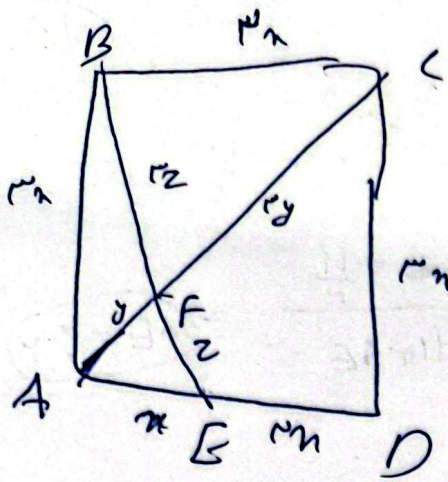


مسئله ۱۰۰

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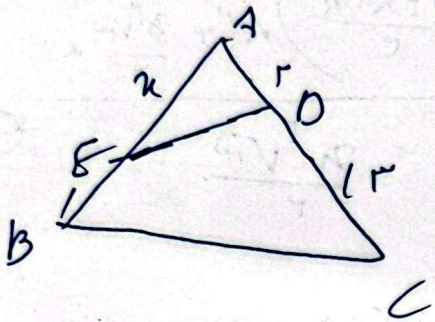


$$\sqrt{1+n^2} = r_2 \Rightarrow r_2 = \frac{n\sqrt{1+n^2}}{\epsilon}$$

$$\sqrt{1+n^2} = r_2 \sqrt{1+n^2} \Rightarrow y = \frac{r_2 \sqrt{1+n^2}}{\epsilon}$$

$$\frac{x}{y} = \frac{\frac{n\sqrt{1+n^2}}{\epsilon}}{\frac{r_2 \sqrt{1+n^2}}{\epsilon}} = \frac{n}{r_2}$$

۲



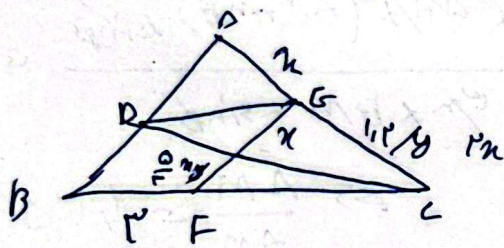
$$\frac{r}{1+n} \leq \frac{n}{l}$$

$$\Rightarrow n^2 + n \leq l$$

$$n^2 + n - l \leq (n+1)(n-1)$$

$$(n+1)(n-1)$$

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$$\frac{DE}{BC} \leq \frac{1}{r}$$

$$\frac{DE}{FC} \leq \frac{r}{\omega}$$

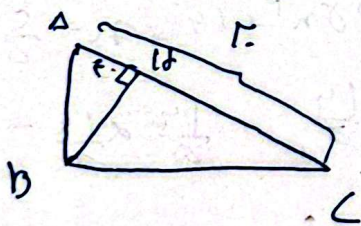
$$r DE \leq BC \Rightarrow r DE \leq r + FC$$

$$r DE \leq r + FC \Rightarrow DE \leq \frac{r}{r}$$

۴

$$\frac{r}{2} DE \leq FC$$

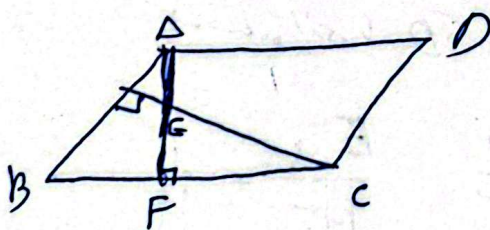
$$\frac{r}{2} DE \leq \frac{r}{2} \Rightarrow DE \leq \frac{r}{2}$$



$$AB \leq AC \Rightarrow AB \leq \sqrt{1+n^2}$$

$$BC \leq \sqrt{1+n^2} \Rightarrow BC \leq \sqrt{1+n^2}$$

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$$\triangle AFB \sim \triangle CFE$$

$$\frac{AF}{EF} = \frac{AB}{FC}$$

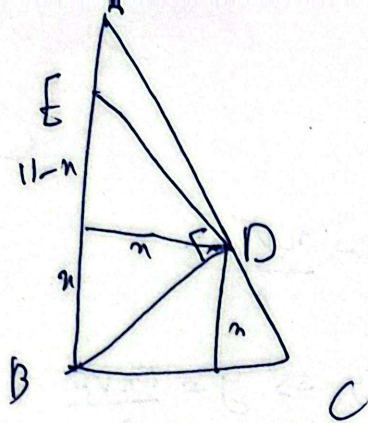
$$FF \leq r$$

$$r \leq r + FC$$

$$(r+1)(r-1)$$

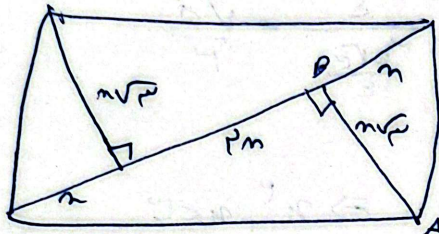
$$(r+1)(r-1)$$

$$r \leq r$$



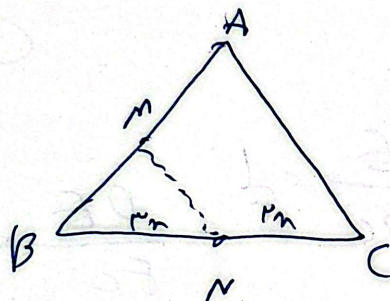
$$n^2 = n(11-n) \quad \leftarrow \begin{matrix} n \cdot \text{side} \\ n \cdot \frac{11}{2} \cdot \text{side} \end{matrix}$$

$$\frac{11}{2} = \frac{AE + \frac{11}{2}}{11 + AE} \Rightarrow AE = \frac{11}{4}$$

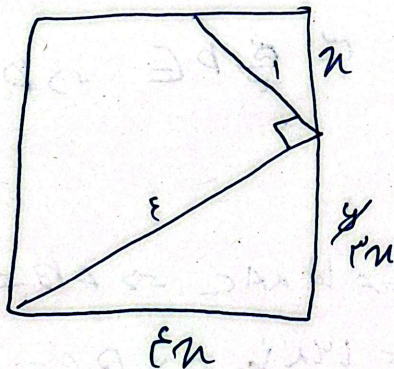


$$n \sin \theta = AB \cdot \sin \theta \Rightarrow AB = n\sqrt{2}$$

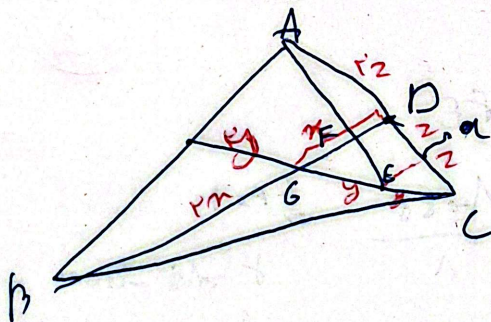
$$\frac{1}{2} \times \left(\frac{n\sqrt{2} \times n}{2} \right) \times 2 + \frac{n\sqrt{2} \times n}{2} \times 2 = \frac{n^2 \sqrt{2}}{2}$$



$$\frac{1}{2} \times \frac{2n}{2} (AM + MB) \sin \theta = \frac{1}{2} \times n \times BM \sin \theta \Rightarrow \frac{BM}{AM} = \frac{1}{2}$$



$$14n^2 + 9n^2 = 14 \Rightarrow 23n^2 = 14 \Rightarrow n = \frac{14}{23}$$



مقدارهای GD و GE را بیابید

$$\frac{FD}{EG} = \frac{1}{2} \quad \frac{EG}{AG} = \frac{1}{2}$$

$$\Rightarrow \frac{FD}{DG} = \frac{1}{2} \Rightarrow FD = \frac{1}{3} n, \quad BD = \frac{2}{3} n \quad \frac{BD}{FD} = 2$$