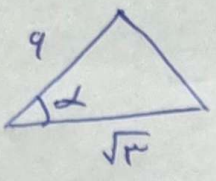


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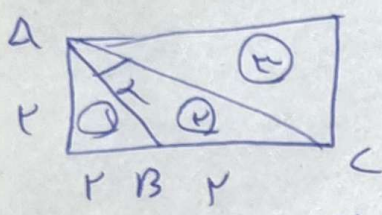
19, 17, 23



$$S_D = \frac{1}{r} a b \sin \alpha \rightarrow \frac{q}{r} = \frac{1}{r} \times \sqrt{r} \times \sqrt{r} \times \sin \alpha$$

$$\sin \alpha = \frac{\sqrt{r}}{r} \rightarrow \alpha = \begin{cases} 40^\circ, 110^\circ \rightarrow \text{max} \\ \downarrow \\ \text{min} \end{cases}$$

$$\frac{110^\circ}{40^\circ} = \boxed{r} \checkmark$$



$$AB = \sqrt{r^2 + r^2} = r\sqrt{2}$$

$$AC = r\sqrt{2}$$

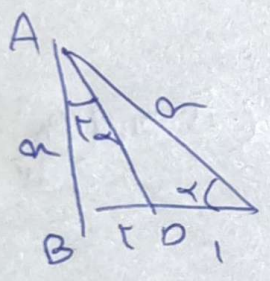
$$S_{\text{rect}} = r \times r = r^2$$

$$\begin{aligned} S_{\text{tri}} &= r^2 \\ S_1 &= r \end{aligned}$$

$$r = \frac{1}{r} \times r\sqrt{2} \times r\sqrt{2} \sin \alpha$$

$$\sin \alpha = \frac{1}{\sqrt{2}}$$

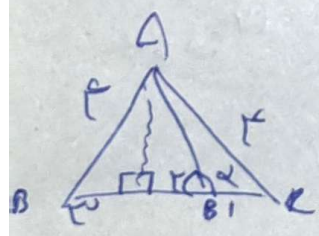
$$\sin \alpha = \frac{1}{\sqrt{2}}, \quad \boxed{90^\circ = \alpha} \checkmark$$



$$\tan 2\alpha = \frac{r \tan \alpha}{1 - \tan^2 \alpha} = \frac{r}{\alpha}$$

$$\tan \alpha = \frac{\alpha}{r} \rightarrow \frac{r}{\alpha} = \frac{r \alpha}{r^2 - \alpha^2} = \frac{4\alpha}{2 - \alpha^2}$$

$$1 - \tan^2 \alpha = 4\alpha^2 \rightarrow 1 - \frac{\alpha^2}{r^2} = 4\alpha^2 \rightarrow \boxed{\alpha = \frac{r}{r}} \checkmark$$



$$AH = \sqrt{r^2 - \left(\frac{r}{2}\right)^2} \rightarrow AH = \sqrt{r^2 - \frac{r^2}{4}} = \frac{\sqrt{3}}{2} r$$

$$\tan B = \frac{\sqrt{3}}{1} \rightarrow \tan \alpha = \tan(\pi - B) = -\tan B$$

$$\boxed{\tan \alpha = \frac{\sqrt{3}}{1}} \checkmark$$

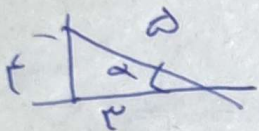
$$\sin^2 \alpha = \frac{1}{r^2} \rightarrow \sin \alpha = \frac{1}{\sqrt{r}} = \frac{\sqrt{r}}{r} \rightarrow \sqrt{r} \begin{array}{c} r \\ \alpha \\ t \end{array} \quad -2$$

$$t = \sqrt{r} \rightarrow (\tan \alpha = \frac{\sqrt{r}}{\sqrt{r}})^r \rightarrow \tan \alpha = \frac{r}{r} = \frac{1}{1} \checkmark$$

$$\frac{\sin^2 \alpha + t(1 - \sin^2 \alpha)}{1 + (1 - \sin^2 \alpha)} = \frac{\cos^2 \alpha + t(1 - \cos^2 \alpha)}{1 + (1 - \cos^2 \alpha)} \quad -4$$

$$\frac{(\sin^2 \alpha - r)^r}{-(-r + \sin^2 \alpha)} = \frac{(\cos^2 \alpha - r)^r}{-(-r + \cos^2 \alpha)} = -\sin^2 \alpha + r + \cos^2 \alpha - r =$$

$$\cos^2 \alpha - \sin^2 \alpha = \boxed{\cos^2 \alpha} \checkmark$$



$$\begin{array}{l} \sin \rightarrow \ominus \\ \cos \rightarrow \ominus \end{array} \rightarrow \cos \alpha (-\sin \alpha) + \cos \alpha = -\frac{r}{r} \left(\frac{r}{r}\right) + \frac{r}{r} = \frac{r-r}{r} = \frac{0}{r} \checkmark \quad -5$$

$$r \cos \frac{r}{r} + \sqrt{r} \left(\sin \frac{r}{r} - \cos \frac{r}{r} \right) = \frac{r}{r} + \sqrt{r} \left(\sqrt{r} \sin \left(\frac{r}{r} - \frac{r}{r} \right) \right) = \frac{r}{r} + r \sin \left(-\frac{r}{r} \right) = \frac{r}{r} - 1 = \boxed{\frac{1}{r}} \checkmark \quad -6$$

$$\left(\tan^2 \frac{\alpha}{r} \right) = \frac{1}{14} = \frac{1 - \cos \alpha}{1 + \cos \alpha} \rightarrow 1 + \cos \alpha = 14 - 14 \cos \alpha \quad -9$$

$$\cos \alpha = \frac{10}{14}$$

$$\frac{\tan \alpha - \sin \alpha}{\sin \alpha - \cos \alpha} = \frac{\frac{1}{10} - \frac{1}{14}}{\frac{1}{14} - \frac{10}{14}} = \boxed{\frac{14}{100}} \checkmark$$

$$\frac{\cos \alpha}{\sin \alpha} > 0 \rightarrow \cos \alpha > 0 \rightarrow r \sin \alpha < r \sin \alpha \cos \alpha \rightarrow 1 < \cos \alpha$$

$$\boxed{r \cos \alpha} \checkmark$$

$$r \sin \alpha < r \sin \alpha \cos \alpha \rightarrow \sin \alpha < \cos \alpha$$