

$$-\sqrt{a^2+b^2} \leq a \cos n + b \sin n \leq \sqrt{a^2+b^2}$$

الف) $-\sqrt{r^2} \leq r \sin n + r \cos n \leq \sqrt{r^2} \quad [-\sqrt{r^2}, \sqrt{r^2}] \checkmark$

ب) $-8 \leq 8 \sin n - 8 \cos n \leq 8 \quad [-8, 8] \checkmark$

ج) $-\sqrt{r^2} \leq \dots \leq \sqrt{r^2} \xrightarrow{[]} \{-4, -3, -2, -1, 0, 1, 2, 3, 4\} \checkmark$

د) $\cos n - 2 \sin n \xrightarrow{[]} [-\sqrt{5}, \sqrt{5}] \xrightarrow{[]} [0, \sqrt{5}] \checkmark$

الف) $\sin^2 n + r \sin n + r$ $\sin n \begin{cases} +1 \rightarrow y \\ -1 \rightarrow 0 \\ -\frac{b}{2a} \end{cases} [0, 4] \checkmark$

ب) $r \sin^2 n + r \sin n + r$ $\sin n \begin{cases} +1 \rightarrow y \\ -1 \rightarrow 1 \\ -\frac{b}{2a} \end{cases} [\frac{r}{4}, y] \checkmark$

الف) $\sin^2 n + \cos^2 n = 1 \Rightarrow y = 1 + r \cos^2 n$ $0 \leq \cos^2 n \leq 1$ $R_f = [1, 4] \checkmark$

ب) $\frac{r \cot n}{1 + \cot n} = r \frac{\cos n}{\sin n} \times \sin^2 n = r \sin n \cos n = \sin 2n$ $[-1, 1] \checkmark$

$$\frac{1-k}{r} \leq \sin^k n + \cos^k n \leq 1$$

الف) $r^{-k} \leq \dots \leq 1 \quad [\frac{1}{r^k}, 1] \checkmark$

ب) $r^{-k} \leq \dots \leq 1 \xrightarrow{[]} [0, 1] \checkmark$

الف) $y = \frac{(n+4)(n-1)}{(n+4)} = n-1 \leq y$ $n = \frac{y+1}{r} \rightarrow (\mathbb{R}) - \{-9\} \checkmark$

$n+4 \neq 0$
 $\frac{n+4}{r} \neq -9 \Rightarrow y \neq -9$

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ب) $y = \frac{(n+1)(n+1)}{(n+1)} = n+1 \leq y$ $\frac{b}{2a} = -\frac{1}{r}$ $y = \frac{r}{4}$ $R_f = [\frac{r}{4}, +\infty) \checkmark$

$D = \mathbb{R} - \{-1\}$ $f_{(-1)} = f_{(-2)} = 3$

چون شصتی است 3 پس 3 حذف کنی!