

$$g = \{(-1, 2), (0, 1), (2, 0), (1, 4)\}$$

$$D_f = [-1, 1]$$

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$$g - f \rightarrow \begin{cases} (-1, 2) - (-1, 0) \Rightarrow (-1, 2) \\ (0, 1) - (0, 2) \Rightarrow (0, -1) \\ (1, 4) - (1, 0) \Rightarrow (1, 4) \end{cases} \quad R_f = \{2, 4, \omega\}$$

$$2 + 4 + \omega = 11$$

$$f(x) = 2x - 1$$

$$\min x = 3 \Rightarrow \min y = \omega \Rightarrow R_f [\omega, +\infty)$$

$$g(x) = \frac{1}{3}x + 3$$

$$\max x = 3 \Rightarrow \max y = 4 \Rightarrow R_f (-\infty, 4]$$

$$\bigcup (-\infty, 4] \cup [\omega, +\infty)$$

$$\frac{-x^2}{2} + x + 3 > \frac{3}{2} \xrightarrow{x^2} -x^2 + 2x + 6 > 3$$

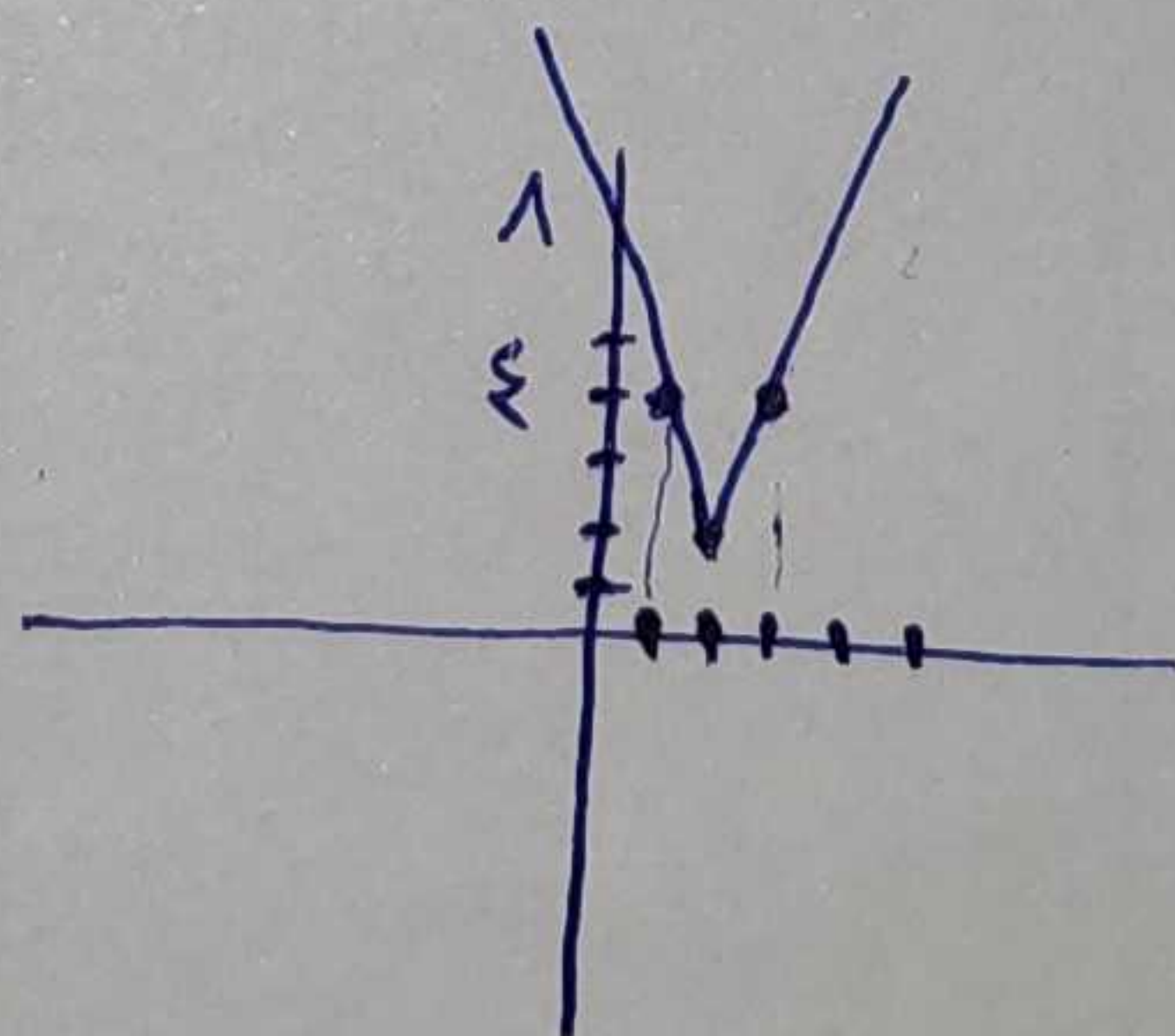
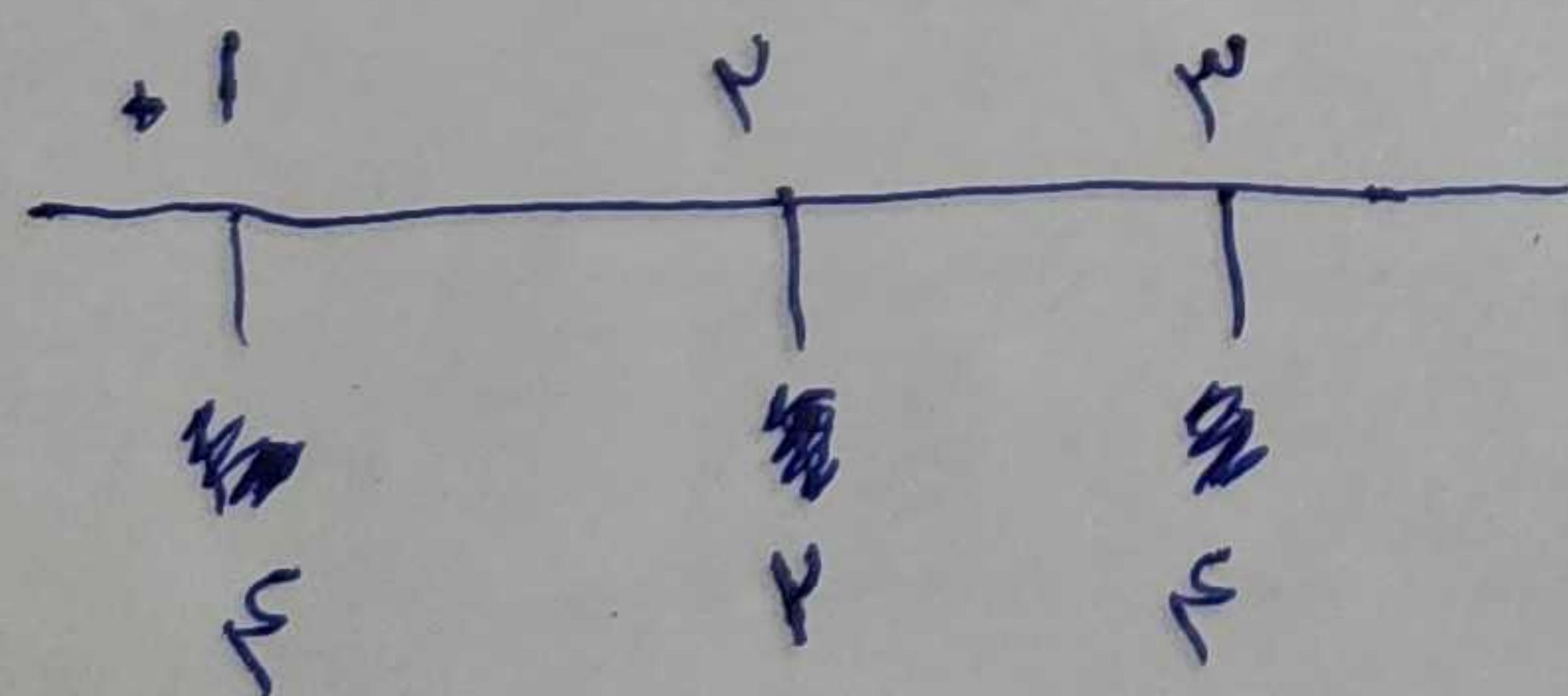
$$x^2 - 2x - 3 < 0$$

$$(x-3)(x+1)$$

$$\frac{-1}{3} \quad \frac{3}{-1} \quad R_f = (-1, 3)$$

$$\sqrt{b-a} = \sqrt{3-(-1)} = 2$$

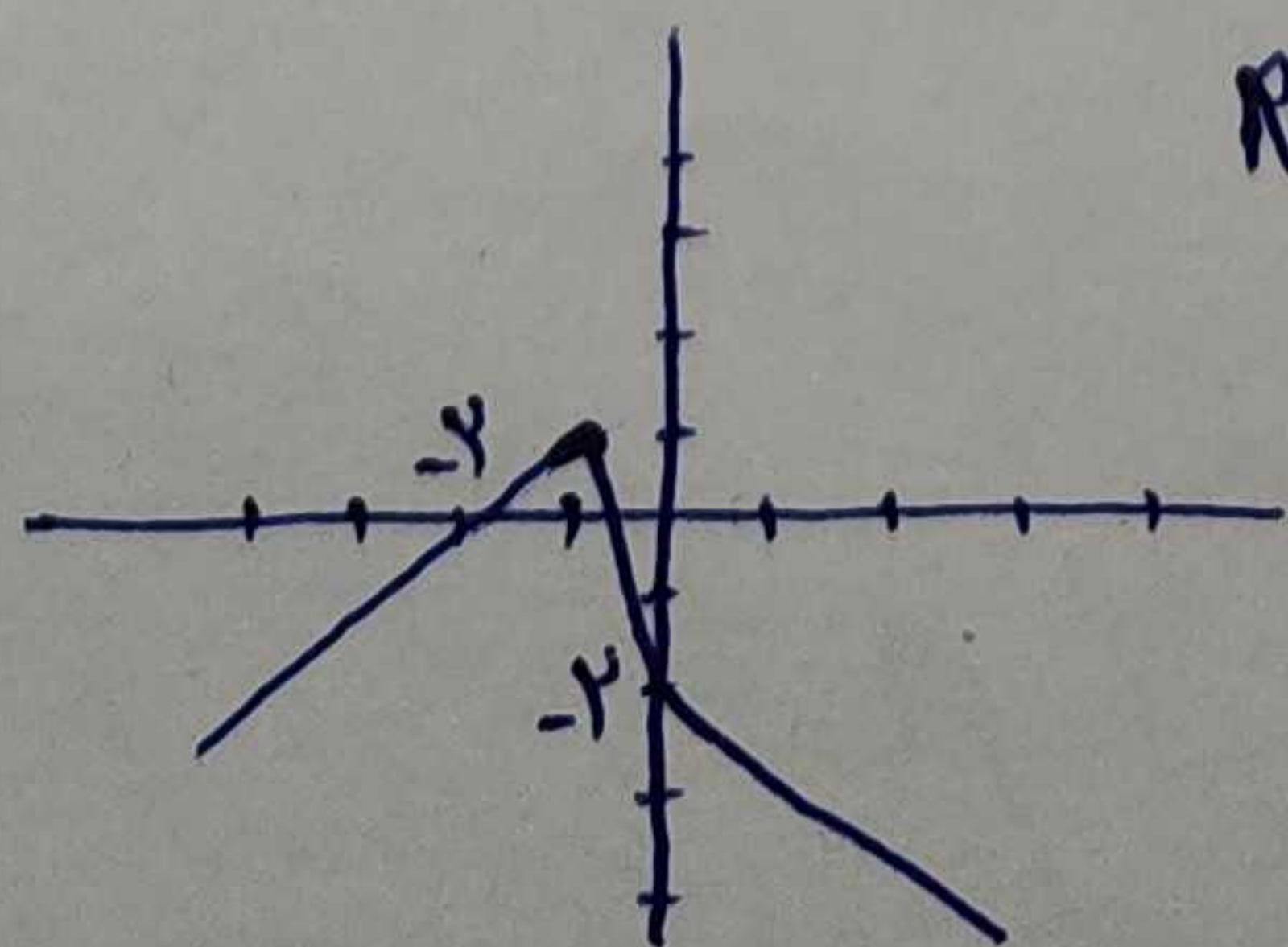
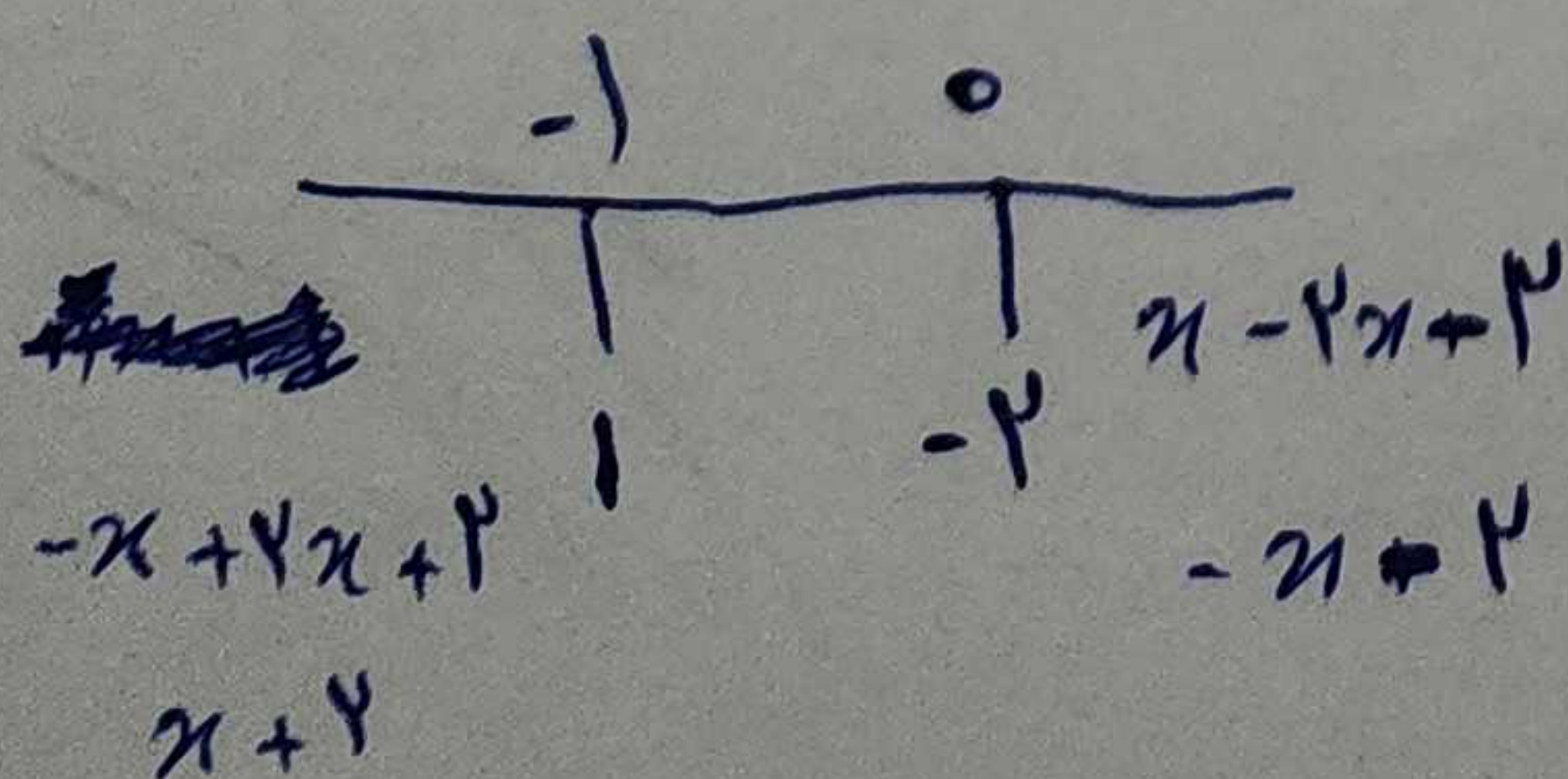
$$|x+1| + |x-3| + |2x-4|$$



$$R = [2, +\infty)$$

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$$|x| - 2|x+1|$$



$$R_f = (-\infty, 1]$$

$$y = \frac{x^2 + \omega x + m}{x+1}$$

$$y(x+y) = x^2 + \omega x + m$$

$$x^2 + x(\omega - y) - y + m = 0$$

$$x = \frac{-(\omega - y) \pm \sqrt{(\omega - y)^2 - 4(-y + m)}}{2}$$

$$\sqrt{y^2 - 4\omega y + 4y + 4m} \leq 0$$

$$y^2 - 4\omega y + 4y + 4m \geq 0$$

$$-4\omega + 4y + 4m \leq 0$$

$$m \leq \omega$$

$$1 \leq y \leq 3 \text{ or } 1 \leq \omega \leq 3$$

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$$x \geq 3 \Rightarrow x+3 \quad [\omega + \infty)$$

$$0 \leq x < 3 \Rightarrow x^2 - 2x + 3 \quad [1, \omega) \xrightarrow{u} [1, +\infty) = \mathbb{R}$$

$$x < 0 \Rightarrow |x| + 3 \rightarrow (3 + \infty)$$

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$$x \leq 0 \Rightarrow x^2 + 5x + 3$$

$$x > 0 \Rightarrow [2x] - 2x$$

$$\textcircled{1} \frac{-b}{2a} = -1 \Rightarrow \min x \Rightarrow \min y = -1 \quad [-1 + \infty)$$

$$-1 < [x] - x \leq 0 \quad (-1, 0] \xrightarrow{u} [-1 + \infty)$$

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$$\max R_f \Rightarrow a+1 - \sqrt{2x+3} = \omega$$

$$\sqrt{2x+3} = 0 \Rightarrow a+1 = \omega \Rightarrow a = \omega$$

$$R_{f \min} = \omega - \sqrt{2x+3}$$

$$2x+3=0 \Rightarrow x = -\frac{3}{2} \quad b = \frac{3}{2}$$

$$ab = \omega \times \frac{3}{2} = -9$$

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$$f(0) = 4$$

$$4 + g(0) = 4$$

$$g(0) = 0$$

$$F(1) = 2\sqrt{2}$$

$$2\sqrt{2} + g(1) = 3\sqrt{2}$$

$$g(1) = \sqrt{2}$$

$$f(-1) = 6\sqrt{2}$$

$$6\sqrt{2} + g(-1) = 3\sqrt{2}$$

$$g(-1) = -\sqrt{2}$$

$$R \frac{f(x)}{4} - \frac{g(x)}{\sqrt{2}} = [0, \sqrt{2}]$$

$$\frac{6\sqrt{2}}{4} + \frac{\sqrt{2}}{\sqrt{2}} = \sqrt{2} \quad \max$$

$$\frac{4}{4} - 1 = 0$$

$$\frac{2\sqrt{2}}{4} - \frac{\sqrt{2}}{\sqrt{2}} = 0$$

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