

$S_{\square} = ab \sin \alpha$
 ارتفاع زاویه بین

هرتا د زاویه میان دو ضلع متوازی ارتفاع با هم برابر است

$S_{\square} = \frac{1}{2} \times 2x \times x \sin \alpha = x^2 \sin \alpha$
 $S_{\square} = \frac{1}{2} \times x^2 \times 2 \Rightarrow x^2 = 1 \Rightarrow x = \sqrt{1} = 1$

ارتفاع را بصورت $\frac{ax}{2} \sin \alpha$ $\frac{ax}{2} \times 2 = ax$ $\frac{ax}{2} \times 2 = ax$
 $\alpha = 1 \Rightarrow \sin \alpha = \frac{1}{2}$
 زاویه متوازی ارتفاع $\frac{ax}{2} \times 2 = ax$

$S_{ABC} = \frac{1}{2} AB \times AC \times \sin \hat{A} = \frac{r \times d}{2} \times \sin \hat{A}$ $\tan \hat{A} = \frac{\sqrt{10}}{3}$

$S_{ADE} = \frac{1}{2} \times AD \times AE \times \sin \hat{A} = 1 \times \sin \hat{A}$ $S_{ABC} = S_{ADE}$

$\frac{r \times d}{2} \sin \hat{A} = \frac{r \times 1}{2} \sin \hat{A} \Rightarrow \frac{r \times d}{2} \sin \hat{A} = \frac{r \times 1}{2} \sin \hat{A} \Rightarrow \frac{d}{2} = \frac{1}{2} \Rightarrow d = 1$
 $\tan \hat{A} = \frac{\sqrt{10}}{3} \Rightarrow \hat{A} = 30^\circ$

$\frac{1 + \sin \alpha}{\cos \alpha} = \frac{1}{\sqrt{\cos \alpha}} - \tan \alpha \rightarrow \frac{1 + \sin \alpha}{\cos \alpha} = \frac{1}{\cos \alpha} - \tan \alpha \rightarrow \frac{\sin \alpha}{\cos \alpha} = -\tan \alpha$
 $\frac{|\sin \alpha|}{\cos \alpha} = -\frac{1}{\cos \alpha} \Rightarrow -\tan \alpha \rightarrow 0 > \sin$

اگر $\frac{\pi}{2} < \alpha < \frac{3\pi}{2}$ \sin منفی α در ناحیه سوم قرار دارد

$\tan(\frac{\pi}{2} - \alpha) = \cot(\alpha)$ $\tan(\beta) = \tan(\pi - \alpha) = -\tan(\alpha)$

$\tan(\beta) = \frac{3}{4} = \frac{3}{4} \rightarrow \tan(\alpha) = -\frac{3}{4}$

$2\pi \times \frac{1}{2} = \pi - 2\pi = -\pi \rightarrow \sin(\pi) = 0$
 $1 \times \frac{1}{2} = \frac{1}{2} \times \pi = \frac{\pi}{2} \rightarrow \sin(\frac{\pi}{2}) = 1$
 $2 \times \frac{1}{2} = 1 \times \pi = \pi \rightarrow \sin(\pi) = 0$
 $2 \times \frac{1}{2} = 1 \times \pi = \pi \rightarrow \cos(\pi) = -1$
 $\frac{-\sin(\pi) - \sin(\pi)}{-\sin(\pi) - \sin(\pi)} = \frac{0}{0}$
 $\frac{-\sin(\pi) - \sin(\pi)}{-\sin(\pi) - \sin(\pi)} = \frac{0}{0}$

نوعی

$$\cos \alpha < \frac{r}{c} \rightarrow \cos^2 \alpha + \sin^2 \alpha = 1 \rightarrow \frac{r^2}{c^2} + \sin^2 \alpha = 1 \rightarrow \sin^2 \alpha = \frac{c^2 - r^2}{c^2} \rightarrow \sin \alpha = \pm \frac{\sqrt{c^2 - r^2}}{c}$$

$$1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha} \rightarrow \frac{1}{c^2} + \tan^2 \alpha = \frac{1}{\frac{r^2}{c^2}} \rightarrow \tan^2 \alpha = \frac{c^2 - r^2}{r^2} \rightarrow \tan \alpha = \pm \frac{\sqrt{c^2 - r^2}}{r}$$

$$\frac{\cos(\alpha) - \sin(\frac{\pi}{2} + \alpha)}{\sin(\frac{\pi}{2} + \alpha) - \sin(\pi - \alpha)} = \frac{(\frac{r}{c} + \frac{\sqrt{c^2 - r^2}}{r})}{\frac{1}{r}} = \frac{1 + c\sqrt{c^2 - r^2}}{r}$$

$\sin^2 \alpha + \cos^2 \alpha < 1$, $\sin^2 \alpha + \cos^2 \alpha \rightarrow \sin^2 \alpha < \cos^2 \alpha$
 $\sin(\alpha) < \cos(\alpha) \rightarrow \cos(\alpha) > \sin(\alpha) \rightarrow \cos(\alpha) > \frac{\sqrt{c^2 - r^2}}{c}$
 $\cos(\alpha) = \frac{-\sqrt{c^2 - r^2}}{c}$

بزرگتر از زاویه α

$\frac{-r}{m-1} = \tan \alpha \rightarrow \frac{-r}{m-1} = \tan \alpha = \frac{1}{\sqrt{c}}$
 $-r = \sqrt{c}m - \sqrt{c} \rightarrow \sqrt{c}m - \sqrt{c} - r = 0 \rightarrow m_1 = \frac{-r + \sqrt{c}}{\sqrt{c}}$
 $m_2 = \frac{-r - \sqrt{c}}{\sqrt{c}}$
 $m_1 - m_2 = \frac{-r + \sqrt{c} + r + \sqrt{c}}{\sqrt{c}} = \frac{2\sqrt{c}}{\sqrt{c}} = 2$

$\frac{\pi}{c} > \frac{\pi}{c} - \alpha > 0$
 $\tan \frac{\pi}{c} > \tan(\frac{\pi}{c} - \alpha) > 0$
 $\tan \frac{\pi}{c} > \frac{1}{\sqrt{c}}$
 $\tan \alpha < \frac{1}{\sqrt{c}}$
 $\frac{1}{\sqrt{c}} < \frac{1}{\sqrt{c+m}} \rightarrow -\sqrt{c} < 1$

$\cos \alpha = \frac{r}{c} \rightarrow \tan \cos \alpha = -\sqrt{c}$
 $\sin \alpha = \frac{\sqrt{c^2 - r^2}}{c}$
 $\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{\frac{\sqrt{c^2 - r^2}}{c}}{\frac{r}{c}} = \frac{\sqrt{c^2 - r^2}}{r}$
 $-\sqrt{c} \times \frac{\sqrt{c^2 - r^2}}{r} = \frac{r}{r}$
 $\frac{r}{r} - \frac{r}{r} = 0 = \tan(\pi - \alpha) \times \cos(\pi - \alpha) + \sin(\pi - \alpha) \times \sin(\pi - \alpha)$