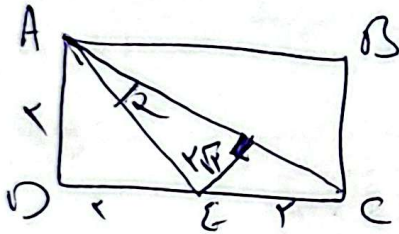


$S = \frac{1}{2} r y \rightarrow \frac{1}{2} \times \sqrt{r^2 + y^2} \times h \rightarrow \alpha = \frac{1}{2} \frac{r y}{\sqrt{r^2 + y^2}}$

$S_{\Delta} \alpha = \frac{\sqrt{r^2 + y^2}}{2} \rightarrow \alpha = \frac{r y}{\sqrt{r^2 + y^2}}$

(1)



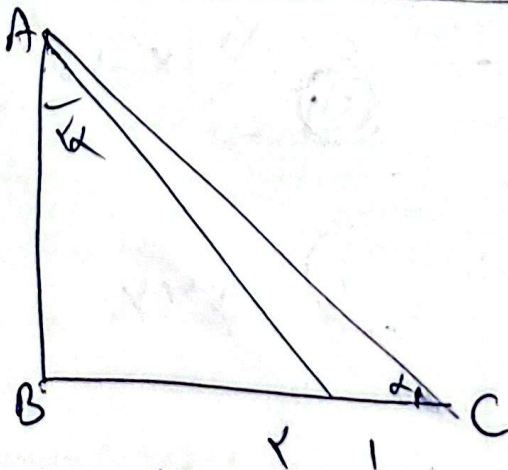
$AC = \sqrt{r^2 + y^2} = \sqrt{r^2 + y^2} = r\sqrt{1 + \frac{y^2}{r^2}} \rightarrow S_{\Delta ADE} = S_{\Delta AEC}$

$\Rightarrow \frac{r \sqrt{1 + \frac{y^2}{r^2}} \times EH}{2} = \frac{y \times \frac{y}{2}}{2} \rightarrow EH = \frac{y \sqrt{1 + \frac{y^2}{r^2}}}{2}$

$\Rightarrow (EH)^2 + (AH)^2 = (AE)^2 \rightarrow AH = \frac{y \sqrt{1 + \frac{y^2}{r^2}}}{2}$

$\Rightarrow \cot \alpha = \frac{AH}{EH} = \frac{\frac{y \sqrt{1 + \frac{y^2}{r^2}}}{2}}{\frac{y \sqrt{1 + \frac{y^2}{r^2}}}{2}} = 1$

(2)



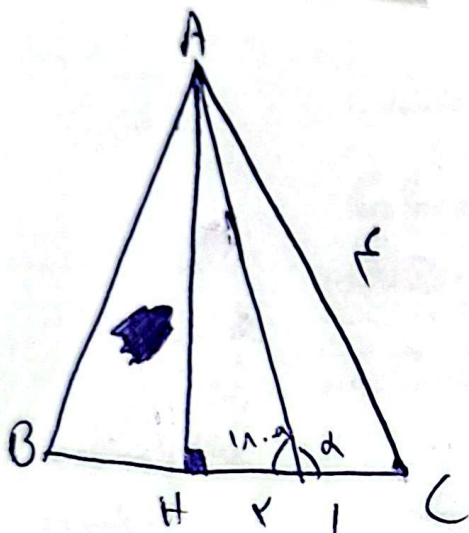
$\tan \alpha = \frac{AB}{BC} \rightarrow \tan \alpha = \frac{r}{y}$

$\Rightarrow \tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha} = \frac{2 \frac{r}{y}}{1 - \frac{r^2}{y^2}} = \frac{2 r y}{y^2 - r^2}$

$\Rightarrow \frac{2 r y (y^2 - r^2)}{y^2 - r^2} = \frac{2 r y}{y^2 - r^2}$

$\cot \alpha = \frac{1}{\tan \alpha} = \frac{y}{r} \Rightarrow AB = \frac{r y}{y} = r$

(3)



$$AH = \sqrt{14 - a} = \sqrt{V}$$

$$\Rightarrow \tan \alpha = -\tan(180^\circ - \alpha)$$

$$\Rightarrow \tan(180^\circ - \alpha) = \frac{\sqrt{V}}{r} \rightarrow \boxed{\tan \alpha = \frac{-\sqrt{V}}{r}}$$

$$r \sin^2 \alpha + \cos^2 \alpha = \frac{e}{c} \rightarrow r^2 \sin^2 \alpha + 1 = \frac{e}{c} \rightarrow r^2 \sin^2 \alpha = \frac{1}{r^2} \quad (2)$$

$$\Rightarrow \cos^2 \alpha = \frac{r}{r^2} \Rightarrow \tan^2 \alpha = \frac{\frac{1}{r^2}}{\frac{r}{r^2}} = \boxed{\frac{1}{r}} \leftarrow$$

$$\frac{r \sin^2 \alpha + \cos^2 \alpha}{1 + \cos^2 \alpha} = \frac{\cos^2 \alpha + e(1 - \cos^2 \alpha)}{1 + 1 - \cos^2 \alpha} = \frac{(r - r \sin^2 \alpha)^2}{r \sin^2 \alpha} \cdot \frac{(r - \cos^2 \alpha)}{r - \cos^2 \alpha}$$

$$\Rightarrow r - r \sin^2 \alpha - r + \cos^2 \alpha = \cos^2 \alpha - r \sin^2 \alpha = \boxed{\cos^2 \alpha}$$

$$-r \sin^2 \left(\frac{90^\circ}{r} + \alpha \right) \cos \left(\frac{90^\circ}{r} - \alpha \right) - \tan \left(\alpha - \frac{90^\circ}{r} \right) = -r \sin^2 \alpha \cos \alpha + \cot \alpha \quad (3)$$

$$\Rightarrow -\left(-\frac{e}{\omega}\right) \left(-\frac{r}{\omega}\right) + \frac{r}{e} = \frac{e \Lambda \omega \omega}{1 \dots} = \frac{13r}{1 \dots} = \boxed{1, r} \leftarrow$$

①

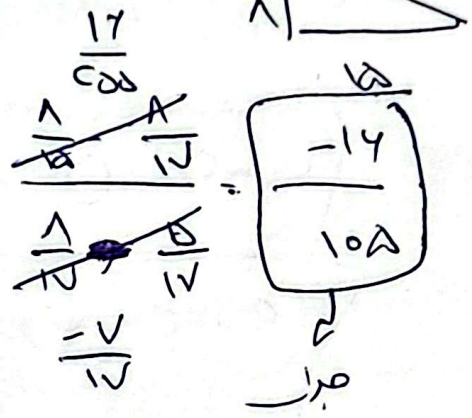
$$r \cos\left(\frac{R}{r}\right) + \sqrt{r} (\sin \alpha - \cos \alpha) = r \cos \frac{R}{r} + \sqrt{r} (\sqrt{r} \sin\left(\frac{R}{r} - \frac{R}{r}\right))$$

$$\Rightarrow \left(r \times \frac{1}{r}\right) + r \left(\frac{-1}{r}\right) = \frac{r}{r} - 1 \Rightarrow \boxed{\frac{1}{r}} \leftarrow \text{جواب}$$

$$\tan \alpha = \frac{r \tan \alpha}{1 - \tan^2 \alpha} \Rightarrow \tan \alpha = \frac{1}{\frac{10}{14}} = \frac{14}{10}$$

④

$$\Rightarrow \tan \alpha = \frac{A}{B} \Rightarrow \begin{cases} \sin \alpha = \frac{A}{10} \\ \cos \alpha = \frac{B}{12} \end{cases}$$



$$r \sin \alpha < r \sin \alpha \cos \alpha \Rightarrow r \sin \alpha - r \sin \alpha \cos \alpha < 0 \quad \text{⑤}$$

$$\Rightarrow r \sin \alpha (1 - \cos \alpha) < 0 \Rightarrow \underbrace{r \sin \alpha}_{(-)} (\underbrace{\cos \alpha - 1}_{(-)}) > 0$$

$$\Rightarrow \frac{\cos \alpha}{\sin \alpha} = \cot \alpha > 0 \Rightarrow \sin \alpha < 0 \Rightarrow r \text{ neg$$