

۱	$\begin{aligned} x=0 &\rightarrow y=r \Rightarrow \log_c (a(x)-b) = -1 \rightarrow c^{-1} = -b \rightarrow b + \frac{1}{c} = 0 \\ &\qquad\qquad\qquad \left. \begin{aligned} b+c &= \frac{1}{c} \\ b-r &= \frac{1}{c} \end{aligned} \right\} c = \frac{1}{b+r} \\ x=1 &\rightarrow y=0 \Rightarrow \log_{\frac{1}{c}} (c^{\frac{1}{c}} a + r) = 1 \\ &\rightarrow r - \frac{1}{c} a = \frac{1}{c} \rightarrow a = 1 \quad (a+c)b = \frac{1}{c} \times (-r) = -\frac{r}{c} \end{aligned}$
۲	$\begin{aligned} x=0 &\rightarrow y = \frac{1}{c} \Rightarrow 1 + c \times r^{a+b} = \frac{1}{c} \rightarrow c \times r^0 = -\frac{1}{c} \\ x=1 &\rightarrow y=0 \Rightarrow c \times r^{a+b} = -1 \quad \frac{r^a}{r^{a+b}} = \frac{1}{r} \rightarrow b = 1 \\ f(-1) &= 1 + r^{a-b} = 1 + \frac{1}{c} = \frac{1}{c} \quad \frac{c \times r^{a-b}}{c \times r^{a-b}} = \frac{1}{\frac{1}{c}} = c-1 \end{aligned}$
۳	$\begin{aligned} x=0 &\rightarrow y \leq r \rightarrow \log_a^b + c = r \rightarrow \log_a^b - r = -c \rightarrow \log_a^{\frac{b}{c}} = c \\ x=r &\rightarrow y=0 \rightarrow \log_a^{r+a+b} = c \Rightarrow r+a+b = \frac{1}{c} \rightarrow r + \frac{a}{b} + 1 = \frac{1}{c} \\ &\rightarrow \frac{a}{b} = \frac{1}{c} - 1 \end{aligned}$
۴	$\begin{aligned} a^r - r - x > 0 &\Rightarrow (a^r - r) > x \rightarrow a^r - r > x \text{ و } a^r - r < -x \\ a^r - a - r > 0 &\Rightarrow D = (-\infty, -1) \cup (r, +\infty) \\ a^r + a - r < 0 &\Rightarrow D = (-r, 1) \end{aligned} \quad \left. \begin{aligned} & \\ & \end{aligned} \right\} \cup \rightarrow D_f = \mathbb{R} - [1, r]$
۵	$\begin{aligned} x=1 &\rightarrow y = r \Rightarrow r + r^{b-a} = r \rightarrow r^{b-a} = r \rightarrow b-a = 1 \\ x=1 &\rightarrow y=0 \Rightarrow r + r^{b+a} = 1 \rightarrow r^{b+a} = 1 - r \rightarrow b+a = r \end{aligned} \quad \left. \begin{aligned} & \\ & \end{aligned} \right\} \begin{aligned} b &= r \\ a &= 1 \end{aligned}$

$$\begin{aligned}
 x^1 &\rightarrow y=0 \Rightarrow \left(\frac{1}{r}\right)^{A+B} \leq r \rightarrow A+B=-1 \\
 x^r &\rightarrow y=r \Rightarrow \left(\frac{1}{r}\right)^{rA+B} \leq r \rightarrow rA+B=-r \quad \left. \vphantom{\begin{aligned} x^1 \\ x^r \end{aligned}} \right\} A=-1, B=0
 \end{aligned}$$

$$f(r) = -r + \left(\frac{1}{r}\right)^{-r} = -r + \Delta = r$$

$$\begin{aligned}
 \Delta^r &= \frac{1}{r} \rightarrow \log \frac{1}{r} = \log \frac{1}{\Delta} = -\log \Delta \\
 &= \frac{0 - \log \Delta + \log \Delta}{r \log \Delta} = -\left(\frac{1}{r\Delta} + \frac{1}{r\Delta}\right) = \frac{r \times \frac{1}{r\Delta} - r \times \frac{1}{r\Delta}}{r\Delta} = \frac{r(\Delta - \Delta)}{r\Delta} = 0
 \end{aligned}$$

$$\begin{aligned}
 \frac{V}{A} &= \frac{1}{V} \rightarrow \log \frac{1}{V} = \log \frac{1}{A} = -\log A \\
 &= \frac{0 - \log A + \log A}{\frac{1}{V} \log A} = \frac{r \times \frac{1}{r\Delta} - r \times \frac{1}{r\Delta}}{\frac{1}{r\Delta}} = \frac{r(\Delta - \Delta)}{\frac{1}{r\Delta}} = 0
 \end{aligned}$$

$$\begin{aligned}
 \frac{qY}{100} &\leq \frac{1}{r} \rightarrow \log \frac{qY}{100} \leq \log \frac{1}{r} = -\log r \\
 &= \frac{0 - \log r + \log q}{\log \frac{qY}{100}} \leq \frac{\log q - \log r}{\log \frac{qY}{100}} \\
 &= \frac{0 - \log r + \log q}{\log \frac{qY}{100}} \leq \frac{0 - \log r + \log q}{\log \frac{qY}{100}} \\
 &= \frac{0 - \log r + \log q}{\log \frac{qY}{100}} \leq \frac{0 - \log r + \log q}{\log \frac{qY}{100}}
 \end{aligned}$$

$$q \log r^x = q \log r^y = q \log r^z$$

$$y = \log r^x, \log r^y, \log r^z$$

