

$$\begin{aligned}
 &rx^r + y^r - rx + ry + k = 0 \rightarrow rx^r - rx + y^r + ry + k = 0 \rightarrow r(x^r - rx) + (y^r + ry) + k = 0 \quad 1 \\
 &\rightarrow r((x-1)^r - 1) + (y+r)^r - 9 + k = 0 \rightarrow r(x-1)^r - r + (y+r)^r - 9 + k = 0 \rightarrow \dots \rightarrow \dots \\
 &\rightarrow r(x-1)^r + (y+r)^r - 11 + k = 0 \rightarrow r(x-1)^r + (y+r)^r = 11 - k \rightarrow 11 - k \geq 0 \\
 &\rightarrow k \leq 11
 \end{aligned}$$

$$f(x) = \begin{cases} x^r + rx \rightarrow x \geq a \\ rx + a + r \rightarrow x \leq a \end{cases} \rightarrow \begin{aligned} &a^r + ra = ra + a + r \\ &a^r + ra = ra + r \\ &a^r + a - r = 0 \\ &(a-1)(a+r) = 0 \rightarrow a \begin{cases} \xrightarrow{-r} \text{قبول} \rightarrow a > 0 \\ \xrightarrow{1} \checkmark \end{cases} \end{aligned}$$

$$f(1) = f(a) = a^r + ra = ra + a + r = 8$$

$$f(x) = \begin{cases} rx^r - b & |x+1| \geq r \\ a + rx & -r \leq x \leq -1 \end{cases} \xrightarrow{x=-r} \begin{aligned} &rx^r - b = a + rx \\ &11 - b = a + (-9) \\ &a + b = 20 \end{aligned}$$

$$y = \sqrt{4x-a} + \sqrt{b-rx} \rightarrow \begin{cases} 4x-a \geq 0 \rightarrow x \geq \frac{a}{4} \\ b-rx \geq 0 \rightarrow x \leq \frac{b}{r} \end{cases} \xrightarrow{\text{میشود}} \begin{aligned} &\frac{a}{4} = \frac{b}{r} = r \rightarrow \begin{cases} a = 16 \\ b = 4 \end{cases} \\ &\frac{b}{a} = \frac{4}{16} = \frac{1}{4} \end{aligned} \quad D = \{r\} \quad 2$$

$$y = \sqrt{\frac{x+1}{|x-r|}} + \sqrt{\frac{4-x}{x^r + rx + r}} \quad \begin{aligned} &x \neq r \\ &x+1 \geq 0 \rightarrow x \geq -1 \\ &4-x \geq 0 \rightarrow x \leq 4 \\ &x^r + rx + r > 0 \rightarrow \text{همیشه مثبت} \end{aligned}$$
$$A \cap B = [-1, 4] - \{r\}$$

$$y = \sqrt{[x]-\varepsilon} + \sqrt{r-[x]} \rightarrow \begin{aligned} &[x]-\varepsilon \geq 0 \Rightarrow [x] \geq r \rightarrow [r, +\infty) = A \\ &r-[x] \geq 0 \Rightarrow [x] \leq r \rightarrow (-\infty, r] = B \end{aligned} \left. \vphantom{\begin{aligned} &[x]-\varepsilon \geq 0 \Rightarrow [x] \geq r \rightarrow [r, +\infty) = A \\ &r-[x] \geq 0 \Rightarrow [x] \leq r \rightarrow (-\infty, r] = B \end{aligned}} \right\} A \cap B = \emptyset$$

$$x^r - x - 4 \geq 0 \rightarrow (x-r)(x+r) \geq 0 \quad -4$$

$$y = \sqrt{\frac{x^r - x - 4}{x^r - 17x^r + 194}}$$

$$x^r - 17x^r + 194 \geq 0 \rightarrow (x^r - 9)(x^r - 14) \geq 0 \rightarrow (x-r)(x+r)(x-r)(x+r) \geq 0$$

$$\begin{array}{c} -r \quad -r \quad r \quad r \\ + \quad - \quad - \quad + \quad + \\ \cup \quad \cup \quad \cup \quad \cup \quad \cup \end{array} \rightarrow Df = (-\infty, r) \cup (r, +\infty)$$

$$y = \sqrt{\frac{x^r - rx^r - 2x + 4}{x^r + rx^r - 2x - 4}} \rightarrow (x-1)(x^r - x - 4) \rightarrow (x-1)(x-r)(x+r)$$

$$\rightarrow (x+1)(x^r + x - 4) \rightarrow (x+1)(x+r)(x-r)$$

$$\begin{array}{c} 1 \quad r \quad -r \\ -r \quad -r \quad -1 \quad 1 \quad r \quad r \\ + \quad - \quad + \quad - \quad + \quad - \\ \cup \quad \cup \quad \cup \quad \cup \quad \cup \quad \cup \end{array}$$

$$Df = (-\infty, -r) \cup [-r, -1) \cup [1, r) \cup [r, +\infty)$$

$$y = \sqrt{[-x] - r} \rightarrow [-x] - r \geq 0 \rightarrow [-x] \geq r \rightarrow -x \geq r \rightarrow x \leq -r \quad -4$$

$$y = \frac{[x]^r + 4}{[x]^r - r[x] - r} \rightarrow ([x] - r)([x] + 1) \neq 0 \rightarrow \begin{cases} [x] = -1 \rightarrow [-1, 0) \cup \\ [x] = r \rightarrow [r, r) \cup \end{cases}$$

$$Df = \mathbb{R}_1 - \{[-1, 0) \cup [r, r)\}$$

$$y = \frac{\cot x + 1}{\tan x + 1} \rightarrow \tan x \neq -1 \rightarrow \frac{\sin x}{\cos x} \neq -1 \rightarrow \cos x \neq 0 \rightarrow \mathbb{R}_1 - \left\{k\pi + \frac{\pi}{2}, k\pi + \frac{3\pi}{2}\right\} - 1$$

$$y = \sqrt{1 - r \sin^r x} \rightarrow 1 - r \sin^r x \geq 0 \rightarrow r \sin^r x \leq 1 \rightarrow \sin^r x \leq \frac{1}{r}$$

$$Df = \left[k\pi - \frac{\pi}{r}, k\pi + \frac{\pi}{r}\right] \quad -\frac{1}{r} \leq \sin x \leq \frac{1}{r}$$

$$y = \sqrt{1 - \log \frac{x-1}{r}} \rightarrow \log \frac{x-1}{r} \leq 1 \rightarrow x-1 \leq \frac{1}{r} \rightarrow x \leq \frac{r}{r} \quad A$$

$$x-1 > 0 \rightarrow x > 1 \quad B$$

$$A \cap B = (1, \frac{r}{r}]$$

$$y = \frac{\sqrt{x^r - x}}{1 - \log \frac{x^r - rx}{r}} \rightarrow 1 - \log \frac{x^r - rx}{r} \neq 0 \rightarrow x^r - rx \neq r \rightarrow x^r - rx - r \neq 0$$

$$x^r - rx > 0 \rightarrow x(x-r) > 0 \quad \begin{array}{c|c|c} & r & \\ \hline + & - & + \\ \hline \end{array} \quad (-\infty, 0) \cup (r, +\infty) \quad B$$

$$x^r - x \geq 0 \rightarrow x(x-1) \geq 0 \quad \begin{array}{c|c|c} & 1 & \\ \hline + & - & + \\ \hline \end{array} \quad (-\infty, 0] \cup [1, +\infty) \quad A$$

$$Df = ((r, +\infty) \cup (-\infty, 0)) - \{-1, r\}$$

$$(-\infty, -1) \cup (-1, 0) \cup (r, r) \cup (r, +\infty)$$

$$y = \sqrt{r^{rx-x^r} - 1} \rightarrow r^{rx-x^r} - 1 \geq 0 \rightarrow r^{rx-x^r} \geq 1 \rightarrow rx - x^r \geq r$$

$$rx - x^r - r \geq 0$$

$$x^r - rx + r \leq 0$$

$$(x-1)(x-r) \leq 0$$

$$Df = [1, r]$$

$$\begin{array}{c|c|c} & 1 & r & \\ \hline + & - & + \\ \hline \end{array}$$

$$y = \left(\frac{rx + a}{rx + r} \right)!$$

$$\frac{rx + a}{rx + r} \in \mathbb{N} \rightarrow rx + a = k(rx + r) \rightarrow rx + a = krx + kr$$

$$rx + a - krx - kr = 0 \rightarrow r(1-k)x + (a - kr) = 0$$

$$Df = \left\{ x = \frac{-k + a}{r - r} \mid k \in \mathbb{N} \right\}$$

$$x = \frac{-k + a}{r - r}$$