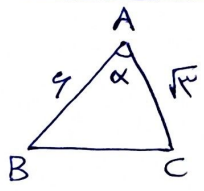


ایزوسم پسر A

تکلیف شتاب ۲۷

ایلیا مسلطی



$$S = \frac{1}{2} \times 4 \times 2\sqrt{5} \times \sin \alpha = 4\sqrt{5} \sin \alpha = \frac{1}{2} \Delta$$

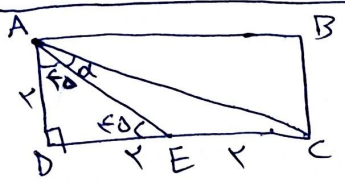
$$\Rightarrow \sin \alpha = \frac{\frac{1}{2} \Delta}{4\sqrt{5}} = \frac{4}{4\sqrt{5}} = \frac{1}{\sqrt{5}}$$

$\alpha \in (0, \pi)$

$$\alpha_{\max} = 180^\circ$$

$$\alpha_{\min} = 0^\circ \Rightarrow \frac{\max}{\min} = \frac{180}{4} = 45$$

(۲) - 1

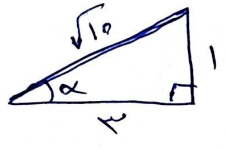


$$AE = \sqrt{4^2 + 4^2} = 4\sqrt{2}$$

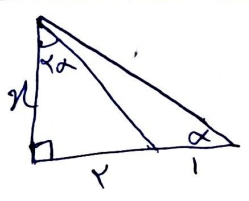
$$AC = \sqrt{4^2 + 4^2} = 4\sqrt{2}$$

$$EC = \sqrt{a^2 + b^2 - 2ab \cos \alpha} = \sqrt{16 + 16 - 16\sqrt{2} \cos \alpha} = 4\sqrt{2 - \sqrt{2} \cos \alpha}$$

$$\Rightarrow \sqrt{16 - 16\sqrt{2} \cos \alpha} = 4\sqrt{2} \Rightarrow 16 - 16\sqrt{2} \cos \alpha = 32 \Rightarrow \cos \alpha = \frac{3}{\sqrt{2}}$$



$$\cot \alpha = 3$$

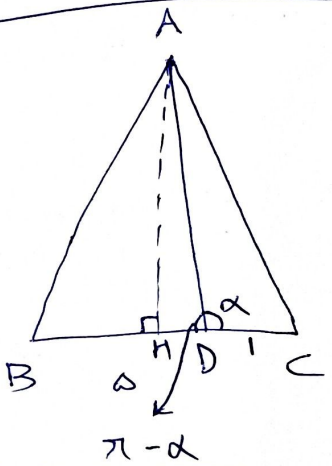


$$\tan \alpha = \frac{x}{1} \quad \cot 2\alpha = \frac{1}{\tan 2\alpha}$$

$$\cot 2\alpha = \frac{1 - \tan^2 \alpha}{2 \tan \alpha} = \frac{1 - \frac{x^2}{1}}{\frac{2x}{1}} = \frac{1 - x^2}{2x}$$

$$1 - \frac{x^2}{1} = \frac{x^2}{1} \Rightarrow \frac{1 - x^2}{1} = 1 \Rightarrow 1 - x^2 = 1 \Rightarrow x = 0$$

$$\Rightarrow \cot \alpha = \frac{1}{x} = \frac{1}{0} = \infty$$



$$AH = \sqrt{AB^2 - BH^2} = \sqrt{14^2 - 9^2} = \sqrt{105}$$

$$\tan(\pi - \alpha) = \frac{AH}{HD} = \frac{\sqrt{105}}{1}$$

$$\tan \alpha = -\tan(\pi - \alpha) = -\frac{\sqrt{105}}{1}$$

$$\sin^2 \alpha + \sin^2 \alpha + \cos^2 \alpha = \frac{1}{4} \Rightarrow \sin^2 \alpha = \frac{1}{8}$$

$$\Rightarrow \frac{1}{8} + \cos^2 \alpha = 1 \Rightarrow \cos^2 \alpha = \frac{7}{8}$$

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{\frac{1}{\sqrt{8}}}{\frac{\sqrt{7}}{\sqrt{8}}} = \frac{1}{\sqrt{7}}$$

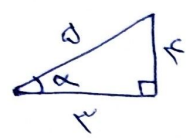
(۲) - 2

$$\sin^r \alpha = (\sin \alpha)^r = (1 - \cos \alpha)^r = \cos^r \alpha + 1 - r \cos \alpha$$

$$\cos^r \alpha = (\cos \alpha)^r = (1 - \sin \alpha)^r = \sin^r \alpha + 1 - r \sin \alpha$$

$$\frac{\cos^r \alpha + 1 - r \cos \alpha + r \cos \alpha}{1 + \cos \alpha} - \frac{\sin^r \alpha + 1 - r \sin \alpha}{1 + \sin \alpha}$$

$$= \frac{(\cos^r \alpha + 1)^r}{\cos^r \alpha + 1} - \frac{(\sin^r \alpha + 1)^r}{\sin^r \alpha + 1} = \cos^r \alpha + 1 - \sin^r \alpha - 1 = \cos^r \alpha - \sin^r \alpha$$



$$\sin \alpha = -\frac{r}{a} \quad \cot \alpha = \frac{r}{r}$$

$$\cos \alpha = -\frac{r}{a}$$

$$\sin\left(\frac{9\pi}{r} + \alpha\right) = \cos \alpha = -\frac{r}{a} \quad \cos\left(\frac{v\pi}{r} - \alpha\right) = -\sin \alpha = \frac{r}{a}$$

$$\tan\left(\alpha - \frac{r\pi}{r}\right) = -\cot \alpha = -\frac{r}{r}$$

$$\sin\left(\frac{9\pi}{r} + \alpha\right) \cos\left(\frac{v\pi}{r} - \alpha\right) - \tan\left(\alpha - \frac{r\pi}{r}\right) = \left(-\frac{r}{a}\right) \times \frac{r}{a} - \left(-\frac{r}{r}\right)$$

$$= \frac{-r^2 + va}{100} = \boxed{\frac{rv}{100}}$$

$$r \cos r\pi = r \cos \frac{\pi}{r} = r \times \frac{1}{r} = \frac{r}{r}$$

$$\sqrt{r} \sin \pi - \sqrt{r} \cos \pi = \sqrt{r} (\sin \pi - \cos \pi)$$

$$\xrightarrow{\text{relax}} r (\sin^r \pi + \cos^r \pi - r \sin \pi \cos \pi) = r (1 - \sin^r \pi)$$

$$= r - r \sin \frac{\pi}{r} = r - 1 = 1 \Rightarrow \sqrt{r} \sin \pi - \sqrt{r} \cos \pi = \begin{matrix} 1 \checkmark \\ -1 \times \end{matrix}$$

$$\Rightarrow \frac{r}{r} + (-1) = \boxed{\frac{1}{r}}$$

$\sin \pi - \cos \pi \Leftrightarrow \pi = \frac{\pi}{14}$

$$\frac{\sin \frac{\alpha}{r}}{\cos \frac{\alpha}{r}} = \frac{1}{r} \Rightarrow \cos \frac{\alpha}{r} = r \sin \frac{\alpha}{r}$$

$$\sin^r \frac{\alpha}{r} + \cos^r \frac{\alpha}{r} = 1$$

$$\sin \alpha = r \sin \frac{\alpha}{r} \cos \frac{\alpha}{r} = r \times \frac{1}{\sqrt{14}} \times \frac{r}{\sqrt{14}} = \frac{r}{14}$$

$$\Rightarrow \sin^r \frac{\alpha}{r} + 14 \sin^r \frac{\alpha}{r} = 1 \Rightarrow \sin \frac{\alpha}{r} = \frac{1}{\sqrt{14}}$$

$$\cos \alpha = \cos^r \frac{\alpha}{r} - \sin^r \frac{\alpha}{r} = \frac{14}{14} - \frac{1}{14} = \frac{13}{14}$$

$$\cos \frac{\alpha}{r} = \frac{r}{\sqrt{14}}$$

$$\frac{\tan \alpha - \sin \alpha}{\sin \alpha - \cos \alpha} = \frac{\frac{r}{14} - \frac{r}{14}}{\frac{r}{14} - \frac{13}{14}} = \boxed{\frac{-14}{100}}$$

$$\sin^r \alpha = r \sin \alpha \cos \alpha \Rightarrow r \sin \alpha < r \sin \alpha \cos \alpha$$

$$\Rightarrow r \sin \alpha \cos \alpha - r \sin \alpha > 0 \quad r \sin \alpha (\cos \alpha - 1) > 0 \Rightarrow \sin \alpha < 0$$

$$\frac{\cot \alpha}{\sin \alpha} > 0 \Rightarrow \cot \alpha < 0 \Rightarrow \cos \alpha > 0 \Rightarrow \boxed{\text{r/100} = \text{val}}$$