r} \sqrt{1+\frac{r^2}{r^2}}$$

$$-r \times -1 = \sqrt{2}$$

$$\leftarrow y = -1$$

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