

الف) $\lim_{x \rightarrow 2^+} f(x) - 3$

$f(2) - 3 = \Delta$ ✓

ب) $\lim_{x \rightarrow 2^-} f(x) - 3$

$f(2) - 3 = \Delta$ ✓

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الف) $\lim_{x \rightarrow 2^+} f[x] - 3$

$f[2^+] - 3 = f(2) - 3 = \Delta$ ✓

ب) $\lim_{x \rightarrow 2^-} f[x] - 3$

$f[2^-] - 3 = f(1) - 3 = 1$ ✓

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الف) $\lim_{x \rightarrow 2^+} [f(x) - 3]$

$[f(2^+) - 3] = [\Delta^+] = \Delta$ ✓

ب) $\lim_{x \rightarrow 2^-} [f(x) - 3]$

$[f(2^-) - 3] = [\Delta^-] = \Delta$ ✓

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الف) $[\lim_{x \rightarrow 2^+} f(x) - 3]$

$\lim_{x \rightarrow 2^+} f(x) - 3 = f(2) - 3 = \Delta$

$[\lim_{x \rightarrow 2^+} f(x) - 3] = [\Delta] = \Delta$ ✓

ب) $[\lim_{x \rightarrow 2^-} f(x) - 3]$

$\lim_{x \rightarrow 2^-} f(x) - 3 = f(2) - 3 = \Delta$

$[\lim_{x \rightarrow 2^-} f(x) - 3] = [\Delta] = \Delta$ ✓

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الف) $\lim_{x \rightarrow 2} \frac{f(x) - 3}{x - 2}$

$\lim_{x \rightarrow 2^+} \frac{9}{0^+} = +\infty$
 $\lim_{x \rightarrow 2^-} \frac{9}{0^-} = -\infty$ ✓

ب) $\lim_{x \rightarrow 2} \frac{f(x) - 3}{(x-2)^2}$

$\lim_{x \rightarrow 2^+} \frac{9}{(0^+)^2} = +\infty$
 $\lim_{x \rightarrow 2^-} \frac{9}{(0^-)^2} = +\infty$ ✓

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الف) $\lim_{x \rightarrow 3} \frac{\epsilon x - 3}{\sqrt{x-3}} \xrightarrow{3^+} \frac{9}{0^+} = +\infty$
 $\xrightarrow{3^-} \frac{9}{0^-} = -\infty$ صحيح

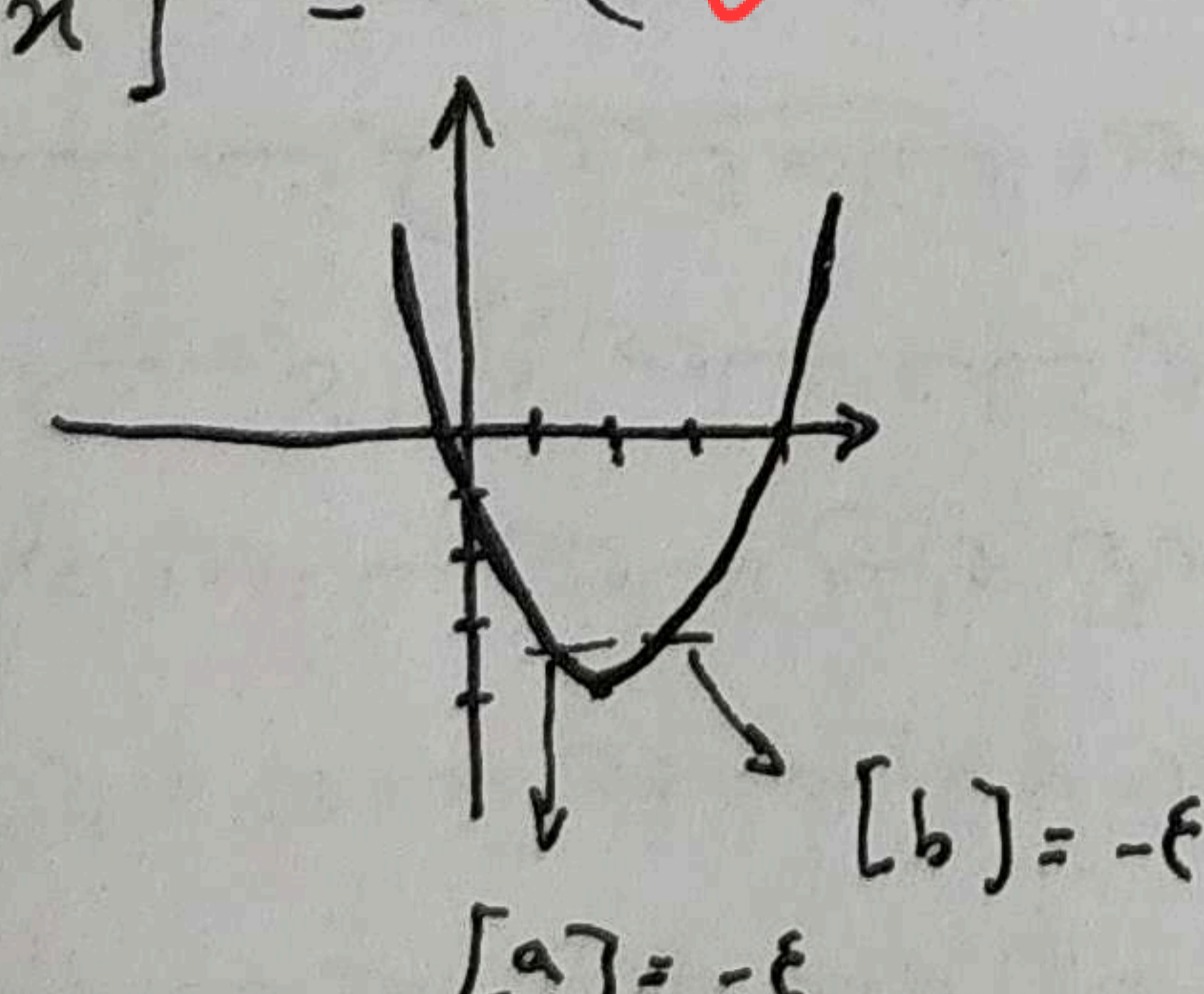
ب) $\lim_{x \rightarrow 3} \frac{\epsilon x - 3}{\sqrt{x^2 - \epsilon x + 3}} \xrightarrow{3^+} \frac{9}{0^+} = +\infty$
 $\xrightarrow{3^-} \frac{9}{0^-} = -\infty$ صحيح

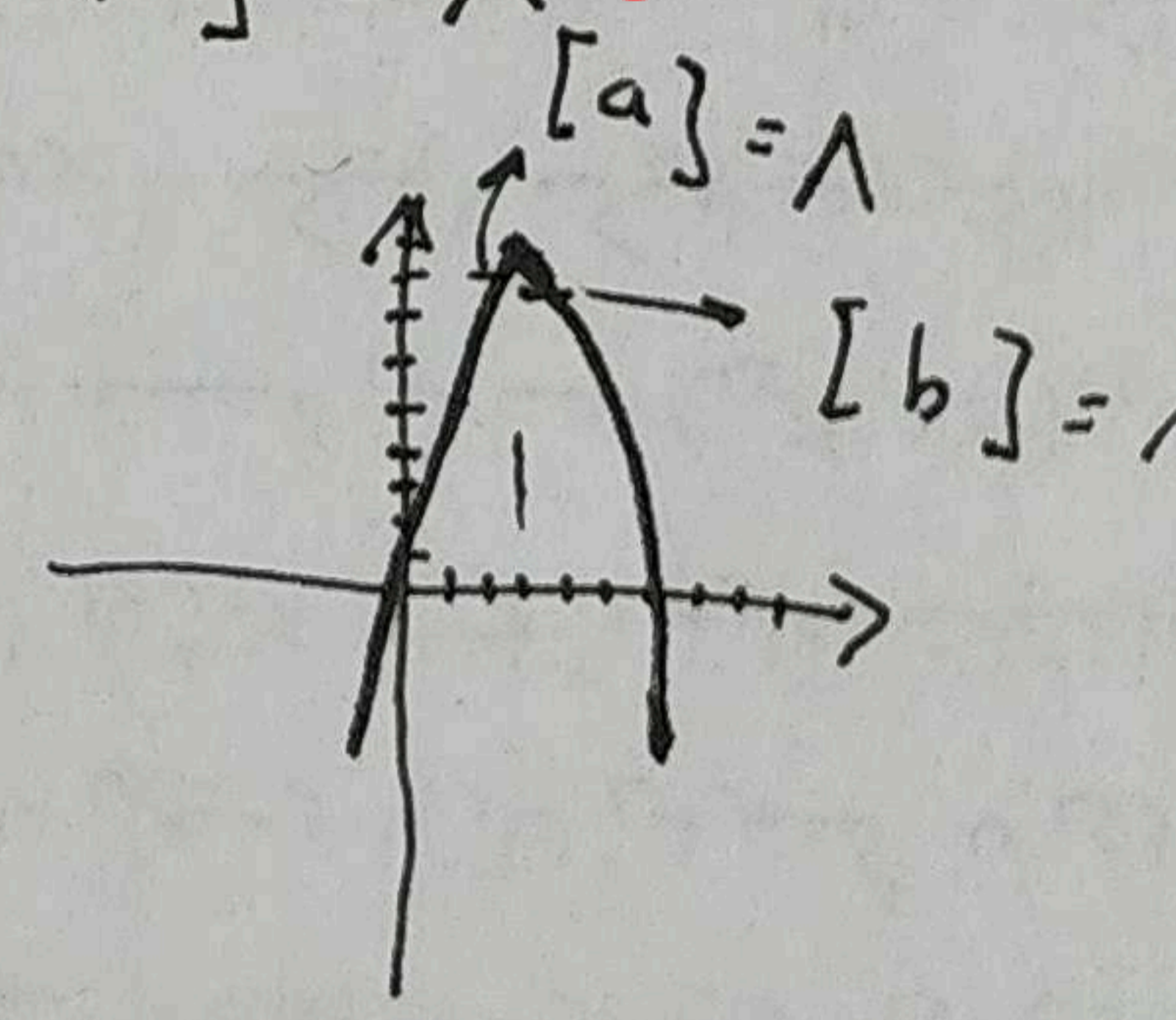
الف) $\lim_{x \rightarrow 3} \frac{\epsilon x - 3}{x^2 - \sqrt{x+1}} \xrightarrow{3^+} \frac{9}{0^-} = -\infty$
 $\xrightarrow{3^-} \frac{9}{0^+} = +\infty$ صحيح

ب) $\lim_{x \rightarrow 3} \frac{\epsilon x - 3}{[x-3]} \xrightarrow{3^+} \frac{9}{[0^+]} = \frac{9}{0}$
 $\xrightarrow{3^-} \frac{9}{[0^-]} = -9$ صحيح

الف) $\lim_{x \rightarrow 3} [3x] + [-2x] \xrightarrow{3^+} 9 + (-6) = 3$
 $\xrightarrow{3^-} 8 + (-6) = 2$ صحيح

ب) $[-\epsilon x] + [2x] \xrightarrow{-4^+} [23, 4] + [-11, 1] = 23 - 11 = 11$
 $\xrightarrow{-4^-} [24, 4] + [-12, 2] = 24 - 12 = 11$ صحيح

الف) $\lim_{x \rightarrow 2} [x^2 - \epsilon x] = -\epsilon$ صحيح
 $\min = \begin{vmatrix} 2 \\ -\epsilon \end{vmatrix}$


ب) $\lim_{x \rightarrow 3} [4x - x^2] = 1$ صحيح
 $\max = \begin{vmatrix} 3 \\ 9 \end{vmatrix}$


الف) $\lim_{x \rightarrow 2} \frac{|x-2|}{x^2 - 3x + 2} \xrightarrow{2^+} \frac{x-2}{(x-2)(x-1)} = \frac{1}{x-1}$
 $\xrightarrow{2^-} \frac{-(x-2)}{(x-2)(x-1)} = \frac{-1}{x-1}$
 $\xrightarrow{2^+} \frac{1}{1} = 1$ صحيح
 $\xrightarrow{2^-} \frac{-1}{-1} = 1$ صحيح

ب) $\lim_{x \rightarrow 1} \frac{x - [x]}{x^2 - 1} \xrightarrow{1^+} \frac{x-1}{(x-1)(x+1)} = \frac{1}{x+1}$
 $\xrightarrow{1^-} \frac{x}{(x-1)(x+1)} = \frac{1}{0^-} = -\infty$ صحيح