

$$\lim_{x \rightarrow 1} \frac{\sqrt{x} \cdot x - 1}{\sqrt{x+1} - 1} = \frac{0}{0} \quad \text{L'Hôpital's Rule} \quad \lim_{x \rightarrow 1} \frac{\sqrt{x} + x}{\sqrt{x+1} - 1} = \frac{1+1}{\sqrt{2}-1} = \frac{2}{\sqrt{2}-1} = \frac{2\sqrt{2}}{\sqrt{2}-1} \cdot \frac{\sqrt{2}+1}{\sqrt{2}+1} = \frac{2\sqrt{2}(\sqrt{2}+1)}{2-1} = 2\sqrt{2}(\sqrt{2}+1) = 4 + 2\sqrt{2}$$

$$\lim_{x \rightarrow 1} \frac{\sqrt{x+1} - 1}{\sqrt{x} - 1} = \frac{0}{0} \quad \text{L'Hôpital's Rule} \quad \lim_{x \rightarrow 1} \frac{\frac{1}{2\sqrt{x+1}}}{\frac{1}{2\sqrt{x}}} = \lim_{x \rightarrow 1} \frac{\sqrt{x}}{\sqrt{x+1}} = \frac{1}{\sqrt{2}}$$

$$\lim_{x \rightarrow \pi} \frac{1 + \cos^2 x}{\sin^2 x} = \frac{0}{0} \quad \text{L'Hôpital's Rule} \quad \lim_{x \rightarrow \pi} \frac{-2\cos x \sin x}{2\sin x \cos x} = \lim_{x \rightarrow \pi} \frac{-\cos x}{\cos x} = -1$$

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{1 - \tan x}{\sin x - \cos x} = \frac{0}{0} \quad \text{L'Hôpital's Rule} \quad \lim_{x \rightarrow \frac{\pi}{2}} \frac{-\sec^2 x}{\cos x + \sin x} = \frac{-1}{1} = -1$$

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\tan^2 x - 1}{\cos^2 x} = \frac{0}{0} \quad \text{L'Hôpital's Rule} \quad \lim_{x \rightarrow \frac{\pi}{2}} \frac{2 \tan x \sec^2 x}{-2\cos x} = \lim_{x \rightarrow \frac{\pi}{2}} \frac{\tan x \sec^2 x}{-\cos x} = \frac{1 \cdot 1}{-1} = -1$$