



$\frac{1}{\sqrt{2}} \times \sqrt{2} \times \sin \alpha = \frac{1}{2} \rightarrow \sin \alpha = \frac{1/2}{1/\sqrt{2}} = \frac{1/2 \times \sqrt{2}}{1/\sqrt{2}} = \frac{\sqrt{2}}{2} = \frac{1}{\sqrt{2}}$

$\sin \alpha = \frac{1}{\sqrt{2}} \begin{cases} \alpha = 45^\circ \\ \alpha = 135^\circ \end{cases} \quad \frac{1/2}{1/\sqrt{2}} = \frac{1}{\sqrt{2}} \checkmark$

  $\tan \alpha = \frac{p}{q} = 1 \rightarrow \alpha = 45^\circ$

$\tan(\alpha + \epsilon) = \frac{p}{q} = 1 \quad \tan(\alpha + \epsilon) = \frac{\tan \alpha + \tan \epsilon}{1 - \tan \alpha \tan \epsilon}$

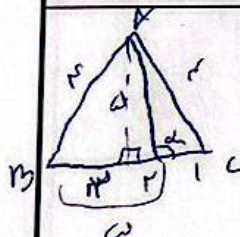
$\frac{\tan \alpha + 1}{1 - \tan \alpha} = 1 \rightarrow \tan \alpha + 1 = 1 - \tan \alpha \rightarrow \tan \alpha = 0 \rightarrow \alpha = 0^\circ$

  $\tan(\alpha) = \frac{p}{q}$

$\tan(\alpha) = \frac{p}{q} \quad \tan \alpha = \frac{p}{q} \quad \left| \tan \alpha = \frac{p}{q} < \frac{1}{p} \rightarrow \cot \alpha = \frac{1}{\tan \alpha} > p \right.$

$\tan(\alpha) = \frac{p}{q} \quad \tan(\alpha + \epsilon) = \frac{\tan \alpha + \tan \epsilon}{1 - \tan \alpha \tan \epsilon} = \frac{p/q + 1}{1 - p/q} = \frac{p+q}{q-p}$

$\frac{p+q}{q-p} = \frac{p}{q} \rightarrow q - \frac{p^2}{q} = \frac{p^2}{q} \rightarrow q - \frac{p^2}{q} = \frac{p^2}{q} \rightarrow q = \frac{2p^2}{q} \rightarrow q^2 = 2p^2 \rightarrow q = \sqrt{2}p$

  $\tan(180^\circ - \alpha) = \frac{p}{q} = \frac{p}{q}$

$\tan(180^\circ) = \frac{0}{1} = 0$

$\frac{0 - \tan \alpha}{1 + 0} = \frac{p}{q} \rightarrow \tan \alpha = -\frac{p}{q}$

$\sin^2 \alpha + \cos^2 \alpha + \sin^2 \alpha = \frac{5}{4} \rightarrow 1 + \sin^2 \alpha = \frac{5}{4} \rightarrow \sin^2 \alpha = \frac{1}{4} \rightarrow \sin \alpha = \frac{1}{2}$

$\sin^2 \alpha + \cos^2 \alpha = 1 \rightarrow \frac{1}{4} + \cos^2 \alpha = 1 \rightarrow \cos^2 \alpha = \frac{3}{4} \rightarrow \cos \alpha = \frac{\sqrt{3}}{2}$

$\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{1/2}{\sqrt{3}/2} = \frac{1}{\sqrt{3}}$

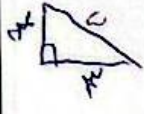
$$\sin^x + \cos^x = (1 - \cos^x)^x + \cos^x \Rightarrow 1 + \cos^x - x \cos^{x-1} + \cos^x = 1 + \cos^x + x \cos^x$$

$$\cos^x + \sin^x = (1 - \sin^x)^x + \sin^x \Rightarrow 1 + \sin^x - x \sin^{x-1} + \sin^x = 1 + \sin^x + x \sin^x$$

$$\frac{(1 + \cos^x)^x - (1 + \sin^x)^x}{1 + \cos^x} = 1 + \cos^x - 1 - \sin^x = \cos^x - \sin^x = 1 - \sin^x - \sin^x = 1 - 2\sin^x$$

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$$\sin\left(\frac{\pi}{4} + \alpha\right) \cos\left(\frac{\pi}{4} + \alpha\right) - \tan\left(\frac{\pi}{4} + \alpha\right) =$$

$$\cos(\alpha) \cdot \sin(\alpha) - \sin(\alpha) + \cos(\alpha)$$


$$\sin \alpha = \frac{1}{2}, \cos \alpha = -\frac{\sqrt{3}}{2}$$

$$-\frac{1}{2} \times \frac{1}{2} + \frac{\sqrt{3}}{2} = -\frac{1}{4} + \frac{\sqrt{3}}{2}$$

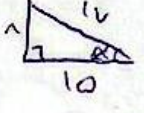
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$$\sqrt{x} \sin x - \sqrt{x} \cos x = \sqrt{x} (\sin x - \cos x) = \sqrt{x} (\sqrt{x} \sin(\frac{x}{\sqrt{x}} - \frac{\pi}{2}))$$

$$\Rightarrow \sqrt{x} \sin\left(\frac{\pi}{14} - \frac{\pi}{2}\right) = \sqrt{x} \sin\left(-\frac{7\pi}{14}\right) = \sqrt{x} \sin\left(-\frac{\pi}{2}\right) = -1$$

$$\sqrt{x} \times \frac{\pi}{14} = \frac{\pi}{2} \Rightarrow \cos\left(\frac{\pi}{14}\right) = \frac{1}{\sqrt{x}} \Rightarrow \sqrt{x} = \frac{1}{\cos\left(\frac{\pi}{14}\right)}$$

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
$$\tan(\alpha) = \frac{\tan\left(\frac{\alpha}{2}\right) + \tan\left(\frac{\alpha}{2}\right)}{1 - \tan\left(\frac{\alpha}{2}\right) \cdot \tan\left(\frac{\alpha}{2}\right)} = \frac{\frac{1}{2} + \frac{1}{2}}{1 - \frac{1}{2} \times \frac{1}{2}} = \frac{1}{\frac{3}{4}} = \frac{4}{3}$$


$$\sin \alpha = \frac{4}{5}, \cos \alpha = \frac{3}{5}$$

$$\frac{\frac{4}{5} - \frac{3}{5}}{\frac{4}{5} - \frac{3}{5}} = \frac{\frac{1}{5}}{\frac{1}{5}} = 1$$

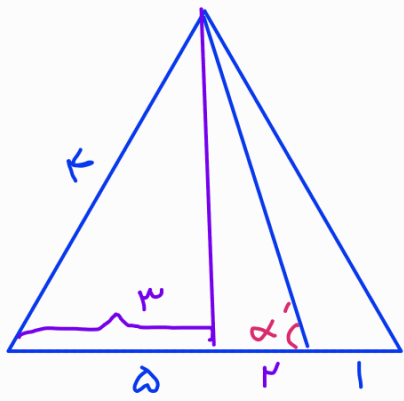
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$$0 < \frac{\cos}{\sin} \Rightarrow 0 < \frac{\cos}{\sin} \Rightarrow \cos > 0$$

$$\cos > 0, \sin < 0$$


$$\sin \alpha < \sqrt{\sin \alpha} \cos \alpha \Rightarrow \sin \alpha < \sin \alpha \cos \alpha$$

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$$h = \sqrt{14 - 9} = \sqrt{5}$$

$$\tan \alpha' = \frac{\sqrt{5}}{r}$$

$$\tan \alpha = -\tan \alpha' = -\frac{\sqrt{5}}{r}$$

-r