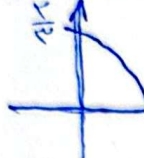
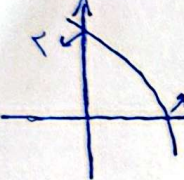
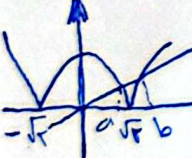


$y_2 = 1 - \log_c (2a-b) \rightarrow 1 - \log_c^{-b} = r \rightarrow \log_c^{-b} = 1-r \rightarrow \frac{1}{c^{-b}} = 1-r \rightarrow c^b = \frac{1}{1-r} \rightarrow b = \log_c \frac{1}{1-r} \quad (1)$
 $b + c = \frac{r}{c} \Rightarrow -\frac{1}{c} + c = \frac{r}{c} \Rightarrow -1 + c^2 = r \Rightarrow c^2 - \frac{r}{c} - 1 = 0$
 $\Rightarrow c^2 - r = 0 \Rightarrow c = \sqrt{r}$
 $\Rightarrow -b = \frac{1}{\sqrt{r}} \Rightarrow \boxed{b = -\frac{1}{\sqrt{r}}}$


 $f(x) = 1 + c \times r^x = \frac{r}{x} \Rightarrow c \times r^x = \frac{r}{x} - 1$
 $f(1) = 1 + c \times r^{a+b} = 0 \Rightarrow 1 + c \times r^a \times r^b = 0 \Rightarrow r^b = -\frac{1}{r^a} \Rightarrow \boxed{b = -1}$
 $\rightarrow f(-1) = ? \Rightarrow 1 + c \times r^{a-1} = 1 + c \times r^a \times r^{-1} = 1 + \frac{1}{r} \times \frac{1}{r} = 1 + \frac{1}{r^2} = \boxed{\frac{r^2 + 1}{r^2}}$


 $r = c + \log_a b \Rightarrow \log_a (r, ta+b) - \log_a b = -r$
 $0 = c + \log_a (r, ta+b)$
 $\hookrightarrow \log_a \frac{r, ta+b}{b} = -r \Rightarrow \frac{r, ta+b}{b} = \frac{1}{r^r} \Rightarrow \frac{r, ta}{b} = -\frac{r}{r^r} \Rightarrow \frac{a}{b} = -\frac{r}{r^r}$
 $\Rightarrow \frac{a}{b} = ? = -\frac{r}{r^r} = \boxed{-\frac{1}{r^{r-1}}}$

$f(x) = \log_f (|a^x - r| - a)$
 $a^x - r = a \Rightarrow a^x - a + r = 0 \Rightarrow a^x = a - r \Rightarrow a < a - r \Rightarrow b = r$
 $-a^x + r = a \Rightarrow a^x + a - r = 0 \Rightarrow a^x = r - a \Rightarrow a = 1 \Rightarrow a = 1$
 $\hookrightarrow (-\infty, 1) \cup (r, +\infty)$


 $\Rightarrow (-\infty, a) \cup (b, +\infty) \Rightarrow a = 0 < a < \sqrt{r}, b > \sqrt{r}$

$f(x) = r + r^{b-ax} \Rightarrow f(1) = g(1) \Rightarrow r + r^{b-a} = r \Rightarrow r^{b-a} = 0 \Rightarrow b-a = 1 \quad (5)$

$g(x) = -2^x - 3x + 1$

$f^{-1}(1) = -1 \Rightarrow f(-1) = 1 = r + r^{b+a} = 1 \Rightarrow r^{b+a} = 0 \Rightarrow b+a = 1$

$r \cdot f(r) - 1 = \boxed{r^2}$

$\Rightarrow \begin{cases} b+a = 1 \\ b-a = 1 \end{cases} \Rightarrow \begin{cases} b = 1 \\ a = 0 \end{cases}$

(6)

$$f(x) = -x + \left(\frac{1}{x}\right)^{Ax+B}$$

$$y = a^x - a \Rightarrow y = a^x - a \xrightarrow{A=1} y = a \rightarrow A(1,0)$$

$$f(x) = ? \quad y = a^x - a \xrightarrow{A=2} y = a^2 \Rightarrow B(2,2)$$

$$\Rightarrow -x + \frac{1}{x} A + B = 0 \Rightarrow A + B = -1$$

$$-x + \frac{1}{x} 2A + B = 2 \Rightarrow 2A + B = -x$$

$$\Rightarrow A = -1, B = 0$$

(7)

$$m(t) = m\left(\frac{1}{9}\right)^t = \frac{1}{9} m = \left(\frac{1}{9}\right)^t = \frac{1}{9} \Rightarrow \frac{1}{9} \times 9 = 1 \text{ min}$$

$$\Rightarrow \log_a \left(\frac{1}{9}\right)^t = \log_a \frac{1}{9} \Rightarrow t \log_a \left(\frac{1}{9}\right) = -\log_a 9$$

$$\log_a 9 = \frac{14}{11} = \frac{V}{\Delta} \rightarrow \log_a 9 = \frac{V}{\Delta} \Rightarrow t \log_a \left(\frac{1}{9}\right) = -\log_a 9 \rightarrow t(\log_a 1 - \log_a 9) = -(\log_a 9 + \log_a 9)$$

$$\log_a \frac{1}{9} = \frac{-t}{11} = \frac{-V}{\Delta} \rightarrow \log_a 9 = \frac{V}{\Delta} \Rightarrow t \left(\frac{-V - t}{11}\right) = -\left(\frac{V + V}{11}\right) \Rightarrow t = \frac{19}{2}$$

(8)

$$m(t) = m\left(\frac{V}{\lambda}\right)^{\frac{t}{V}} \Rightarrow \frac{1}{V} m \Rightarrow m\left(\frac{V}{\lambda}\right)^{\frac{t}{V}} = \left(\frac{V}{\lambda}\right)^{\frac{t}{V}} = \frac{1}{V}$$

$$\log \left(\frac{V}{\lambda}\right)^{\frac{t}{V}} = \log \left(\frac{1}{V}\right) = \frac{t}{V} \log \frac{V}{\lambda} \Rightarrow \frac{t}{V} (\log V - \log \lambda) = -\log V$$

$$\log V = 0.14 = \log \frac{V}{\lambda} = \frac{\Delta}{\lambda}$$

$$\log \lambda = 1.4 = \log \frac{\lambda}{V} = \frac{\Delta}{\lambda} \Rightarrow \frac{t}{V} (\log V - 3 \log \lambda) = -\log V$$

$$\Rightarrow \frac{t}{V} \left(-\frac{\Delta}{\lambda}\right) = -\frac{\Delta}{\lambda} \Rightarrow \frac{t}{\Delta \lambda} = 1 \Rightarrow \boxed{t = \Delta \lambda}$$

(9)

$$f(t) = A \left(\frac{99}{100}\right)^t = \frac{A}{100} \Rightarrow \left(\frac{99}{100}\right)^t = \frac{1}{100}$$

$$\Rightarrow \log \left(\frac{99}{100}\right)^t = \log \frac{1}{100} \Rightarrow t (\log 99 - \log 100) = -\log 100 \Rightarrow \log 99 + \log 99 - 2 = -\log 100$$

$$\rightarrow \log 99 + \log 99 - 2 = -\log 100$$

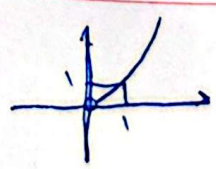
$$\rightarrow t (\log 99 + \log 99 - 2) = -\log 100 \Rightarrow 0.02t = -0.158 \Rightarrow \boxed{t = 7.9}$$

(10)

$$a) y = a \cdot \log a^x$$

$$\hookrightarrow a \cdot \log a^x = \boxed{a^2}$$

$$\Rightarrow (0, +\infty)$$



$$b) y = \log a^x$$

$$y = x \log a$$

$$D = \mathbb{R} - \{0\}$$

