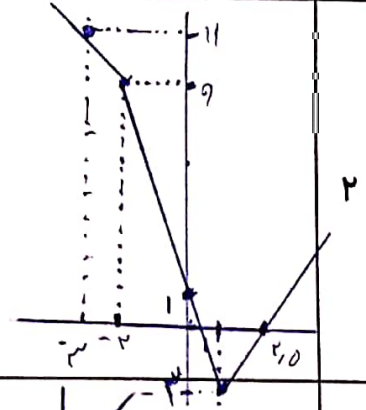


الف)
$$f(x) = \begin{cases} x + 2x - 1 = 3x - 1 & x \geq 1 \quad (1) \\ x - 2x + 1 = -x + 1 & x < 1 \quad (2) \end{cases}$$
 $R_f = 1 \cup 2 \Rightarrow [2, \infty) \cup (-1, \infty) =$
 $R_f = [2, \infty)$

ب)
$$f(x) = \begin{cases} x - 2 + x - 1 - x = -x - 1 & x \geq 1 \quad (1) \\ -2x + 2 + x - 1 - x = -x + 1 & 1 > x \geq 1 \quad (2) \\ -x + 2 - x + 1 - x = -3x + 3 & 1 > x \geq 0 \quad (3) \\ -x + 2 + x + 1 + x = x + 3 & x < 0 \quad (4) \end{cases}$$
 $R_f = 1 \cup 2 \cup 3 \cup 4$
 $R_f = [-1, \infty)$

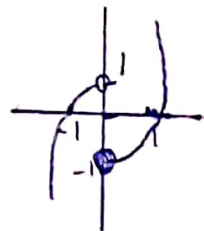
الف)
$$f(x) = \begin{cases} 2x - 2 - x - 2 = -x - 4 & x \geq 1 \\ -3x + 3 - x - 2 = -4x + 1 & 1 > x \geq -2 \\ -3x + 3 + x + 2 = -2x + 5 & x < -2 \end{cases}$$

 $K = -10$
 $-x - 4 = -10 \Rightarrow -x = -6 \Rightarrow x = 6$
 $-4x + 1 = -10 \Rightarrow -4x = -11 \Rightarrow x = 2.75$
 $-2x + 5 = -10 \Rightarrow -2x = -15 \Rightarrow x = 7.5$



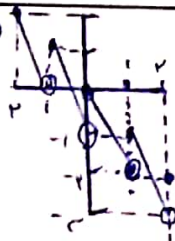
الف)
$$f(x) = \begin{cases} x + \frac{x}{x} = x + 1 & x > 0 \\ x + \frac{x}{-x} = x - 1 & x < 0 \end{cases}$$

ب)
$$f(x) = \begin{cases} x^2 - 1 & x > 0 \\ -x^2 + 1 & x < 0 \end{cases}$$



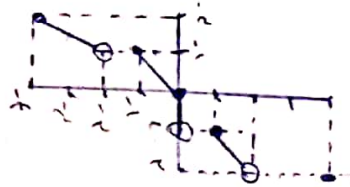
الف)
$$f(x) = \begin{cases} -2 - 2x & x \geq 1 \\ -1 - 2x & 0 < x < 1 \\ -2x & x < 0 \end{cases}$$

 $1 - 2x$ $1 > x \geq 1$ $1 - 2x = 1 \Rightarrow x = 0$



ب)
$$f(x) = \begin{cases} -2|x| & -1 > x \geq -2 \\ -|x| & 0 > x \geq -1 \\ |x| & x \geq 0 \end{cases}$$

 $|x|$ $x \geq 0$ $x^2 = x \Rightarrow x = 0$



الف)
$$\begin{cases} x \in \mathbb{Z} & x - [x] = 0 \quad (1) \\ x \notin \mathbb{Z} & x - [x] \in (0, 1) \quad (2) \end{cases}$$

 $(1) \cup (2) \Rightarrow R_f = [0, 1)$

ب)
$$f(x) = x - [x] \Rightarrow f([0, 1))$$

 $R_f = [0, 1)$

2.
$$0 \leq \left(\frac{x}{\omega} - \left[\frac{x}{\omega} \right] \right) \leq 1 \Rightarrow [0, 1)$$

3)
$$[x] - x \Rightarrow -(x - [x])$$

 $R_f = [0, 1) \Rightarrow [-1, 0]$

1) $a=3, b=1 \quad R_F = [-\sqrt{a^2+b^2}, \sqrt{a^2+b^2}] \Rightarrow R_F = [-\sqrt{10}, \sqrt{10}] = [-\sqrt{10}, \sqrt{10}]$ 2) $a=4, b=-2 \quad R_F = [-\sqrt{16+4}, \sqrt{16+4}] = [-\sqrt{20}, \sqrt{20}] \Rightarrow R_F = [-\sqrt{20}, \sqrt{20}]$ 3) $a=2, b=0 \quad R_F = [-\sqrt{4+0}, \sqrt{4+0}] = [-2, 2] \Rightarrow R_F = \{-2, -1, 0, 1, 2\}$ 4) $\cos(x) - 2\sin(x) = -2\sin(x) + \cos(x) \quad a = -2, b = 1 \quad R_F = [-\sqrt{4+1}, \sqrt{4+1}]$ $R_F = [-\sqrt{5}, \sqrt{5}] \Rightarrow R_F = [-\sqrt{5}, \sqrt{5}]$	6 7 8
الف) $\sin(x) = [-1, 1]$ $\frac{-b}{\sqrt{a^2+b^2}} = \frac{-2}{\sqrt{5}} \quad \frac{-2}{\sqrt{5}} \in [-1, 1]$ 1) $1+2+2=5 \quad -1 \rightarrow 1-2+2=1 \quad R_F = [0, 4]$ 2) $\sin(x) = [-1, 1]$ $\frac{-b}{\sqrt{a^2+b^2}} = \frac{-2}{\sqrt{5}} \in [-1, 1]$ $\frac{-2}{\sqrt{5}} \rightarrow 2(-\frac{2}{\sqrt{5}}) + 2(-\frac{2}{\sqrt{5}}) + 2 = \frac{2}{\sqrt{5}}$ 1) $2+2+2=6 \quad -1 \rightarrow 2-2+2=2 \quad R_F = [\frac{2}{\sqrt{5}}, 6]$	9 10
الف) $\sin^2 + \cos^2 = \sin^2 + \cos^2 + \cos^2 \rightarrow (1 + \cos^2) \cos^2 = [0, 1]$ ② 2) $1 \rightarrow 1 + [0, 1] \Rightarrow [1, 2]$ 3) $1 + \cos^2 = \frac{\sin^2}{\sin^2} + \frac{\cos^2}{\sin^2} = \frac{\sin^2 + \cos^2}{\sin^2} = \frac{1}{\sin^2}$ $\frac{1}{\sin^2} = \frac{1}{\sin^2} \times \sin^2 = \cos^2 \sin^2 \rightarrow \sin(2x) \rightarrow \sin(4x) = [-1, 1]$	11
الف) $(\sin^2 + \cos^2)(\sin^2 - \sin^2 \cos^2 + \cos^2) \rightarrow (1 - \sin^2 \cos^2 - \sin^2 \cos^2 + 1 - \sin^2 \cos^2)$ ① $\sin(2x) = 2\sin \cos \Rightarrow \sin^2 \cos^2 = \sin^2(x) \quad \frac{1}{2} \sin^2(x) + \sin^2 \cos^2(x) \quad 1, 2 \rightarrow 1 - \frac{1}{2} \sin^2(x)$ $\sin^2(x) = [0, 1] \rightarrow 1 \geq (1 - \frac{1}{2} \sin^2(x)) \geq \frac{1}{2} \rightarrow R_F = [\frac{1}{2}, 1]$ ② $(\sin^2 + \cos^2)^2 - 2\sin^2 \cos^2$ ② ① ② $\rightarrow (1 - 2\sin^2 \cos^2)^2 - \sin^2 \cos^2 = 1 - 2\sin^2 \cos^2$ ③ $(1 - \frac{1}{2} \sin^2(x))^2 - \frac{1}{2} \sin^2(x) \rightarrow 1 - \sin^2(x) + \frac{1}{4} \sin^4(x)$ $-\frac{b}{\sqrt{a^2+b^2}} = \frac{1}{2} \in [-1, 1] \quad -1 \rightarrow 1 - 0 = 1 \quad 1 \rightarrow 1 - 1 + \frac{1}{4} = \frac{1}{4} \quad R_F = [\frac{1}{4}, 1] \rightarrow \{0, 1\}$	12
الف) $\rightarrow \frac{(n-1)(n+1)}{n+1} \quad n \neq -1 \quad n-1 \rightarrow 2(-1) - 1 = -3 \rightarrow 3 \neq -1$ $R_F = \mathbb{R} - \{-1\}$ 2) $\frac{(n-1)(n^2+n+1)}{n-1} \quad n \neq 1 \quad n^2+n+1 \rightarrow 1+1+1=3 \neq 0$ 3) $\frac{-b}{\sqrt{a^2+b^2}} = -\frac{1}{2} \rightarrow (-\frac{1}{2})^2 + -\frac{1}{2} + 1 = \frac{1}{4} - \frac{1}{2} + 1 = \frac{3}{4} \quad R_F = [\frac{3}{4}, 3] \cup (3, \infty)$	13