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$$\lim_{x \rightarrow 2} \frac{f(x)^p - \sqrt{p} + p}{(2x)^p - 1 + p} = \frac{0}{0} \xrightarrow{\text{رنگ لایه}} \lim_{x \rightarrow 2} \frac{(f(x)-\sqrt{p})(x-1)}{(2x-1)(x-1)} = \frac{f-\sqrt{p}}{2-1} = \boxed{\frac{1}{2}}$$

$$\lim_{x \rightarrow 0} \frac{|1^p x - 1| - |1^p x + 1|}{x} \begin{cases} + \frac{(-1^p x + 1) - (1^p x + 1)}{x} = \frac{-2x}{x} = \boxed{-2} \\ - \frac{(-1^p x + 1) - (1^p x + 1)}{x} = \frac{-2x}{x} = \boxed{-2} \end{cases}$$

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$$\lim_{x \rightarrow f} \frac{x-f}{\sqrt{x}-f} = \frac{0}{0} \xrightarrow{\text{رنگ لایه}} \lim_{x \rightarrow f} \frac{x-f}{\sqrt{x}-f} \times \frac{\sqrt{x}+f}{\sqrt{x}+f} = \frac{x\sqrt{x} + fx - f\sqrt{x} - f}{x-f} = \frac{f(x-f) + \sqrt{x}(x-f)}{x-f} = \frac{(x-f)(1+\sqrt{x})}{x-f} = \boxed{1}$$

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$$\lim_{x \rightarrow p} \frac{x - \sqrt{px}}{p^2 x^p - x - y} = \frac{0}{0} \xrightarrow{\text{رنگ لایه}} \lim_{x \rightarrow p} \frac{x - \sqrt{px}}{(p^2 x^p - x - y)(x-p)} \times \frac{x + \sqrt{px}}{x + \sqrt{px}} = \frac{x^2 - px}{(p^2 x^p - x - y)(x-p)(x + \sqrt{px})} = \frac{x(x-p)}{(p^2 x^p - x - y)(x-p)(x + \sqrt{px})} = \frac{x}{(p^2 x^p - x - y)(x + \sqrt{px})} = \frac{p}{p \times p} = \boxed{\frac{1}{p}}$$

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$$\lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{x - \sqrt{a-x}} = \frac{0}{0} \xrightarrow{\text{رنگ لایه}} \lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{x - \sqrt{a-x}} \times \frac{1 + \sqrt{x}}{1 + \sqrt{x}} \times \frac{1 + \sqrt{a-x}}{1 + \sqrt{a-x}} = \frac{(1-x)(1+\sqrt{a-x})}{(x-1)(1+\sqrt{x})} = \frac{-1 - \sqrt{a-x}}{1 + \sqrt{x}} = \frac{-1-1}{2} = \boxed{-1}$$

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$$\lim_{x \rightarrow f} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{3x+2} - 1} = \frac{0}{0} \xrightarrow{\text{رابطه}} \lim_{x \rightarrow f} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{3x+2} - 1} \times \frac{\sqrt[3]{3x+2} + 1}{\sqrt[3]{3x+2} + 1} \times \frac{\sqrt[3]{(3x+2)^2} + \sqrt[3]{3x+2} + 1}{\sqrt[3]{(3x+2)^2} + \sqrt[3]{3x+2} + 1}$$

$$= \frac{3x+2 - 1}{3x+2 - 1} \times \frac{1}{1} = \frac{(3x-1) \times 3}{(3x-1) \times 3} = \frac{3(x-1) \times 3}{3(x-1) \times 3} = \boxed{\frac{1}{1}}$$

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$$\lim_{x \rightarrow 1} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{x} - 1} = \frac{0}{0} \xrightarrow{\text{رابطه}} \lim_{x \rightarrow 1} \frac{\sqrt[3]{3x+2} - 1}{\sqrt[3]{x} - 1} \times \frac{\sqrt[3]{x^2} + 1 + \sqrt[3]{x}}{\sqrt[3]{x^2} + 1 + \sqrt[3]{x}} \times \frac{\sqrt[3]{(3x+2)^2} + \sqrt[3]{3x+2} + 1}{\sqrt[3]{(3x+2)^2} + \sqrt[3]{3x+2} + 1} = \frac{3x+2-1}{x-1} \times \frac{1}{1}$$

$$= \frac{3(x-1) + \sqrt{3} - 1}{x-1} \times \frac{1}{1} = \frac{3(\sqrt{3}-1) + (\sqrt{3}-1) + (\sqrt{3}-1)}{(\sqrt{3}-1)(\sqrt{3}+1)} \times \frac{1}{1} = \frac{(\sqrt{3}-1)(3(\sqrt{3}+1) + 1)}{(\sqrt{3}-1)(\sqrt{3}+1)} \times \frac{1}{1} = \frac{3}{1} \times \frac{1}{1} = \boxed{\frac{3}{1}}$$

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$$\lim_{x \rightarrow \pi} \frac{1 + \cos^3 x}{\sin^3 x} = \frac{0}{0} \xrightarrow{\text{رابطه}} \frac{(1 + \cos x)(1 + \cos^2 x - \cos x)}{(1 + \cos x)(1 - \cos x)} = \frac{1 + \cos^2 x - \cos x}{1 - \cos x} = \frac{1 - (-1) + (-1)^2}{1}$$

$$= \boxed{\frac{3}{1}}$$

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$$\lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \tan x}{\sin x - \cos x} = \frac{0}{0} \xrightarrow{\text{رابطه}} \frac{1 - \frac{\sin x}{\cos x}}{\sin x - \cos x} = \frac{\frac{\cos x - \sin x}{\cos x}}{-(\cos x - \sin x)} = \frac{1}{-\cos x} = -\frac{1}{\frac{\sqrt{2}}{2}} = \boxed{-\sqrt{2}}$$

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$$\lim_{x \rightarrow \frac{\pi}{4}} \frac{\tan^3 x - 1}{\cos^3 x} = \frac{0}{0} \xrightarrow{\text{رابطه}} \frac{\frac{\sin^3 x}{\cos^3 x} - 1}{\cos^3 x} = \frac{-(\cos^3 x)}{\cos^3 x} = -\frac{1}{\cos^3 x} = -\frac{1}{(\frac{\sqrt{2}}{2})^3} = -\frac{1}{\frac{\sqrt{2}}{2}} = \boxed{-\sqrt{2}}$$