

$$\lim_{x \rightarrow 2} \frac{f(x)^{\mu} - \sqrt{x} + \nu}{(a x^{\mu} - 1)x + \mu} = \frac{0}{0} \xrightarrow{\text{رنگ لیلی}} \lim_{x \rightarrow 2} \frac{(f(x)^{\mu} - \nu)(x-1)}{(a x^{\mu} - \nu)(x-1)} = \frac{f - \nu}{a - \nu} = \boxed{\frac{1}{\mu}}$$

(۲) -۱

$$\lim_{x \rightarrow 0} \frac{|f(x)-1| - |f(x)+1|}{x} \begin{cases} + \frac{(-\nu x + 1) - (\nu x + 1)}{x} = \frac{-\nu x}{x} = -\nu \\ - \frac{(-\nu x + 1) - (\nu x + 1)}{x} = \frac{-\nu x}{x} = -\nu \end{cases}$$

(۲) -۲

$$\lim_{x \rightarrow f} \frac{x-f}{\sqrt{x}-\nu} = \frac{0}{0} \xrightarrow{\text{رنگ لیلی}} \lim_{x \rightarrow f} \frac{x-f}{\sqrt{x}-\nu} \times \frac{\sqrt{x}+\nu}{\sqrt{x}+\nu} = \frac{x\sqrt{x} + \nu x - f\sqrt{x} - \nu}{x-f} = \frac{\nu(x-f) + \sqrt{x}(x-f)}{x-f} = \frac{(x-f)(\nu + \sqrt{x})}{x-f} = \boxed{\nu}$$

(۲) -۳

$$\lim_{x \rightarrow \nu} \frac{x - \sqrt{\nu x}}{\nu x^{\mu} - x - \nu} = \frac{0}{0} \xrightarrow{\text{رنگ لیلی}} \lim_{x \rightarrow \nu} \frac{x - \sqrt{\nu x}}{(\nu x + \nu)(x - \nu)} \times \frac{x + \sqrt{\nu x}}{x + \sqrt{\nu x}} = \frac{x^{\mu} - \nu x}{(\nu x + \nu)(x - \nu)(x + \sqrt{\nu x})} = \frac{x(x - \nu)}{(\nu x + \nu)(x - \nu)(x + \sqrt{\nu x})} = \frac{x}{(\nu x + \nu)(x + \sqrt{\nu x})} = \frac{\nu}{\nu \times \nu} = \boxed{\frac{1}{\nu}}$$

(۲) -۴

$$\lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{\nu - \sqrt{a-x}} = \frac{0}{0} \xrightarrow{\text{رنگ لیلی}} \lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{\nu - \sqrt{a-x}} \times \frac{1 + \sqrt{x}}{1 + \sqrt{x}} \times \frac{\nu + \sqrt{a-x}}{\nu + \sqrt{a-x}} = \frac{(1-x)(\nu + \sqrt{a-x})}{(x-1)(1 + \sqrt{x})} = \frac{-\nu - \sqrt{a-x}}{1 + \sqrt{x}} = \frac{-\nu - \nu}{\nu} = \boxed{-2}$$

(۲) -۵

$$\lim_{x \rightarrow 1} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{3x+2} - 1} = \frac{0}{0} \xrightarrow{\text{ل'Hôpital}} \lim_{x \rightarrow 1} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{3x+2} - 1} \times \frac{\sqrt[3]{3x+2} + 1}{\sqrt[3]{3x+2} + 1} \times \frac{\sqrt[3]{(3x+2)^2} + \sqrt[3]{3x+2} + 1}{\sqrt[3]{(3x+2)^2} + \sqrt[3]{3x+2} + 1}$$

$$= \frac{3x+2 - 1}{3x+2 - 1} \times \frac{1}{1} = \frac{(3x-1) \times 3}{(3x-1) \times 3} = \frac{3}{3} = 1$$

$$\lim_{x \rightarrow 1} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{x} - 1} = \frac{0}{0} \xrightarrow{\text{ل'Hôpital}} \lim_{x \rightarrow 1} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{x} - 1} \times \frac{\sqrt[3]{x^2} + 1 + \sqrt[3]{x}}{\sqrt[3]{x^2} + 1 + \sqrt[3]{x}} \times \frac{\sqrt[3]{3x+2} + 1}{\sqrt[3]{3x+2} + 1} = \frac{3x+2 - 1}{x - 1} \times \frac{1}{1}$$

$$= \frac{3(x-1) + \sqrt[3]{x} - 1}{x-1} \times \frac{1}{1} = \frac{3(\sqrt[3]{x}-1)(\sqrt[3]{x}+1) + (\sqrt[3]{x}-1)}{(\sqrt[3]{x}-1)(\sqrt[3]{x}+1)} \times \frac{1}{1} = \frac{(\sqrt[3]{x}-1)(3(\sqrt[3]{x}+1) + 1)}{(\sqrt[3]{x}-1)(\sqrt[3]{x}+1)} \times \frac{1}{1} = \frac{1}{1} = 1$$

$$\lim_{x \rightarrow \pi} \frac{1 + \cos^2 x}{\sin^2 x} = \frac{0}{0} \xrightarrow{\text{ل'Hôpital}} \frac{(1 + \cos^2 x)(1 + \cos^2 x - \cos^2 x)}{(1 + \cos^2 x)(1 - \cos^2 x)} = \frac{1 + \cos^2 x - \cos^2 x}{1 - \cos^2 x} = \frac{1 - (-1) + (-1)^2}{1}$$

$$= \frac{1}{1} = 1$$

$$\lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \tan x}{\sin x - \cos x} = \frac{0}{0} \xrightarrow{\text{ل'Hôpital}} \frac{1 - \frac{\sin x}{\cos x}}{-(\cos x - \sin x)} = \frac{\cos x - \sin x}{\cos x} = \frac{1 - \cos x}{\cos x} = \frac{1}{\cos x} = \frac{1}{\frac{\sqrt{2}}{2}} = \sqrt{2}$$

$$\lim_{x \rightarrow \frac{\pi}{4}} \frac{\tan^2 x - 1}{\cos^2 x} = \frac{0}{0} \xrightarrow{\text{ل'Hôpital}} \frac{\frac{\sin^2 x}{\cos^2 x} - 1}{\cos^2 x} = \frac{(\cos^2 x)}{\cos^2 x} = -\frac{1}{\cos^2 x} = -\frac{1}{(\frac{\sqrt{2}}{2})^2} = -\frac{1}{\frac{1}{2}} = -2$$