

$$\cot x = \frac{\cos x}{\sqrt{1-\cos x}} \Rightarrow \frac{\cos x}{\sin x} = \frac{\cos x}{\sqrt{1-\cos x}} = \frac{\cos x}{|\sin x|} \Rightarrow |\sin x| = \sin x \Rightarrow \sin x \geq 0 \quad (1)$$

$$\frac{1}{\sqrt{\cos x}} - \frac{1}{\cot x} = \frac{1-\sin x}{|\cos x|} \Rightarrow \frac{1}{|\cos x|} - \frac{\sin x}{\cos x} = \frac{1-\sin x}{|\cos x|} \Rightarrow |\cos x| = \cos x \Rightarrow \cos x \geq 0 \quad (11)$$

5 (1) \cap (11) \Rightarrow Jod ✓

$$-\frac{\pi}{4} < x < \frac{\pi}{4} \Rightarrow -\frac{1}{\sqrt{2}} < \sin x < \frac{1}{\sqrt{2}} \Rightarrow -\frac{1}{\sqrt{2}} < \frac{m-1}{\sqrt{2}} \leq 1 \quad (2)$$

$$\Rightarrow -\sqrt{2} < m-1 \leq \sqrt{2} \Rightarrow \boxed{-1 < m \leq 2} \quad \checkmark$$

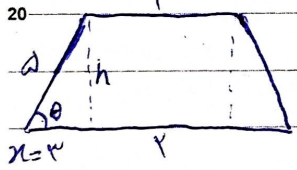
$$\frac{3\pi}{4} < x < \pi \Rightarrow \sin x + \cos x < 0 \Rightarrow \frac{\sin x}{\cos x} + \frac{\cos x}{\sin x} = -\sqrt{2} \quad (2)$$

$$\Rightarrow \frac{\sin^2 x + \cos^2 x}{\sin x \cos x} = -\sqrt{2} \Rightarrow \frac{1}{\sin x \cos x} = -\sqrt{2} \Rightarrow \sin x \cos x = -\frac{1}{\sqrt{2}}$$

$$15 \frac{1}{\sin^2 x + \cos^2 x} = \frac{1}{(\sin + \cos)(\sin^2 + \cos^2 - \sin \cos)} = \frac{1}{\sqrt{2}(\sin + \cos)}$$

$$\frac{1}{\sqrt{2} \sqrt{\sin^2 + \cos^2 + \sqrt{2} \sin \cos}} = \frac{1}{\sqrt{2} \times (-\frac{1}{\sqrt{2}})} = \boxed{\frac{\sqrt{2}}{-1}} \quad \checkmark$$

$$20 \cos \theta = \frac{9}{9} \Rightarrow x = 9 \times \frac{9}{9} = 9 \Rightarrow h = 9 \quad (2)$$



$$S = \frac{9(R+r)}{2} = \boxed{90} \quad \checkmark$$

$$\tan(x\Delta) = \tan\left(\frac{3\pi}{4} + \Delta\right) = -\cot \Delta \quad (2)$$

$$25 \tan(-1\Delta) = \tan(-\pi + \Delta) = \tan \Delta$$

$$\sin(1.9\Delta) = \sin(4\pi + \Delta) = \sin \Delta$$

$$\cos\left(\frac{3\pi}{4} - \Delta\right) = -\sin \Delta$$

$$\Rightarrow \tan(x\Delta) \tan(-1\Delta) - \sin(1.9\Delta) \cos(1.2\Delta) = k \cos^2 \Delta$$

$$30 (-\cot \Delta)(\tan \Delta) - (\sin \Delta)(-\sin \Delta) = \text{---} - 1 - (-\sin^2 \Delta) = -\cos^2 \Delta$$

$$-\cos^2 \Delta = k \cos^2 \Delta \Rightarrow \boxed{k = -1} \quad \checkmark$$

$$\sin(\pi + 4\pi) = \sin(\pi + 4\pi) = -\sin 4\pi = -\cos 4\pi \quad (r) \quad -9$$

$$\cos 10\pi = \cos(\pi - 4\pi) = -\cos 4\pi$$

$$A = \sqrt{r} \times \left(-\frac{\sqrt{r}}{r}\right) \times (-\cos 4\pi) = \sqrt{r} \times \frac{\sqrt{r}}{r} \times (-\cos 4\pi) = \cos 4\pi \left(\frac{r}{r} + 1\right)$$

$$\Rightarrow \frac{A}{\cos 4\pi} = \frac{\frac{r}{r} \cos 4\pi}{\cos 4\pi} = \boxed{\frac{r}{r}} \quad = \frac{r}{r} \cos 4\pi \quad 5$$

$$f\left(\frac{\pi}{19}\right) = 14 \underbrace{\cos\left(\frac{\pi}{19}\right)}_{1 + \cos \frac{2\pi}{9}} \underbrace{\cos\left(\frac{\pi}{9}\right)}_{\frac{r}{r}} \underbrace{\cos\left(\frac{\pi}{9}\right)}_{\frac{1}{r}} \underbrace{\cos\left(\frac{12\pi}{19}\right)}_{\frac{1}{r}} \quad (r) \quad -11$$

$$= 14 \left(\frac{r + \sqrt{r}}{r}\right) \times \frac{r}{r} \times \frac{1}{r} \times \frac{1}{r} = \frac{r(r + \sqrt{r})}{14} = \boxed{\frac{r + \sqrt{r}}{14}} \quad 10$$

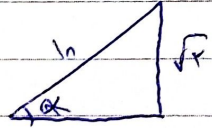
$$1 - \sin x = r + r \sin x \Rightarrow \sin x = -\frac{r}{r} \quad (r) \quad -11$$

$$\sin x = \frac{r \tan \frac{x}{2}}{1 + \tan^2 \frac{x}{2}} = -\frac{r}{r} \Rightarrow \tan \frac{x}{2} = -\frac{r}{r} - \tan^2 \frac{x}{2} \quad 15$$

$$\Rightarrow \tan^2 \frac{x}{2} + \tan \frac{x}{2} + \frac{r}{r} = 0 \Rightarrow \tan \frac{x}{2} < \boxed{-\frac{r}{r}} \quad \text{so here}$$

$$\frac{\sin^2 \theta + 1 - \cos^2 \theta}{(1 - \cos \theta)(\sin \theta)} = \frac{\sin^2 \theta + \sin^2 \theta + \cos^2 \theta - \cos^2 \theta}{(1 - \cos \theta)(\sin \theta)} = \frac{r \sin^2 \theta}{(1 - \cos \theta)(\sin \theta)} = \frac{r \sin \theta}{1 - \cos \theta} \quad (r) \quad -17$$

$$\Rightarrow \frac{r \sin \theta}{1 - \cos \theta} = k \frac{\cos \theta}{\sin \theta} \Rightarrow \frac{\sin \theta}{1 - \cos \theta} = \frac{\cos \theta}{\sin \theta} \Rightarrow \boxed{k = r} \quad 20$$



$$\cos \alpha = \frac{\sqrt{91}}{10}$$

$$\begin{aligned} \cos\left(\frac{11\pi}{9} + \alpha\right) &= \cos\left(\frac{11\pi}{9}\right) \cos \alpha - \sin\left(\frac{11\pi}{9}\right) \sin \alpha \\ &= \left(\frac{-\sqrt{r}}{r}\right) \times \left(-\frac{\sqrt{91}}{10}\right) - \left(\frac{\sqrt{r}}{10} \times \frac{\sqrt{r}}{r}\right) = \end{aligned} \quad (r) \quad -25$$

$$\frac{\sqrt{194}}{10} - \frac{r}{10} = \frac{1r}{10} = \boxed{\frac{r}{10}} \quad 30$$