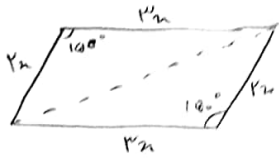


B

المساحة المثلثية



$$S_{\square} = S_{\triangle} = r_1 \frac{1}{2} r_2 \sin 100^\circ = \omega \epsilon$$

$$\Rightarrow \frac{1}{2} r_1 r_2 = \omega \epsilon \Rightarrow r_2 = \frac{2\omega \epsilon}{r_1} \Rightarrow r_2 = 1 \Rightarrow r_2 = \sqrt{2}$$

$$P = r_1 + r_2 + r_1 + r_2 = 1 + \sqrt{2} = \sqrt{2} \sqrt{2} \checkmark$$

(2)

$$S_{ABC} = \frac{1}{2} \times \omega \times V \times \sin A = \frac{1}{2} \omega V \sin \hat{A}$$

$$S_{ADE} = \frac{1}{2} \times \epsilon \times V \times \sin A = \frac{1}{2} \epsilon V \sin \hat{A}$$

$$S_{ABC} = S_{ADE} \Rightarrow \frac{1}{2} \omega V \sin A = \frac{1}{2} \epsilon V \sin A \Rightarrow \sin A = \frac{\epsilon}{\omega}$$

$$\Rightarrow \hat{A} = 30^\circ \quad \tan 30^\circ = \tan A = \frac{1}{\sqrt{3}} \checkmark$$

(2)

$$\frac{1}{\sqrt{\cos \alpha}} - \tan \alpha = \frac{1 + \sin \alpha}{|\cos \alpha|} \Rightarrow \frac{1}{|\cos \alpha|} - \tan \alpha = \frac{1 + \sin \alpha}{|\cos \alpha|} \Rightarrow \frac{1}{|\cos \alpha|} - \frac{\sin \alpha}{|\cos \alpha|} = \frac{1 + \sin \alpha}{|\cos \alpha|}$$

$$\Rightarrow -\frac{\sin \alpha}{\cos \alpha} = \frac{\sin \alpha}{|\cos \alpha|} \Rightarrow |\cos \alpha| = -\cos \alpha \Rightarrow \cos \alpha < 0$$

$$\frac{|\sin \alpha|}{\cos \alpha} = -\frac{1}{\cot \alpha} \Rightarrow \frac{|\sin \alpha|}{\cos \alpha} = -\frac{\sin \alpha}{\cos \alpha} \Rightarrow |\sin \alpha| = -\sin \alpha \Rightarrow \sin \alpha < 0$$

(2)

$$\tan(\pi - \alpha) = \frac{r}{\epsilon} = \frac{r}{\epsilon}$$

$$\tan(\frac{\pi}{2} - \alpha) = \cot \alpha \quad \tan(\pi - \alpha) = -\tan \alpha$$

$$-\tan \alpha = \frac{r}{\epsilon} \Rightarrow \tan \alpha = -\frac{r}{\epsilon} \Rightarrow \cot \alpha = \frac{-\epsilon}{r} \checkmark$$

(2)

$$\frac{r \cos(\pi - \alpha) - r \sin(\frac{\pi}{2} - \alpha)}{\sin(\frac{\pi}{2} - \alpha) - \cos(\pi - \alpha)} = \frac{r \cos(\pi - \alpha) - r \sin(\frac{\pi}{2} - \alpha)}{\sin(\frac{\pi}{2} - \alpha) - \cos(\pi - \alpha)} = \frac{-r \sin \alpha - r \cos \alpha}{\cos \alpha - (-\cos \alpha)} = \frac{-r(\sin \alpha + \cos \alpha)}{2 \cos \alpha} = \frac{-\omega}{2 \cos \alpha} = \frac{\omega}{2} \checkmark$$

(2)

$$\frac{\pi}{4} < \alpha < \frac{\pi}{2} \quad \cos \alpha = \frac{r}{\epsilon}$$

$$\Rightarrow \frac{\sin(\frac{\pi}{4} + \alpha) - \sin(\alpha - \frac{\pi}{4})}{|\tan \alpha - 1|} = \frac{\cos \alpha + \sin \alpha}{\frac{\omega}{\epsilon} - 1} = \frac{\frac{r}{\epsilon} - \frac{\sqrt{\omega}}{\epsilon}}{\frac{1}{\epsilon}} = \frac{\epsilon(r - \sqrt{\omega})}{\epsilon} \checkmark$$

(2)

$$\sin \alpha = r \cos \alpha \Rightarrow \cos \alpha = \frac{1}{r} \Rightarrow \tan \alpha = r$$

$$\frac{1}{\cos^2 \alpha} = 1 + \tan^2 \alpha \Rightarrow \frac{1}{\cos^2 \alpha} = 1 + r^2 \Rightarrow \cos \alpha = \frac{1}{\sqrt{1+r^2}} \Rightarrow \cos \alpha = \frac{-\sqrt{\omega}}{\omega} \checkmark$$

(2)

$$r m n + (m^2 - 1) y = r \quad \tan 45^\circ = \sqrt{r}$$

$$\frac{-r m}{m^2 - 1} = \sqrt{r} \Rightarrow \sqrt{r} m^2 + r m - \sqrt{r} = 0 \Rightarrow |m_1 - m_2| = \frac{\sqrt{\Delta}}{|a|} = \frac{\sqrt{4r}}{\sqrt{r}} = \frac{2}{\sqrt{r}} \checkmark$$

(2)

$$-\frac{\pi}{2} < x < \frac{\pi}{2} \quad \tan(\frac{\pi}{2} - x) = \frac{1-m}{r+m}$$

$$\Rightarrow 0 < \tan(\frac{\pi}{2} - x) \Rightarrow 0 < \frac{1-m}{r+m} \Rightarrow \frac{-r}{-1+1} \Rightarrow -r < m < 1 \checkmark$$

(2)

$$\tan(\frac{\pi}{4}) \cos(\frac{\pi}{4}) + \tan(\frac{\pi}{4}) \sin(\frac{\pi}{4}) = -\tan 45^\circ \times (-\cos 45^\circ) + (-\tan 45^\circ \times \sin 45^\circ)$$

$$= (-\sqrt{r} \times \frac{-\sqrt{r}}{r}) + (-\sqrt{r} \times \frac{\sqrt{r}}{r}) = \frac{r}{r} - \frac{r}{r} = 0 \checkmark$$

(2)