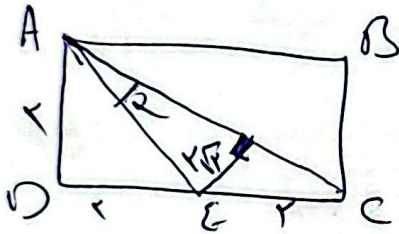


19, 175

$$S = \frac{1}{2} x y \rightarrow \frac{1}{2} x \sqrt{2} x \rightarrow \alpha = \frac{1}{\sqrt{2}}$$

$$S_{\text{في } \alpha} = \frac{\sqrt{2}}{2} \rightarrow \alpha \begin{cases} \alpha = 45^\circ \\ \alpha = 135^\circ \end{cases} \rightarrow \frac{150}{y} = 2 \quad \text{✓}$$

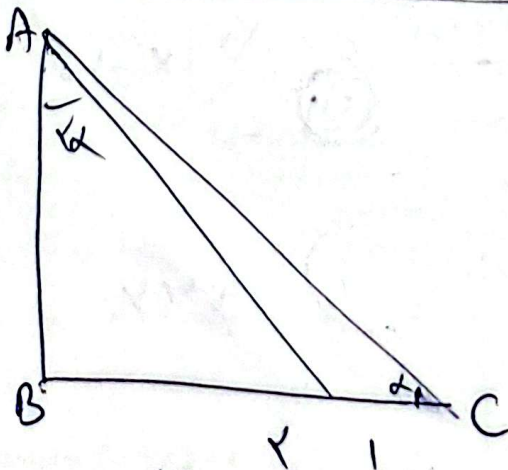


$$AC = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2} \rightarrow S_{\triangle ADE} = S_{\triangle AEC}$$

$$\Rightarrow \frac{2\sqrt{2} \times h}{2} = \frac{y \times x}{2} \rightarrow h = \frac{y\sqrt{2}}{2}$$

$$\Rightarrow (EH)^2 + (AH)^2 = (AE)^2 \rightarrow AH = \frac{y\sqrt{2}}{2}$$

$$\Rightarrow \cot \alpha = \frac{AH}{EH} = \frac{\frac{y\sqrt{2}}{2}}{\frac{y\sqrt{2}}{2}} = 1 \quad \text{✓}$$

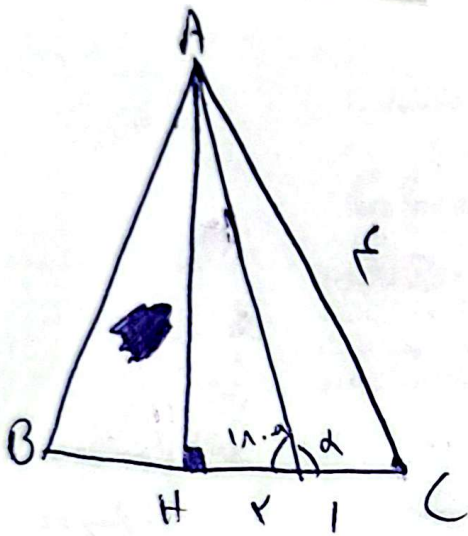


$$\tan \alpha = \frac{AB}{BC} \rightarrow \tan \alpha = \frac{y}{x}$$

$$\Rightarrow \tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha} \Rightarrow \frac{y}{x} = \frac{2 \frac{y}{x}}{1 - \frac{y^2}{x^2}}$$

$$\Rightarrow \frac{yAB(AB)}{yAB - y} = \frac{y}{AB}$$

$\cot \alpha = 1 \Rightarrow \tan \alpha = 1 \Rightarrow AB = \frac{y}{1} \Rightarrow yAB = y$



$$AH = \sqrt{14 - a} = \sqrt{V}$$

$$\Rightarrow \tan \alpha = -\tan(180^\circ - \alpha)$$

$$\Rightarrow \tan(180^\circ - \alpha) = \frac{\sqrt{V}}{r} \rightarrow \tan \alpha = \frac{-\sqrt{V}}{r}$$

$$r \sin^2 \alpha + \cos^2 \alpha = \frac{c}{c} \rightarrow r \sin^2 \alpha + 1 = \frac{c}{c} \rightarrow r \sin^2 \alpha = \frac{1}{r}$$

$$\Rightarrow \cos^2 \alpha = \frac{r}{r} \Rightarrow \tan^2 \alpha = \frac{1}{r} = \frac{1}{r}$$

$$\frac{r \sin^2 \alpha + \cos^2 \alpha}{1 + \cos^2 \alpha} = \frac{\cos^2 \alpha + \cos^2 \alpha}{1 + 1 - \cos^2 \alpha} = \frac{(r - r \sin^2 \alpha)^2}{r \sin^2 \alpha} = \frac{(r - \cos^2 \alpha)^2}{r \cos^2 \alpha}$$

$$\Rightarrow r - r \sin^2 \alpha - r + \cos^2 \alpha = \cos^2 \alpha - r \sin^2 \alpha = \cos^2 \alpha$$

$$-r \left( \frac{r}{r} + \alpha \right) \cos \left( \frac{r}{r} - \alpha \right) - \tan \left( \alpha - \frac{r}{r} \right) = -r \sin^2 \alpha + \cos^2 \alpha$$

$$\Rightarrow - \left( -\frac{r}{r} \right) \left( -\frac{r}{r} \right) + \frac{r}{r} = \frac{-r \sin^2 \alpha}{1} = \frac{1 - r}{1} = \frac{1 - r}{1}$$

0, rV

(۲) (۱)

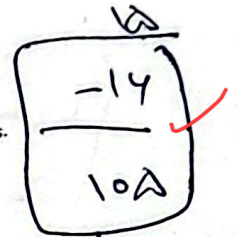
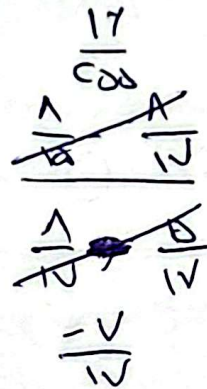
$$r \cos\left(\frac{R}{r}\right) + \sqrt{r} (\sin \alpha - \cos \alpha) = r \cos \frac{R}{r} + \sqrt{r} (\sqrt{r} \sin\left(\frac{R}{r} - \frac{R}{r}\right))$$

$$\Rightarrow \left(r \times \frac{1}{r}\right) + r \left(\frac{-1}{r}\right) = \frac{r}{r} - 1 \Rightarrow \boxed{\frac{1}{r}} \leftarrow \text{جواب}$$

$$\tan \alpha = \frac{r \tan \alpha}{1 - \tan^2 \alpha} \Rightarrow \tan \alpha = \frac{1}{\frac{10}{14}} = \frac{14}{10}$$

(۲) (۴)

$$\Rightarrow \tan \alpha = \frac{A}{W} \Rightarrow \begin{cases} \sin \alpha = \frac{A}{10} \\ \cos \alpha = \frac{W}{10} \end{cases}$$



$$r \sin \alpha < r \sin \alpha \cos \alpha \Rightarrow r \sin \alpha - r \sin \alpha \cos \alpha < 0$$

(۲) (۱۰)

$$\Rightarrow r \sin \alpha (1 - \cos \alpha) < 0 \Rightarrow \underbrace{r \sin \alpha}_{(-)} (\underbrace{\cos \alpha - 1}_{(-)}) > 0$$

$$\Rightarrow \frac{\cos \alpha}{\sin \alpha} > \cos \alpha \Rightarrow \sin \alpha < 1 \Rightarrow r \text{ موجوب$$