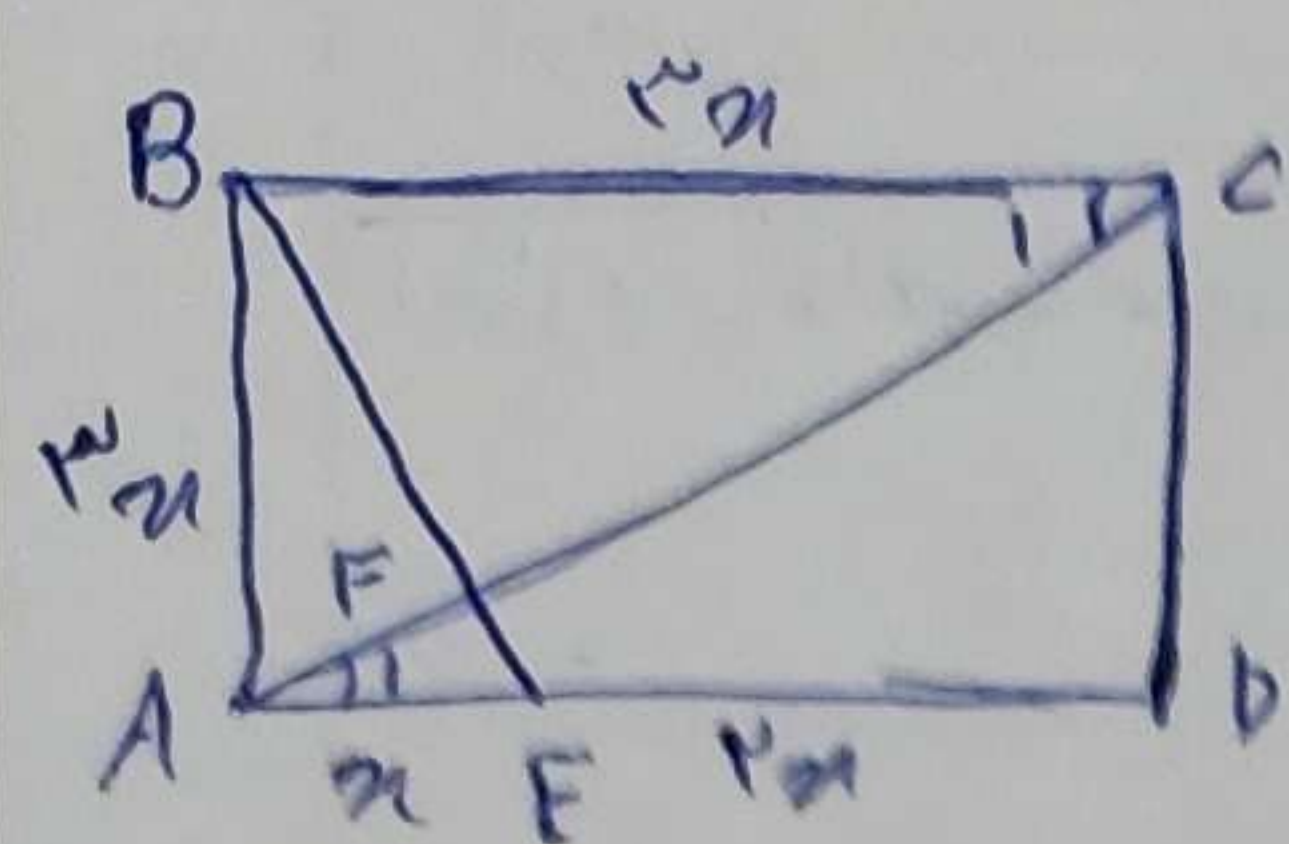


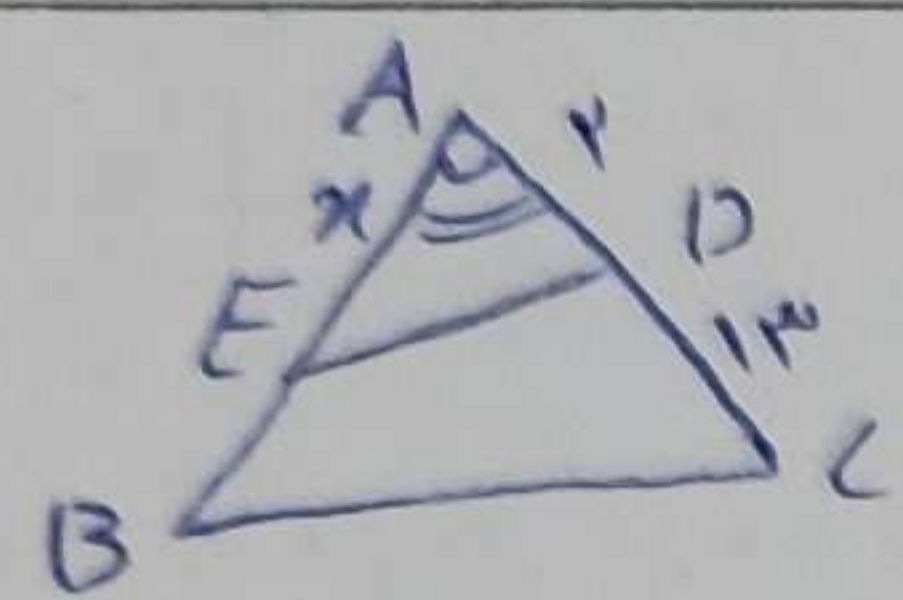
نام و نام خانوادگی آفرین پاسخنامه تشریحی تکلیف شماره ۲۱ کلاس ۲۱ نام و نام خانوادگی آفرین



$$\left. \begin{array}{l} \overline{BC} \parallel \overline{AD} \Rightarrow \hat{A}_1 = \hat{C}_1 \\ \overline{AC} \\ F_1 = F_1 \end{array} \right\} \Rightarrow \triangle BCF \cong \triangle EAF$$

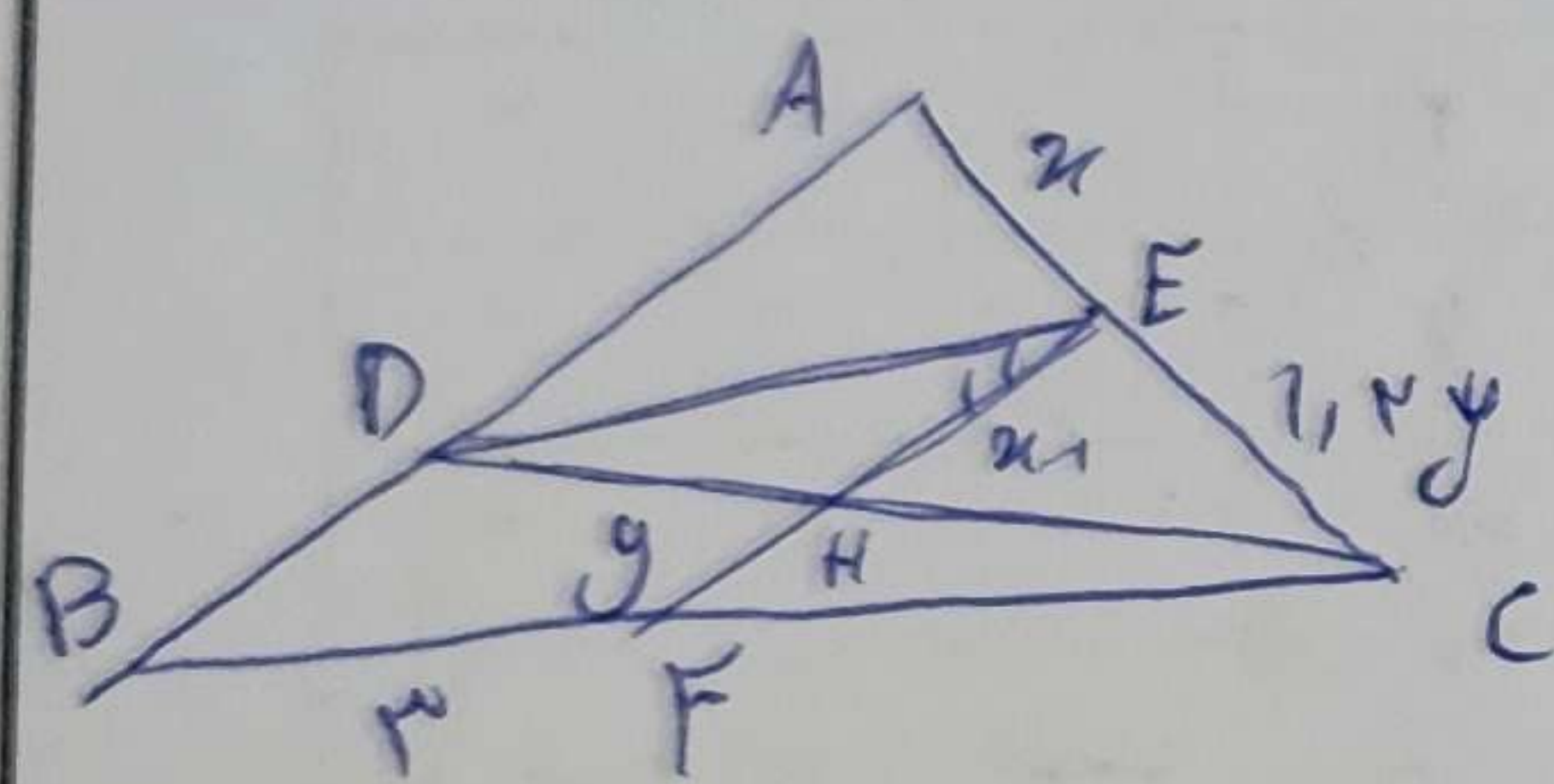
$$\frac{BC}{AE} = \frac{32}{21} = 3 \rightarrow 12$$

$$\left. \begin{array}{l} \overline{BE} = \sqrt{(32)^2 + 21^2} = \sqrt{1021} \\ \overline{AC} = \sqrt{(32)^2 + (32)^2} = 32\sqrt{2} \\ \overline{EF} \in \overline{BC} \Rightarrow \frac{1}{3} \overline{BC} = \overline{EF} \rightarrow \overline{EF} = \frac{\sqrt{1021}}{3} \cdot 21 \\ \overline{AF} \in \overline{AC} \Rightarrow \frac{1}{3} \overline{AC} = \overline{AF} \rightarrow \overline{AF} = \frac{32\sqrt{2}}{3} \cdot 21 \end{array} \right\} \Rightarrow \frac{\sqrt{1021}}{3}$$



$$\left. \begin{array}{l} \triangle AED \sim \triangle ABC \\ \hat{A} \text{ مشترک} \end{array} \right\} \Rightarrow \frac{AE}{AC} = \frac{AD}{AB} \Rightarrow \frac{21}{10} = \frac{2}{21+1} \Rightarrow 21^2 + 21 - 2 = 0$$

$$21 = 0 \quad 21 = -4$$



$$\left. \begin{array}{l} 3y = 2x \\ H_1 \neq H_1 \\ E_1 = F_1 \end{array} \right\} \Rightarrow \triangle HDE \sim \triangle HFE$$

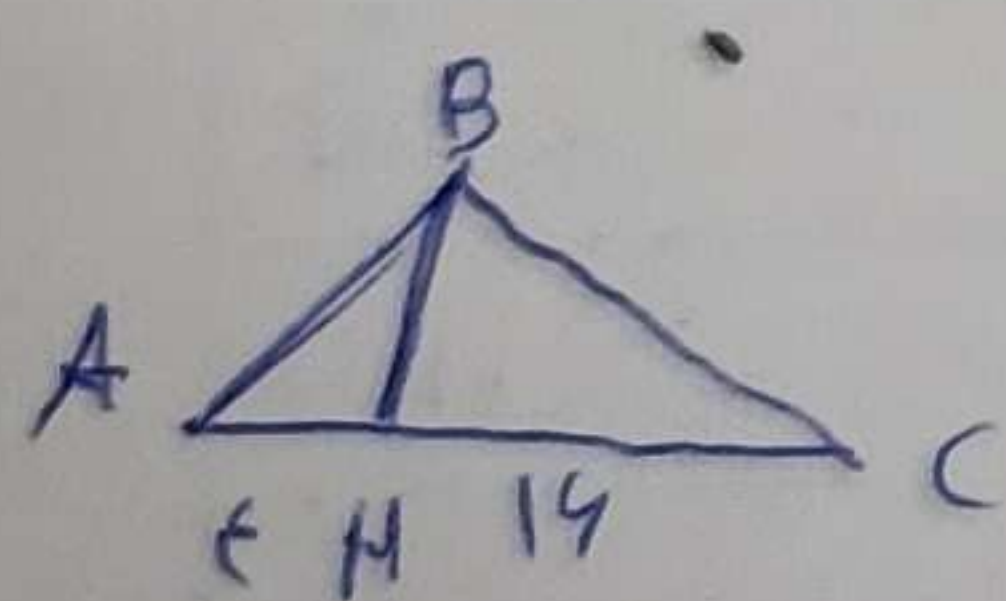
$$\overline{DE} \parallel \overline{BC} \rightarrow \frac{DE}{BC} = \frac{AD}{AB} = \frac{AE}{AC}$$

$$\frac{3x}{2y} = \frac{DE}{CF} \rightarrow 2z$$

$$\begin{aligned} 3y &= 2x \\ 11y &= \frac{2x}{3} \times \frac{4}{21} \times x \\ 11y &= 2x \end{aligned}$$

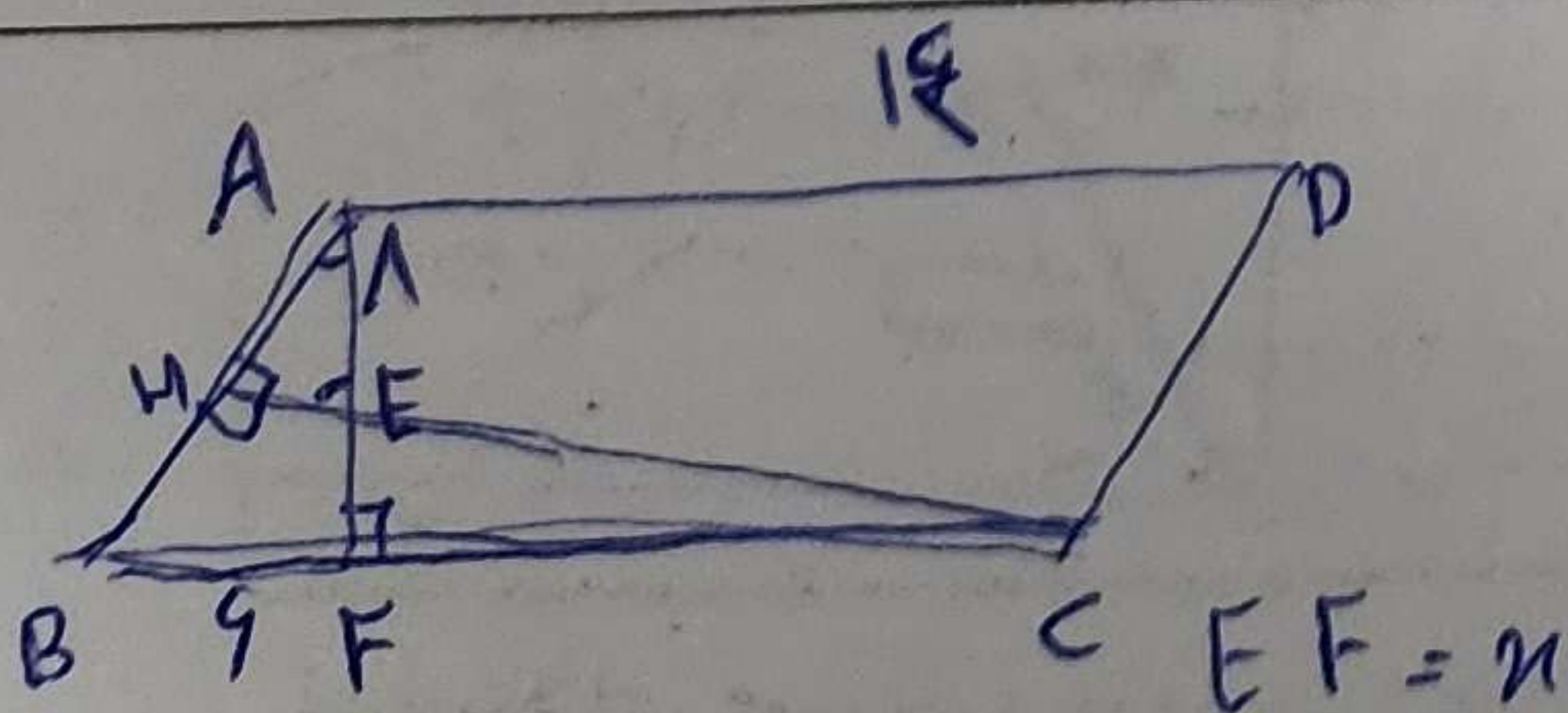
$$\frac{3z}{2z+3} = \frac{2}{11y+21} \Rightarrow \frac{3z}{2z+3} = \frac{2}{32}$$

$$BC = 3 + 2z = \frac{17}{2} \checkmark$$



$$\begin{aligned} AB^2 &= AH \times AC \Rightarrow AB = 4\sqrt{5} \\ BC^2 &= CH \times AC \Rightarrow BC = 1\sqrt{5} \end{aligned}$$

نسبت ۲



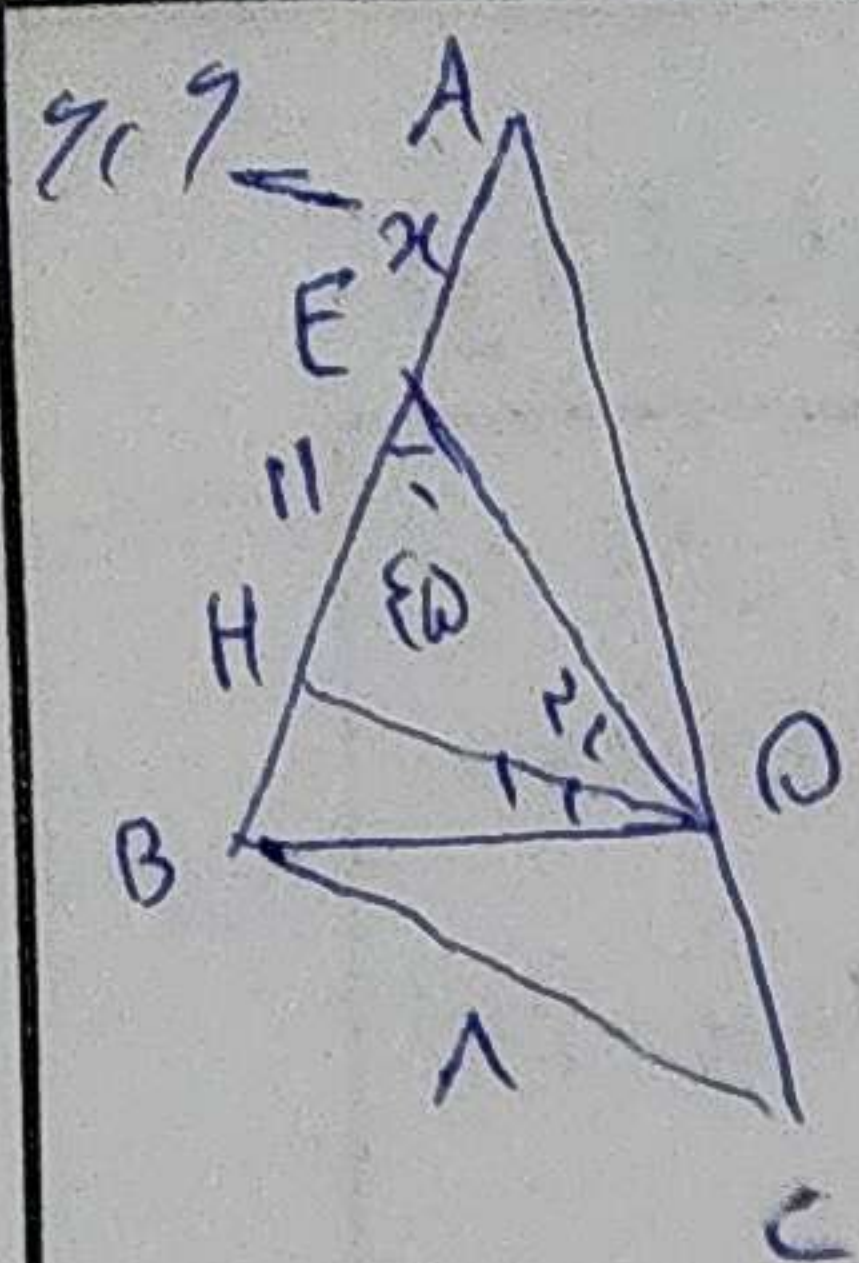
$$\left. \begin{array}{l} E_1 = F_1 \\ 90^\circ = H_1 = F_1 \end{array} \right\} \Rightarrow \triangle AHE \sim \triangle FEC$$

$$\left. \begin{array}{l} \hat{A}_1 = \hat{C}_1 \\ F_1 = F_1 = 90^\circ \end{array} \right\} \Rightarrow \triangle ABF \sim \triangle FEC$$

$$\begin{aligned} EF &= 4 \\ AF &= 1 + E = 12 \checkmark \end{aligned}$$

$$\frac{AB}{CE} = \frac{BF}{FE} = \frac{AF}{FC} \Rightarrow \frac{4}{2} = \frac{1+2}{1} \Rightarrow 2 = 3 \checkmark$$

$$2^2 + 12^2 = 14^2 \Rightarrow 14^2 = 14^2 \checkmark$$



$$B_1 = B_2$$

$$DH \parallel BC \rightarrow BP = D_1$$

$$B_1 + D_1 = 90$$

$$B_1 = B_2 = 90$$

$$\left. \begin{array}{l} B_1 = B_2 \\ B_1 = B_2 = D_1 = 90 \end{array} \right\} B_1 = B_2 = D_1 = 90$$

$$HD^2 = \sqrt{(\omega/\omega)^2} = \omega/\omega$$

$$B_1 + E_1 = 90$$

$$E_1 + E_1 = 90$$

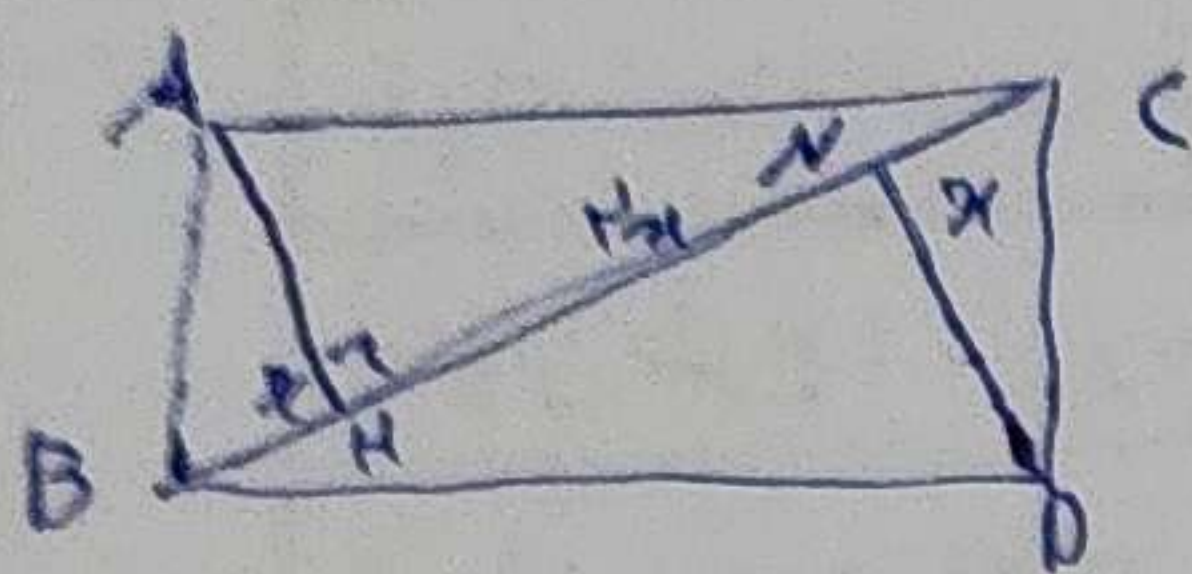
$$\downarrow$$

$$\left. \begin{array}{l} E_1 = B_1 \rightarrow BD = ED \\ D = 90 \end{array} \right\} EH = BH$$

$$\frac{H}{P} = \omega/\omega$$

$$DH \parallel BC \rightarrow \frac{DH}{BC} = \frac{AH}{AB} \Rightarrow \frac{\omega/\omega}{1} = \frac{x + \omega/\omega}{x + 1} \Rightarrow$$

$$\omega/\omega x + 9/\omega = 1 x + 9 \Rightarrow x = 9, 9 \checkmark$$



$$AB \perp C \rightarrow AH^2 = BH \times BC$$

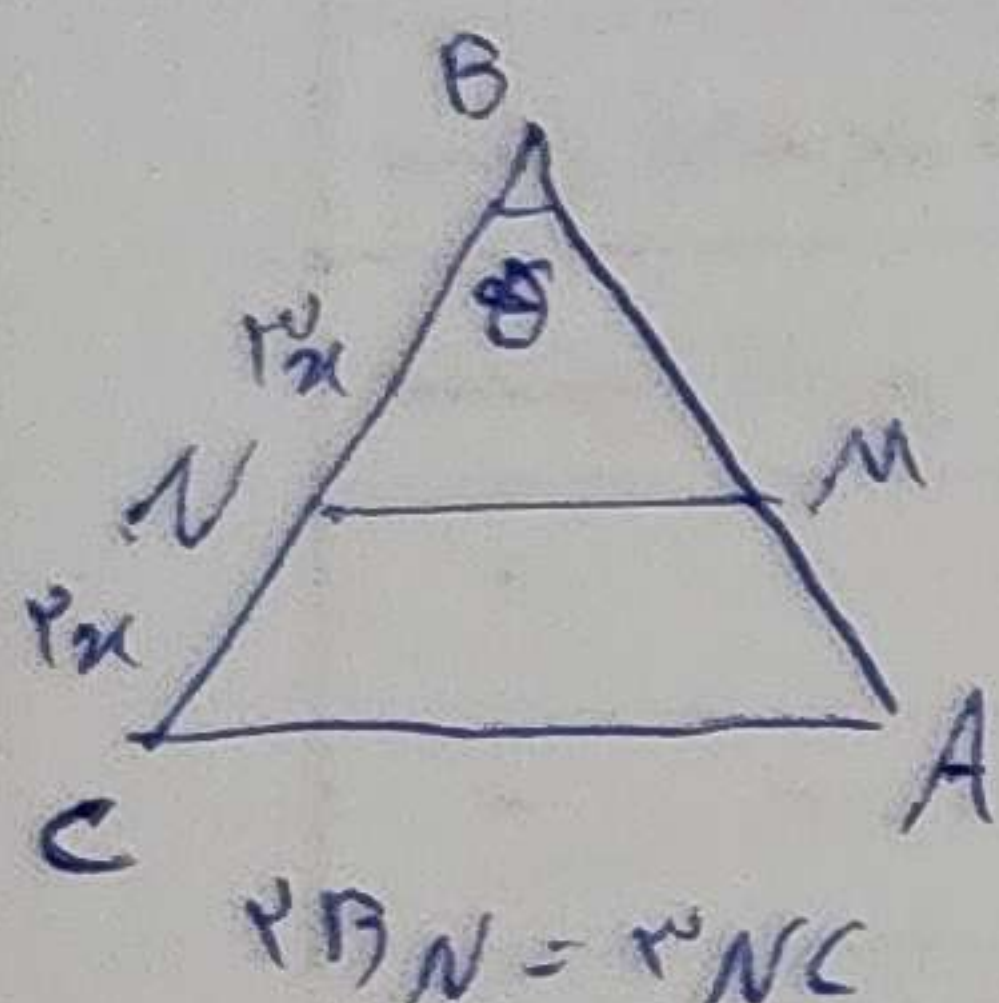
$$AH^2 = x \times y$$

$$AH = \sqrt{xy}$$

$$S \rightarrow ABC \perp S^2 = F \sqrt{xy}$$

$$NCD \perp ABHS = \frac{\sqrt{xy} \times x}{y} = \frac{\sqrt{xy} \times y}{x}$$

$$\frac{S_{ABHS}}{S_{ABHS}} = \frac{F \sqrt{xy}}{\sqrt{xy}} = 1 \checkmark$$



$$\frac{S_{ABC}}{S_{ANM}} = \frac{\frac{1}{2} \sin \theta BC \times AB}{\frac{1}{2} \sin \theta BN \times BM} = \frac{1}{y}$$

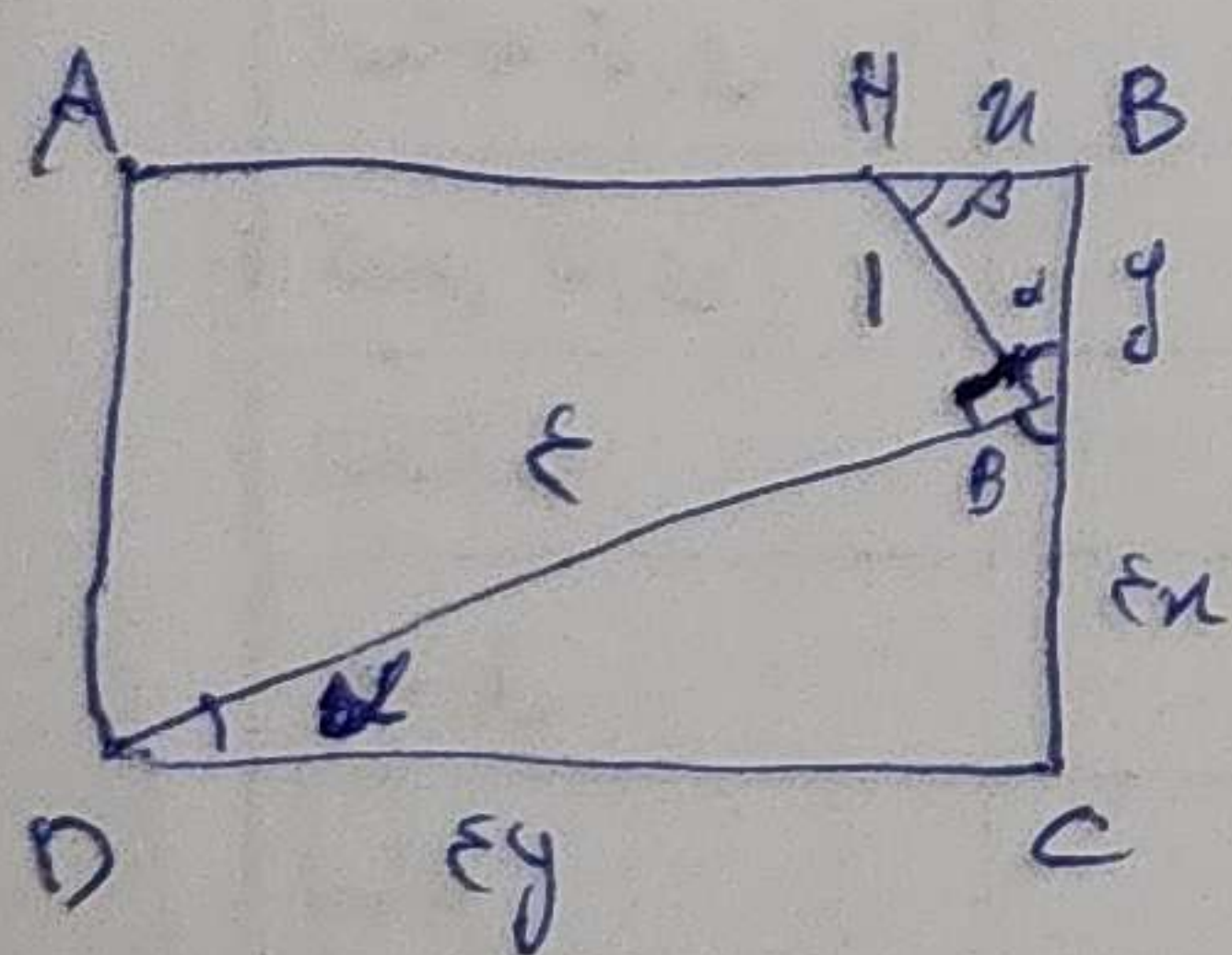
$$\frac{BC \times AB}{BN \times BM} = \frac{\omega/\omega}{y} \times \frac{BM + MA}{BM} = \frac{1}{y}$$

$$\frac{BM + MA}{BM} = \frac{1}{y}$$

$$\frac{1 + MA}{MB} = \frac{1}{y}$$

$$\frac{MA}{MB} = \frac{1}{y}$$

$$\frac{BM}{AM} = \frac{1}{y} \checkmark$$



$$x^2 + y^2 = 1 \rightarrow Ex + y = Ey$$

$$xy = Ex$$

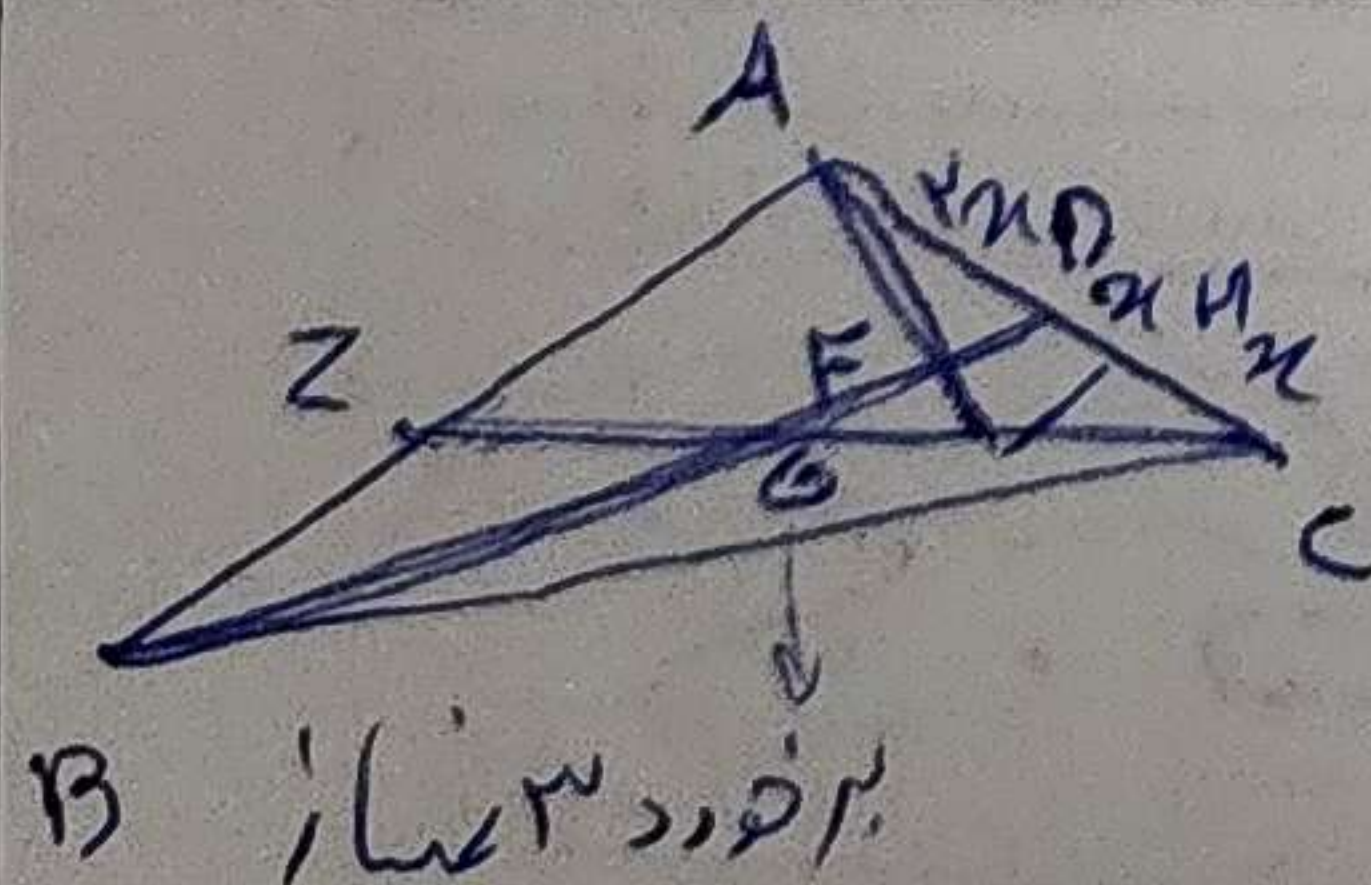
$$y = \frac{Ex}{x}$$

$$Ey = \frac{19}{\omega}$$

$$\frac{Ex}{x} = 1$$

$$\frac{1}{x} x = 1 \quad x = \frac{19}{\omega}, y = \frac{19}{\omega}$$

$$EGS = (Ey)^2 = \left(\frac{19}{\omega}\right)^2 = \frac{19 \times 19}{\omega^2} \checkmark$$



$$GE = EC$$

$$AB, EH \parallel BD \rightarrow BD \Rightarrow AD = DC$$

$$HE \parallel BD \Rightarrow \frac{FD}{EH} = \frac{AD}{AH} = \frac{1}{x} = \frac{1}{y}$$

$$HE \parallel BD \rightarrow \frac{EH}{GD} = \frac{CH}{CD} = \frac{1}{x} = \frac{1}{y}$$

$$\frac{GD}{BD} = \frac{1}{x}, \frac{EH}{BD} = \frac{1}{y}$$

$$\frac{1}{x} \times \frac{1}{y} = \frac{1}{9}$$

$$\frac{FD}{BD} \times \frac{FD}{EH} \times \frac{EH}{BD} = \frac{1}{9}$$

$$\frac{BD}{FD} = 9 \checkmark$$