

$$f(x) = \sqrt{1-x^2} \quad g(x) = \{(-1, 1), (0, 1), (1, 0), (1, 1)\}$$

$$D_f = 1-x^2 \geq 0 \quad \Rightarrow \quad 1 \geq x^2 \rightarrow 1 \geq x \geq -1 \rightarrow D_f \cap D_g = \{1, -1, 0\}$$

$$f(x) - g(x) = \{(-1, 1), (-1, 1), (0, 1), (1, 1)\} \quad R_{f-g} = \{1, 0, 1\}$$

$$f(x) = x-1 \quad g(x) = \frac{1}{x}x+r \quad R_f \cup R_g = [0, +\infty) \cup (-\infty, r]$$

$$R_f = [0, +\infty) \quad R_g = (-\infty, r]$$

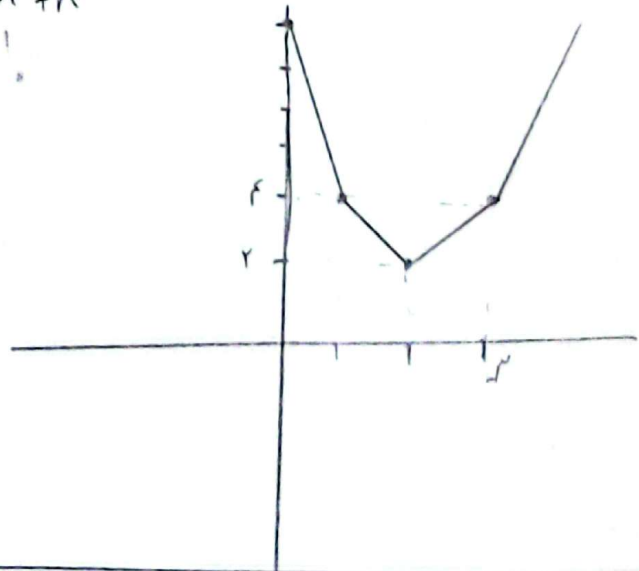
$$y = \frac{-x^2}{r} + x + r \quad \frac{-x^2}{r} + x + r > \frac{r}{r} \rightarrow -\frac{x^2}{r} + x + \frac{r}{r} > 0 \rightarrow x_1 = -1 \quad x_2 = r$$

$$(-1, r)$$

$$y = |x-1| + |x-r| + |r-x-1|$$

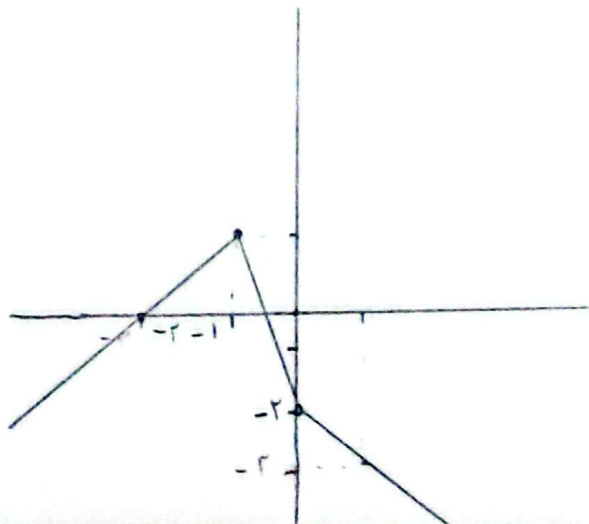
$$\boxed{y_{\min} = r}$$

$$\boxed{x = r}$$



$$y = |x| - r|x+1|$$

$$R_f = (-\infty, 1]$$



$$\frac{x^2 + ax + m}{x+1} = y \quad yx + y = x^2 + ax + m \rightarrow x^2 + (a-y)x + m - y$$

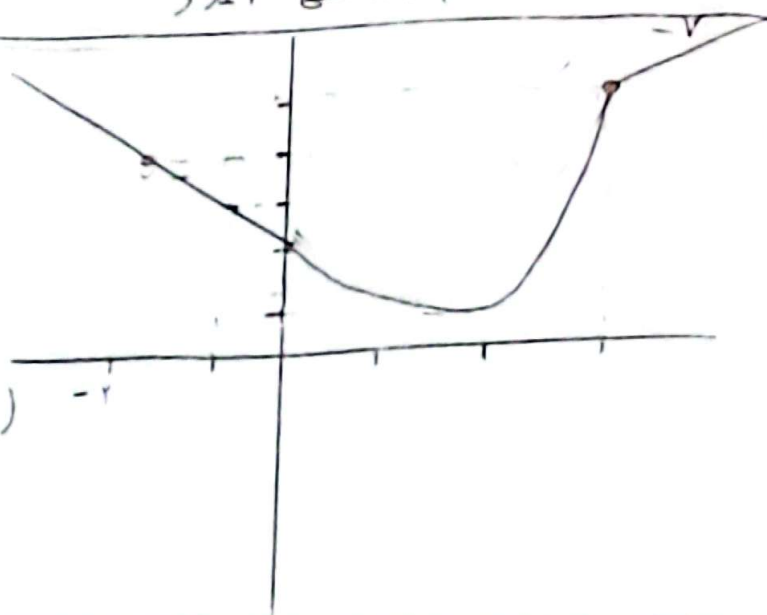
$$\Delta = y^2 - 4y + 4a - 4m \quad m - y = 0$$

$$x+1 \leftarrow m = y$$

$$f(x) = \begin{cases} x+r & x \geq r \\ x^2 \sqrt{x+r} & 0 \leq x < r \\ |x|+r & x < 0 \end{cases}$$

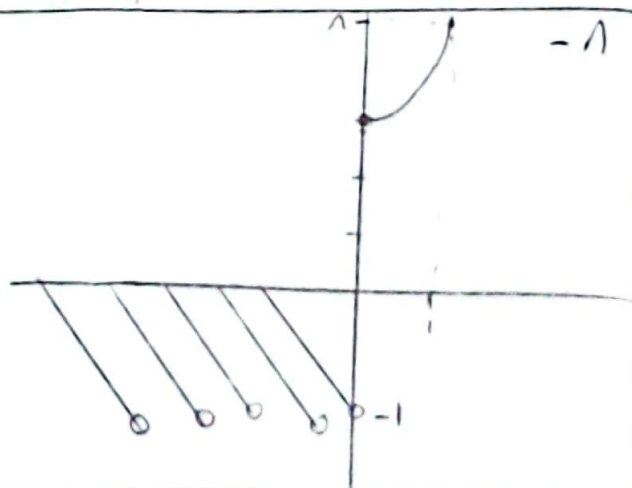
$$\frac{1}{r} = 1$$

$$1-r+r=1 \quad R = [1, +\infty)$$



$$f(x) = \begin{cases} x^2 + rx + r & x \leq 0 \\ [rx] - rx & x > 0 \end{cases}$$

$$(-1, 0] \cup [r, +\infty)$$



$$y = a + 1 - \sqrt{rx+r} \quad rx+r \geq 0 \quad b = \frac{r}{r}$$

$$a = a + 1 - \sqrt{-r+r} \quad (a = f) \quad rx - \frac{r}{r} = -y$$

$$I \quad x+1 \geq 0 \rightarrow x \geq -1 \quad I \cap II \rightarrow [-1, 1] \quad f(x) = r\sqrt{x+1} + r\sqrt{1-x}$$

$$II \quad 1-x \geq 0 \rightarrow 1 \geq x$$

$$f(x) + g(x) = r\sqrt{r+r\sqrt{1-x}}$$

$$r\sqrt{x+1} + r\sqrt{1-x} + g(x) = r\sqrt{r+r\sqrt{1-x}}$$

$$g(x) = r\sqrt{r+r\sqrt{1-x}} - r\sqrt{x+1} - r\sqrt{1-x}$$

$$y = \sqrt{x+1} + r\sqrt{1-x} - \sqrt{r\sqrt{1+x} + r\sqrt{1-x}}$$

$$y(-1) = \sqrt{r} \quad [0, \sqrt{r}]$$

$$y(1) = 0$$