


۲۰ آفرین!

۱- (۲) $\cot \alpha = \frac{\cos \alpha}{\sqrt{1-\cos^2 \alpha}} \Rightarrow \frac{\cos \alpha}{\sin \alpha} = \frac{\cos \alpha}{|\sin \alpha|} \Rightarrow \sin \alpha > 0$ یعنی α در ربع اول و دوم

$\frac{1}{|\cos \alpha|} - \frac{\sin \alpha}{\cos^2 \alpha} = \frac{1}{|\cos \alpha|} - \frac{\sin \alpha}{\cos \alpha} \Rightarrow \cos \alpha > 0$ یعنی α در ربع اول و چهارم

۲- (۲) $-\frac{\pi}{12} < \alpha < \frac{\omega \pi}{12} \Rightarrow -\frac{\pi}{4} < 2\alpha < \frac{\omega \pi}{6} \Rightarrow -\frac{1}{2} < \sin 2\alpha < 1$

$\Rightarrow -\frac{1}{2} < \frac{m-1}{2} \leq 1 \Rightarrow -2 < m-1 \leq 4 \Rightarrow -1 < m \leq 5$ [-۱، ۵]

۳- (۲) $\frac{\pi}{4} < \alpha < \frac{3\pi}{4} \Rightarrow \frac{\sqrt{2}}{2} < \alpha < \frac{\pi}{2}$ 

$\tan \alpha + \cot \alpha = -3 \Rightarrow \frac{\sin \alpha}{\cos \alpha} + \frac{\cos \alpha}{\sin \alpha} = -3 \Rightarrow \frac{\sin^2 \alpha + \cos^2 \alpha}{\sin \alpha \cos \alpha} = -3$

$\frac{1}{\sin \alpha \cos \alpha} = -3 \Rightarrow \sin \alpha \cos \alpha = -\frac{1}{3}$

$(\sin \alpha + \cos \alpha)^2 = \sin^2 \alpha + \cos^2 \alpha + 2 \sin \alpha \cos \alpha = 1 - \frac{2}{3} = \frac{1}{3} = (\sin \alpha + \cos \alpha)^2$

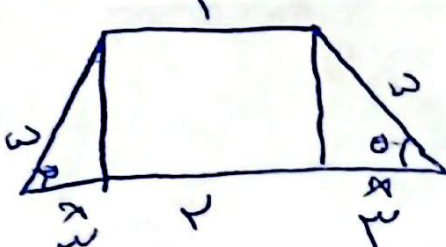
$\Rightarrow \sin \alpha + \cos \alpha = -\frac{\sqrt{3}}{2}$

$\frac{1}{\sin^2 \alpha + \cos^2 \alpha} = \frac{1}{(\sin \alpha + \cos \alpha)(\sin^2 \alpha + \cos^2 \alpha - \sin \alpha \cos \alpha)}$

$\Rightarrow \frac{1}{(-\frac{\sqrt{3}}{2})(1 + \frac{1}{3})} = \frac{1}{-\frac{2\sqrt{3}}{3}} = -\frac{3}{2\sqrt{3}} = -\frac{\sqrt{3}}{2}$ $-\frac{\sqrt{3}}{2}$

۴- (۲) $\cos \theta = \frac{9}{10} \Rightarrow \frac{9}{10} = \frac{a}{5} \Rightarrow a = 9$

$\sin \theta = \frac{4}{5} = \frac{(a+b)}{5} \Rightarrow \frac{4}{5} = \frac{9+b}{5} \Rightarrow 4 = 9+b \Rightarrow b = -5$ $\frac{4}{5}$



$$\tan\left(\frac{\pi}{2} + 15^\circ\right) \times -\tan\left(\pi - 15^\circ\right) - \left(\sin\left(\frac{\pi}{2} + 15^\circ\right) \times \cos\left(\frac{\pi}{2} - 15^\circ\right)\right) = k \cos 15^\circ$$

$$\Rightarrow -\cot 15^\circ \times \tan 15^\circ - (\sin 15^\circ \times -\sin 15^\circ) = k \cos^2 15^\circ$$

$$\Rightarrow -1 + \sin^2 15^\circ = k \cos^2 15^\circ \Rightarrow -\frac{(1 - \sin^2 15^\circ)}{\cos^2 15^\circ} = k \cos^2 15^\circ$$

$$\Rightarrow k = -1 \quad \checkmark$$

~~\Rightarrow [scribble]~~

$$\sqrt{3} \times \frac{\sqrt{\frac{3}{4}}}{\cos 45^\circ} \times \sin(45^\circ - 45^\circ) - (\sqrt{3} \times \frac{\sqrt{3}}{4} \times \cos(45^\circ - 45^\circ)) \quad (2)$$

$$\Rightarrow \frac{3\sqrt{3}}{4} \cos 90^\circ + \cos 90^\circ = \frac{3\sqrt{3}}{4} \cos 45^\circ = \frac{3\sqrt{3}}{4} \times \frac{1}{\sqrt{2}} = \frac{3\sqrt{6}}{4} = \frac{3}{4} = 1/\omega \quad (2)$$

$$f\left(\frac{\pi}{4}\right) = 14 \cos^2\left(\frac{\pi}{12}\right) \cos^2\left(\frac{\pi}{4}\right) \cos^2\left(\frac{\pi}{12}\right) \cos^2\left(\frac{\pi}{12}\right) \quad (2)$$

$$14 \times \cos^2\left(\frac{\pi}{12}\right) \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$$

$$\frac{\cos 2\alpha + 1}{2} = \cos^2 \alpha \Rightarrow \cos 2\alpha + 1 = 2 \cos^2 \alpha$$

$$\Rightarrow 14 \times \left(\cos\left(\frac{\pi}{12}\right) + 1\right) \times \frac{1}{4} = \frac{14}{4} \times \frac{1}{4} = \frac{14}{16} = \frac{7}{8} \quad (2)$$

$$\frac{1 - \sin x}{1 + \sin x} = \frac{1 - \sin x}{1 + \sin x} \Rightarrow 1 - \sin x = \frac{1 - \sin^2 x}{1 + \sin x} \Rightarrow \sin x = -\frac{1}{3} \quad (2)$$

$$1 - \sin^2 x = \cos^2 x = \cos x = 1 - \frac{1}{9} = \frac{8}{9} \Rightarrow \cos x = \frac{2\sqrt{2}}{3}$$

$$\tan \frac{x}{2} = \frac{\sin x}{1 + \cos x} \Rightarrow \tan \frac{x}{2} = \frac{-\frac{1}{3}}{1 + \frac{2\sqrt{2}}{3}} = \frac{-1}{3 + 2\sqrt{2}} = \frac{-1(3 - 2\sqrt{2})}{9 - 8} = -3 + 2\sqrt{2} \quad (2)$$

$$\frac{\sin \theta}{1 + \cos \theta} = \tan \frac{\theta}{2} \Rightarrow \frac{1 + \cos \theta}{\sin \theta} = \cot \frac{\theta}{2} \quad (2)$$

$$\frac{1 - \cos \theta}{\sin \theta} = \tan \frac{\theta}{2} \Rightarrow \frac{\sin \theta}{1 - \cos \theta} = \cot \frac{\theta}{2}$$

$$\frac{\sin \theta}{1 - \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = k \cot \frac{\theta}{2} \Rightarrow \cot \frac{\theta}{2} + \cot \frac{\theta}{2} = k \cot \frac{\theta}{2}$$

$$\Rightarrow k = 2 \quad (2)$$

$$1 - \sin^2 \alpha = \cos^2 \alpha \Rightarrow 1 - \frac{1}{100} = \cos^2 \alpha \Rightarrow \cos \alpha = -\frac{\sqrt{99}}{10} \quad -10$$

$$\cos\left(\frac{17\pi}{4} + \alpha\right) \Rightarrow \cos\left(7\pi + \frac{\pi}{4} + \alpha\right) \Rightarrow \cos\left(\frac{\pi}{4} + \alpha\right) \quad (2)$$

$$= \cos \frac{\pi}{4} \cos \alpha - \sin \frac{\pi}{4} \sin \alpha = \frac{\sqrt{2}}{2} \times -\frac{\sqrt{99}}{10} - \left(\frac{\sqrt{2}}{2} \times \frac{\sqrt{2}}{10}\right)$$

$$= \frac{\sqrt{2} \times \sqrt{2}}{20} = \frac{2}{20} = \frac{1}{10} - \frac{1}{10} = \boxed{0/10} \quad \checkmark$$